

Package ‘BSL’

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Type Package

Title Bayesian Synthetic Likelihood

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Description

Bayesian synthetic likelihood (BSL, Price et al. (2018) <doi:10.1080/10618600.2017.1302882>) is an alternative to standard, non-parametric approximate Bayesian computation (ABC). BSL assumes a multivariate normal distribution for the summary statistic likelihood and it is suitable when the distribution of the model summary statistics is sufficiently regular. This package provides a Metropolis Hastings Markov chain Monte Carlo implementation of three methods (BSL, uBSL and semiBSL) and two shrinkage estimations (graphical lasso and Warton's estimation). uBSL (Price et al. (2018) <doi:10.1080/10618600.2017.1302882>) uses an unbiased estimator to the normal density. A semi-parametric version of BSL (semiBSL, An et al. (2018) <arXiv:1809.05800>) is more robust to non-normal summary statistics. Shrinkage estimations can help to bring down the number of simulations when the dimension of the summary statistic is high (e.g., BSLLasso, An et al. (2019) <doi:10.1080/10618600.2018.1537928>). Extensions to this package are planned.

Depends R (>= 3.4.0)

License GPL (>= 2)

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 'gaussianSynLikeGhuryeOlkin.R' 'imports.R' 'kernelCDF.R'
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 'semiparaKernelEstimate.R'

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BSL-package	<i>Bayesian synthetic likelihood</i>
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Description

Bayesian synthetic likelihood (BSL, Price et al (2018)) is an alternative to standard, non-parametric approximate Bayesian computation (ABC). BSL assumes a multivariate normal distribution for the summary statistic likelihood and it is suitable when the distribution of the model summary statistics is sufficiently regular.

In this package, a Metropolis Hastings Markov chain Monte Carlo (MH-MCMC) implementation of BSL is available. We also include implementations of three methods (BSL, uBSL and semiBSL) and two shrinkage estimations (graphical lasso and Warton's estimation).

Methods: (1) BSL (Price et al., 2018), which is the standard form of Bayesian synthetic likelihood, assumes the summary statistic is roughly multivariate normal; (2) uBSL (Price et al., 2018), which uses an unbiased estimator to the normal density; and (3) semiBSL (An et al. 2018), which relaxes the normality assumption to an extent and maintains the computational advantages of BSL without any tuning.

Shrinkage estimations are designed particularly to reduce the number of simulations if method is BSL or semiBSL: (1) graphical lasso (Friedman et al., 2008) finds a sparse precision matrix with a L1-regularised log-likelihood. (An et al., 2019) use graphical lasso within BSL to bring down the number of simulations significantly when the dimension of the summary statistic is high; and (2) Warton's estimator (Warton 2008) penalises the correlation matrix and is straightforward to compute.

Parallel computing is supported through the `foreach` package and users can specify their own parallel backend by using packages like `doParallel` or `doMC`. Alternatively a vectorised simulation function that simultaneously generates n simulation results is also supported.

The main functionality is available through

- `bsl`: The general function to perform BSL, uBSL, and semiBSL (with or without parallel computing).
- `selectPenalty`: A function to select the penalty for BSL and semiBSL.

Several examples have also been included. These examples can be used to reproduce the results of An et al. (2019), and can help practitioners learn how to use the package.

- `ma2`: The MA(2) example from An et al. (2019).
- `mgnk`: The multivariate G&K example from An et al. (2019).
- `cell`: The cell biology example from Price et al. (2018) and An et al. (2019).

Extensions to this package are planned.

Author(s)

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References

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- An, Z., South, L. F., Nott, D. J. & Drovandi, C. C. (2019). Accelerating Bayesian synthetic likelihood with the graphical lasso. *Journal of Computational and Graphical Statistics*. <https://doi.org/10.1080/10618600.2018.1537928>
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- Warton, D. I. (2008). Penalized Normal Likelihood and Ridge Regularization of Correlation and Covariance Matrices, *Journal of the American Statistical Association*. <https://doi.org/10.1198/016214508000000021>

bsl

Performing BSL, BSLasso and semiBSL

Description

This is the main function for performing MCMC BSL, MCMC uBSL, MCMC BSLasso and MCMC semiBSL. Parallel computing is supported with the R package foreach. Several input arguments in 2.0.0 or earlier versions are replaced by model in the new update and will be deprecated in a future release.

Usage

```
bsl(y, n, M, model, covRandWalk, theta0, fnSim, fnSum, method = c("BSL",
  "uBSL", "semiBSL")[1], shrinkage = NULL, penalty = NULL,
  fnPrior = NULL, simArgs = NULL, sumArgs = NULL,
  logitTransformBound = NULL, standardise = FALSE, GRC = FALSE,
  parallel = FALSE, parallelArgs = NULL, thetaNames = NULL,
  plotOnTheFly = FALSE, verbose = FALSE)
```

Arguments

y	The observed data. Note this should be the raw dataset NOT the set of summary statistics.
n	The number of simulations from the model per MCMC iteration for estimating the synthetic likelihood.
M	The number of MCMC iterations.
model	A “BSLMODEL” object generated with function <code>BSLModel</code> . See BSLModel .
covRandWalk	The covariance matrix of a multivariate normal random walk proposal distribution used in the MCMC.

theta0	Deprecated, will be removed in the future, use <code>model</code> instead. Initial guess of the parameter value, which is used as the starting value for MCMC.
fnSim	Deprecated, will be removed in the future, use <code>model</code> instead. A function that simulates data for a given parameter value. The first argument should be the parameters. Other necessary arguments (optional) can be specified with <code>simArgs</code> .
fnSum	Deprecated, will be removed in the future, use <code>model</code> instead. A function for computing summary statistics of data. The first argument should be the observed or simulated dataset. Other necessary arguments (optional) can be specified with <code>sumArgs</code> .
method	A string argument indicating the method to be used. The default, “BSL”, runs standard BSL. “uBSL” uses the unbiased estimator of a normal density of Ghurye and Olkin (1969). “semiBSL” runs the semi-parametric BSL algorithm and is more robust to non-normal summary statistics.
shrinkage	A string argument indicating which shrinkage method to be used. The default is <code>NULL</code> , which means no shrinkage is used. Shrinkage estimation is only available for method “BSL” and “semiBSL”. Current options are “glasso” for the graphical lasso method of Friedman et al (2008) and “Warton” for the ridge regularisation method of Warton (2008).
penalty	The penalty value to be used for the specified shrinkage method. Must be between zero and one if the shrinkage method is “Warton”.
fnPrior	Deprecated, will be removed in the future, use <code>model</code> instead. A function that computes the log of prior density for a parameter. The default is <code>NULL</code> , which uses an improper flat prior over the real line for each parameter. The function must have a single input: a vector of parameter values.
simArgs	Deprecated, will be removed in the future, use <code>model</code> instead. A list of additional arguments to pass into the simulation function. Only use when the input <code>fnSim</code> requires additional arguments. The default is <code>NULL</code> .
sumArgs	Deprecated, will be removed in the future, use <code>model</code> instead. A list of additional arguments to pass into the summary statistics function. Only use when the input <code>fnSum</code> requires additional arguments. The
logitTransformBound	A p by 2 numeric matrix indicating the upper and lower bound of parameters if a logit transformation is used on the parameter space, where p is the number of parameters. The default is <code>NULL</code> , which means no logit transformation is used. It is also possible to define other transformations with <code>fnSim</code> and <code>fnPrior</code> . The first column contains the lower bound of each parameter and the second column contains the upper bound. Infinite lower or upper bound is also supported, e.g. <code>matrix(c(1, Inf, 0, 10, -Inf, 0.5), 3, 2, byrow=TRUE)</code> .
standardise	A logical argument that determines whether to standardise the summary statistics before applying the graphical lasso. This is only valid if <code>method</code> is “BSL”, <code>shrinkage</code> is “glasso” and <code>penalty</code> is not <code>NULL</code> . The diagonal elements will not be penalised if the shrinkage method is “glasso”. The default is <code>FALSE</code> .
GRC	A logical argument indicating whether the Gaussian rank correlation matrix (Boudt et al., 2012) should be used to estimate the covariance matrix in “BSL” method. The default is <code>FALSE</code> , which uses the sample covariance by default.

<code>parallel</code>	A logical value indicating whether parallel computing should be used for simulation and summary statistic evaluation. The default is FALSE. When model simulation is fast, it may be preferable to perform serial computations to avoid significant communication overhead between workers.
<code>parallelArgs</code>	A list of additional arguments to pass into the <code>foreach</code> function. Only used when parallel computing is enabled, default is NULL.
<code>thetaNames</code>	Deprecated, will be removed in the future, use <code>model</code> instead. A string vector of parameter names, which must have the same length as the parameter vector. The default is NULL.
<code>plotOnTheFly</code>	A logical or numeric argument defining whether or by how many iterations a posterior figure will be plotted during running. If TRUE, a plot of approximate univariate posteriors based on the current accepted samples will be shown by every one thousand iterations. The default is FALSE.
<code>verbose</code>	A logical argument indicating whether the iteration numbers (1 : M) and accepted proposal flags should be printed to track progress. The default is FALSE.

Value

An object of class `bsl` is returned, containing the following components:

- `theta`: MCMC samples from the joint approximate posterior distribution of the parameters.
- `loglike`: Accepted MCMC samples of the estimated log-likelihood values.
- `call`: The original code that was used to call the method.
- `model`: The “BSLMODEL” object.
- `acceptanceRate`: The acceptance rate of the MCMC algorithm.
- `earlyRejectionRate`: The early rejection rate of the algorithm (early rejection may occur when using bounded prior distributions).
- `errorRate`: The error rate. If any infinite summary statistic or positive infinite loglike occurs during the process, it is marked as an error and the proposed parameter will be rejected.
- `y`: The input observed data.
- `n`: The number of simulations from the model per MCMC iteration.
- `M`: The number of MCMC iterations.
- `covRandWalk`: The covariance matrix used in multivariate normal random walk proposals.
- `method`: The string argument indicating the used method.
- `shrinkage`: The string argument indicating the shrinkage method.
- `penalty`: The penalty value.
- `standardise`: Logical, whether to standardise the summary statistics.
- `GRC`: Logical, if Gaussian rank correlation matrix is used.
- `logitTransform`: Logical, whether a logit transformation is used in the algorithm.
- `logitTransformBound`: The matrix of `logitTransformBound`.
- `parallel`: Logical, whether parallel computing is used in the process.
- `parallelArgs`: The list of additional arguments to pass into the `foreach` function.
- `time`: The running time of class `difftime`.

Author(s)

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References

- Price, L. F., Drovandi, C. C., Lee, A., & Nott, D. J. (2018). Bayesian synthetic likelihood. *Journal of Computational and Graphical Statistics*. <https://doi.org/10.1080/10618600.2017.1302882>
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See Also

`ma2`, `cell` and `mgnk` for examples. `selectPenalty` for a function to tune the BSLasso tuning parameter and `plot` for functions related to visualisation.

bsl-class

S4 class “bsl”.

Description

The result from function `bsl` is saved as class “BSL”.

Summarise a “bsl” class object.

Plot the univariate marginal posterior plot of a “bsl” class object.

Usage

```
## S4 method for signature 'bsl'
show(object)

summary(object, ...)
```

```

## S4 method for signature 'bsl'
summary(object, thetaNames = NULL)

plot(x, y, ...)

## S4 method for signature 'bsl,missing'
plot(x, which = 1L, thin = 1,
      thetaTrue = NULL, options.plot = NULL,
      top = "Approximate Univariate Posteriors", options.density = list(),
      options.theme = list())

```

Arguments

object	A “bsl” class object to be displayed.
...	Other arguments.
thetaNames	Parameter names to be shown in the summary table. If not given, parameter names of the “bsl” object will be used by default.
x	A “bsl” class object to plot.
y	Ignore.
which	An integer argument indicating which plot function to be used. The default, 1L, uses the plain plot to visualise the result. 2L uses ggplot2 to draw the plot.
thin	A numeric argument indicating the gap between samples to be taken when thinning the MCMC draws. The default is 1, which means no thinning is used.
thetaTrue	A set of values to be included on the plots as a reference line. The default is NULL.
options.plot	A list of additional arguments to pass into the plot function. Only use when which is 1L.
top	A character argument of the combined plot title if which is 2L.
options.density	A list of additional arguments to pass into the geom_density function. Only use when which is 2L.
options.theme	A list of additional arguments to pass into the theme function. Only use when which is 2L.

Value

A vector of the number of simulations per iteration, acceptance rate of the Markov chain and scaled effective sample size for each parameter.

Methods (by generic)

- **show:** Display the basic information of a “bsl” object. See [show.bsl](#).
- **summary:** Summarise a bsl class object. See [summary.bsl](#).
- **plot:** Plot the univariate marginal posterior plot of a “bsl” class object. See [plot.bsl](#).

Slots

theta Object of class “matrix”. MCMC samples from the joint approximate posterior distribution of the parameters.

loglike Object of class “numeric”. Accepted MCMC samples of the estimated log-likelihood values.

call Object of class “call”. The original code that was used to call the method.

model Object of class “BSLMODEL”.

acceptanceRate Object of class “numeric”. The acceptance rate of the MCMC algorithm.

earlyRejectionRate Object of class “numeric”. The early rejection rate of the algorithm (early rejection may occur when using bounded prior distributions).

errorRate Object of class “numeric”. The error rate. If any infinite summary statistic or positive infinite loglike occurs during the process, it is marked as an error and the proposed parameter will be rejected.

y Object of class “ANY”. The observed data.

n Object of class “numeric”. The number of simulations from the model per MCMC iteration.

M Object of class “numeric”. The number of MCMC iterations.

covRandWalk Object of class “matrix”. The covariance matrix used in multivariate normal random walk proposals.

method Object of class “character”. The character argument indicating the used method.

shrinkage Object of class “characterOrNULL”. The character argument indicating the shrinkage method.

penalty Object of class “numericOrNULL”. The penalty value.

GRC Object of class “logical”. Whether the Gaussian rank correlation matrix is used.

logitTransform Object of class “logical”. The logical argument indicating whether a logit transformation is used in the algorithm.

logitTransformBound Object of class “matrixOrNULL”. The matrix of logitTransformBound.

standardise Object of class “logical”. The logical argument that determines whether to standardise the summary statistics.

parallel Object of class “logical”. The logical value indicating whether parallel computing is used in the process.

parallelArgs Object of class “listOrNULL”. The list of additional arguments to pass into the foreach function.

time Object of class “difftime”. The running time.

BSLMODEL-class	<i>S4 class “BSLMODEL”</i>
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Description

The S4 class contains the simulation and summary statistics function and other necessary arguments for a model to run in the main bsl function.

`BSLModel` is the constructor function for a BSLMODEL object.

`initialize.BSLMODEL` initialises a “BSLMODEL” object.

`validBSLModelObject` check the validity of a “BSLMODEL” object.

Usage

```
BSLModel(fnSim, fnSimVec, fnSum, fnLogPrior, simArgs, sumArgs, theta0,
thetaNames, test = TRUE)

initialize.BSLMODEL(.Object, fnSim, fnSimVec, simArgs, fnSum, sumArgs,
fnLogPrior, theta0, thetaNames, test = TRUE)

validBSLModelObject(object)

## S4 method for signature 'BSLMODEL'
fn(.Object)

## S4 method for signature 'BSLMODEL'
setns(.Object)
```

Arguments

<code>fnSim</code>	A function that simulates data for a given parameter value. The first argument should be the parameters. Other necessary arguments (optional) can be specified with <code>simArgs</code> .
<code>fnSimVec</code>	A vectorised function that simulates a number of datasets simultaneously for a given parameter value. The first two arguments should be the number of simulations to run and parameters, respectively. Other necessary arguments (optional) can be specified with <code>simArgs</code> . The output must be a list of each simulation result.
<code>fnSum</code>	A function for computing summary statistics of data. The first argument should be the observed or simulated dataset. Other necessary arguments (optional) can be specified with <code>sumArgs</code> .
<code>fnLogPrior</code>	A function that computes the log of prior density for a parameter. If this is missing, the prior by default is an improper flat prior over the real line for each parameter. The function must have a single input: a vector of parameter values.
<code>simArgs</code>	A list of additional arguments to pass into the simulation function. Only use when the input <code>fnSim</code> requires additional arguments.

sumArgs	A list of additional arguments to pass into the summary statistics function. Only use when the input <code>fnSum</code> requires additional arguments.
theta0	Initial guess of the parameter value.
thetaNames	A string vector of parameter names, which must have the same length as the parameter vector.
test	Logical, whether a short simulation test will be ran upon initialisation.
.Object	A “BSLMODEL” object.
object	A “BSLMODEL” object.

Methods (by generic)

- `fn`: Generate the generic simulation and summary statistics function for `n` simulations and fixed `theta` (for internal use).
- `setns`: Find and set the length of summary statistics with a test run (for internal use).

Slots

`fnSim` A function that simulates data for a given parameter value. The first argument should be the parameters. Other necessary arguments (optional) can be specified with `simArgs`.

`fnSimVec` A vectorised function that simulates a number of datasets simultaneously for a given parameter value. If this is not `NULL`, vectorised simulation function will be used instead of `fnSim`. The first two arguments should be the number of simulations to run and parameters, respectively. Other necessary arguments (optional) can be specified with `simArgs`. The output must be a list of each simulation result.

`fnSum` A function for computing summary statistics of data. The first argument should be the observed or simulated dataset. Other necessary arguments (optional) can be specified with `sumArgs`. The users should code this function carefully so the output have fixed length and never contain any `Inf` value.

`fnLogPrior` A function that computes the log of prior density for a parameter. The default is `NULL`, which uses an improper flat prior over the real line for each parameter. The function must have a single input: a vector of parameter values.

`simArgs` A list of additional arguments to pass into the simulation function. Only use when the input `fnSim` or `fnSimVec` requires additional arguments. The default is `NULL`.

`sumArgs` A list of additional arguments to pass into the summary statistics function. Only use when the input `fnSum` requires additional arguments. The default is `NULL`.

`theta0` Initial guess of the parameter value, which is used as the starting value for MCMC.

`thetaNames` Expression, parameter names.

`ns` The number of summary statistics of a single observation. Note this will be generated automatically, thus is not required for initialisation.

`test` Logical indicator of whether a short simulation test will be ran upon initialisation.

Examples

```
data(ma2)
model <- BSLModel(fnSim = ma2_sim, fnSum = ma2_sum, simArgs = ma2$sim_options, theta0 = ma2$start,
                   fnLogPrior = ma2_logPrior)
isValidObject(model)
```

`cell`*Cell biology example*

Description

This example estimates the probabilities of cell motility and cell proliferation for a discrete-time stochastic model of cell spreading. We provide the data and tuning parameters required to reproduce the results in An et al. (2019).

Usage

```
cell_sim(theta, Yinit, rows, cols, sim_iters, num_obs)

cell_sum(Y, Yinit)

cell_prior(theta)

cell_logPrior(theta)
```

Arguments

<code>theta</code>	A vector of proposed model parameters, P_m and P_p .
<code>Yinit</code>	The initial matrix of cell presences of size <code>rows</code> by <code>cols</code> .
<code>rows</code>	The number of rows in the lattice (rows in the cell location matrix).
<code>cols</code>	The number of columns in the lattice (columns in the cell location matrix).
<code>sim_iters</code>	The number of discretisation steps to get to when an observation is actually taken. For example, if observations are taken every 5 minutes but the discretisation level is 2.5 minutes, then <code>sim_iters</code> would be 2. Larger values of <code>sim_iters</code> lead to more “accurate” simulations from the model, but they also increase the simulation time.
<code>num_obs</code>	The total number of images taken after initialisation.
<code>Y</code>	A <code>rows</code> by <code>cols</code> by <code>num_obs</code> array of the cell presences at times <code>1:num_obs</code> (not time 0).

Details

Cell motility (movement) and proliferation (reproduction) cause tumors to spread and wounds to heal. If we can measure cell proliferation and cell motility under different situations, then we may be able to use this information to determine the efficacy of different medical treatments.

A common method for measuring in vitro cell movement and proliferation is the scratch assay. Cells form a layer on an assay and, once they are completely covering the assay, a scratch is made to separate the cells. Images of the cells are taken until the scratch has closed up and the cells are in contact again. Each image can be converted to a binary matrix by forming a lattice and recording the binary matrix (of size `rows` x `cols`) of cell presences.

The model that we consider is a random walk model with parameters for the probability of cell movement (Pm) and the probability of cell proliferation (Pp) and it has no tractable likelihood function. We use the uninformative priors $Pm \sim U(0, 1)$ and $Pp \sim U(0, 1)$.

We have a total of 145 summary statistics, which are made up of the Hamming distances between the binary matrices for each time point and the total number of cells at the final time.

Details about the types of cells that this model is suitable for and other information can be found in Price et al. (2018) and An et al. (2019). Johnston et al. (2014) use a different ABC method and different summary statistics for a similar example.

A simulated dataset

An example “observed” dataset and the tuning parameters relevant to that example can be obtained using `data(cell)`. This “observed” data is a simulated dataset with $Pm = 0.35$ and $Pp = 0.001$. The lattice has 27 rows and 36 cols and there are `num_obs = 144` observations after time 0 (to mimic images being taken every 5 minutes for 12 hours). The simulation is based on there initially being 110 cells in the assay.

Further information about the specific choices of tuning parameters used in BSL and BSLasso can be found in An et al. (2019).

- `data`: The `rows x cols x num_obs` array of the cell presences at times 1:144.
- `sim_options`: Values of `sim_options` relevant to this example.
- `sum_options`: Values of `sum_options` relevant to this example, i.e. just the value of `Yinit`.
- `start`: A vector of suitable initial values of the parameters for MCMC.
- `cov`: The covariance matrix of a multivariate normal random walk proposal distribution used in the MCMC, in the form of a 2 by 2 matrix

Author(s)

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References

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Examples

```
require(doParallel) # You can use a different package to set up the parallel backend
# Loading the data for this example
```

```

data(cell)
model <- BSLModel(fnSim = cell_sim, fnSum = cell_sum, simArgs = cell$sim_options,
                    sumArgs = cell$sum_options, theta0 = cell$start, fnLogPrior = cell_logPrior,
                    thetaNames = expression(P[m], P[p]))
true_cell <- c(0.35, 0.001)

# Performing BSL (reduce the number of iterations M if desired)
# Opening up the parallel pools using doParallel
cl <- makeCluster(detectCores() - 1)
registerDoParallel(cl)
resultCellBSL <- bsl(cell$data, n = 5000, M = 10000, model = model, covRandWalk = cell$cov,
                      parallel = TRUE, verbose = TRUE)
stopCluster(cl)
registerDoSEQ()
show(resultCellBSL)
summary(resultCellBSL)
plot(resultCellBSL, thetaTrue = true_cell, thin = 20)

# Performing uBSL (reduce the number of iterations M if desired)
# Opening up the parallel pools using doParallel
cl <- makeCluster(detectCores() - 1)
registerDoParallel(cl)
resultCelluBSL <- bsl(cell$data, n = 5000, M = 10000, model = model, covRandWalk = cell$cov,
                      method = 'uBSL', parallel = TRUE, verbose = TRUE)
stopCluster(cl)
registerDoSEQ()
show(resultCelluBSL)
summary(resultCelluBSL)
plot(resultCelluBSL, thetaTrue = true_cell, thin = 20)

# Performing tuning for BSLasso
ssy <- cell_sum(cell$data, cell$sum_options$Yinit)
lambda_all <- list(exp(seq(0.5, 2.5, length.out=20)), exp(seq(0, 2, length.out=20)),
                     exp(seq(-1, 1, length.out=20)), exp(seq(-1, 1, length.out=20)))
# Opening up the parallel pools using doParallel
cl <- makeCluster(detectCores() - 1)
registerDoParallel(cl)
set.seed(100)
sp_cell <- selectPenalty(ssy, n = c(500, 1000, 1500, 2000), lambda_all, theta = true_cell,
                           M = 100, sigma = 1.5, model = model, method = 'BSL', shrinkage = 'glasso',
                           parallelSim = TRUE, parallelMain = FALSE)
stopCluster(cl)
registerDoSEQ()
sp_cell
plot(sp_cell)

# Performing BSLasso with a fixed penalty (reduce the number of iterations M if desired)
# Opening up the parallel pools using doParallel
cl <- makeCluster(detectCores() - 1)
registerDoParallel(cl)
resultCellBSLasso <- bsl(cell$data, n = 1500, M = 10000, theta0 = cell$start,
                           covRandWalk = cell$cov, fnSim = cell_sim, fnSum = cell_sum,
                           shrinkage = 'glasso', penalty = 1.3, fnPrior = cell_prior,

```

```

simArgs = cell$sim_options, sumArgs = cell$sum_options,
parallel = TRUE, parallelArgs = list(.packages = 'BSL'),
thetaNames = expression(P[m], P[p]), verbose = TRUE)
stopCluster(cl)
registerDoSEQ()
show(resultCellBSLasso)
summary(resultCellBSLasso)
plot(resultCellBSLasso, thetaTrue = true_cell, thin = 20)

# Performing semiBSL (reduce the number of iterations M if desired)
# Opening up the parallel pools using doParallel
cl <- makeCluster(detectCores() - 1)
registerDoParallel(cl)
resultCellSemiBSL <- bsl(cell$data, n = 5000, M = 10000, theta0 = cell$start,
                           covRandWalk = cell$cov, fnSim = cell_sim, fnSum = cell_sum,
                           method = 'semiBSL', fnPrior = cell_prior,
                           simArgs = cell$sim_options, sumArgs = cell$sum_options,
                           parallel = TRUE, parallelArgs = list(.packages = 'BSL'),
                           thetaNames = expression(P[m], P[p]), verbose = TRUE)
stopCluster(cl)
registerDoSEQ()
show(resultCellSemiBSL)
summary(resultCellSemiBSL)
plot(resultCellSemiBSL, thetaTrue = true_cell, thin = 20)

# Plotting the results together for comparison
# plot using the R default plot function
par(mar = c(5, 4, 1, 2), oma = c(0, 1, 2, 0))
combinePlotsBSL(list(resultCellBSL, resultCelluBSL, resultCellBSLasso, resultCellSemiBSL),
                which = 1, thetaTrue = true_cell, thin = 20, label = c('bsl', 'ubsl', 'bslasso', 'semibSL'),
                col = 1:4, lty = 1:4, lwd = 1)
mtext('Approximate Univariate Posteriors', outer = TRUE, cex = 1.5)

```

combinePlotsBSL

Plot the densities of multiple “bsl” class objects.

Description

The function `combinePlotsBSL` can be used to plot multiple BSL densities together, optionally with the true values for the parameters.

Usage

```

combinePlotsBSL(objectList, which = 1L, thin = 1, thetaTrue = NULL,
                 label = NULL, legendPosition = c("auto", "right", "bottom")[1],
                 legendNcol = NULL, col = NULL, lty = NULL, lwd = NULL,
                 cex.lab = 1, cex.axis = 1, cex.legend = 0.75,
                 top = "Approximate Marginal Posteriors", options.color = list(),

```

```
options.linetype = list(), options.size = list(),
options.theme = list())
```

Arguments

objectList	A list of “bsl” class objects.
which	An integer argument indicating which plot function to be used. The default, 1L, uses the plain <code>plot</code> to visualise the result. 2L uses <code>ggplot2</code> to draw the plot.
thin	A numeric argument indicating the gap between samples to be taken when thinning the MCMC draws. The default is 1, which means no thinning is used.
thetaTrue	A set of values to be included on the plots as a reference line. The default is NULL.
label	A string vector indicating the labels to be shown in the plot legend. The default is NULL, which uses the names from <code>objectList</code> .
legendPosition	One of the three string arguments, “auto”, “right” or “bottom”, indicating the legend position. The default is “auto”, which automatically choose from “right” and “bottom”. Only used when <code>which</code> is 1L.
legendNcol	A integer argument indicating the number of columns of the legend. The default, NULL, put all legends in the same row or column depending on <code>legendPosition</code> . Only used when <code>which</code> is 1L.
col	A vector argument containing the plotting color for each density curve. Each element of the vector will be passed into <code>lines</code> . Only used when <code>which</code> is 1L.
lty	A vector argument containing the line type for each density curve. Each element of the vector will be passed into <code>lines</code> . Only used when <code>which</code> is 1L.
lwd	A vector argument containing the line width for each density curve. Each element of the vector will be passed into <code>lines</code> . Only used when <code>which</code> is 1L.
cex.lab	The magnification to be used for x and y labels relative to the current setting of <code>cex</code> . To be passed into <code>plot</code> . Only used when <code>which</code> is 1L.
cex.axis	The magnification to be used for axis annotation relative to the current setting of <code>cex</code> . To be passed into <code>plot</code> . Only used when <code>which</code> is 1L.
cex.legend	The magnification to be used for legend annotation relative to the current setting of <code>cex</code> . Only used when <code>which</code> is 1L.
top	A string argument of the combined plot title. Only used when <code>which</code> is 2L.
options.color	A list of additional arguments to pass into function <code>ggplot2::scale_color_manual</code> . Only used when <code>which</code> is 2L.
options.linetype	A list of additional arguments to pass into function <code>ggplot2::scale_linetype_manual</code> . Only used when <code>which</code> is 2L.
options.size	A list of additional arguments to pass into function <code>ggplot2::scale_size_manual</code> . Only used when <code>which</code> is 2L.
options.theme	A list of additional arguments to pass into the <code>theme</code> function. Only use when <code>which</code> is 2L.

See Also

[ma2](#) for an example

cor2cov*Convert a correlation matrix to a covariance matrix*

Description

This function converts a correlation matrix to a covariance matrix

Usage

```
cor2cov(corr, std)
```

Arguments

- | | |
|-------------------|--|
| <code>corr</code> | The correlation matrix to be converted. This must be symmetric. |
| <code>std</code> | A vector that contains the standard deviations of the variables in the correlation matrix. |

Value

The covariance matrix.

fn*Functions to be used in bsl (for internal use)*

Description

Generate the generic simulation and summary statistics function for n simulations and fixed theta (for internal use).

Usage

```
fn(.Object)
```

Arguments

- | | |
|----------------------|----------------------|
| <code>.Object</code> | A “BSLMODEL” object. |
|----------------------|----------------------|

`gaussianRankCorr` *Gaussian rank correlation*

Description

This function computes the Gaussian rank correlation of Boudt et al. (2012).

Usage

```
gaussianRankCorr(x, vec = FALSE)
```

Arguments

- x A numeric matrix representing data where the number of rows is the number of independent data points and the number of columns are the number of variables in the dataset.
- vec A logical argument indicating if the vector of correlations should be returned instead of a matrix.

Value

Gaussian rank correlation matrix (default) or a vector of pair correlations.

References

Boudt, K., Cornelissen, J., and Croux, C. (2012). The Gaussian rank correlation estimator: robustness properties. *Statistics and Computing*, 22(2):471-483.

See Also

[cor2cov](#) for converting a correlation matrix to a covariance matrix.

Examples

```
data(ma2)
set.seed(100)

# generate 1000 simulations from the ma2 simulation function
x <- t(replicate(1000, ma2_sim(ma2$start, 10)))

corr1 <- cor(x) # traditional correlation matrix
corr2 <- gaussianRankCorr(x) # Gaussian rank correlation matrix
par(mfrow = c(1, 2))
image(corr1, main = 'traditional correlation matrix')
image(corr2, main = 'Gaussian rank correlation matrix')

std <- apply(x, MARGIN = 2, FUN = sd) # standard deviations
cor2cov(gaussianRankCorr(x), std) # convert to covariance matrix
```

Description

This function estimates the Gaussian synthetic likelihood function of Wood (2010). Shrinkage on the Gaussian covariance matrix is also available (see An et al 2019).

Usage

```
gaussianSynLike(ssy, ssx, shrinkage = NULL, penalty = NULL,
  standardise = FALSE, GRC = FALSE, log = TRUE, verbose = FALSE)
```

Arguments

<code>ssy</code>	The observed summary statistic.
<code>ssx</code>	A matrix of the simulated summary statistics. The number of rows is the same as the number of simulations per iteration.
<code>shrinkage</code>	A string argument indicating which shrinkage method to be used. The default is <code>NULL</code> , which means no shrinkage is used. Shrinkage estimation is only available for method “BSL” and “semiBSL”. Current options are “glasso” for the graphical lasso method of Friedman et al (2008) and “Warton” for the ridge regularisation method of Warton (2008).
<code>penalty</code>	The penalty value to be used for the specified shrinkage method. Must be between zero and one if the shrinkage method is “Warton”.
<code>standardise</code>	A logical argument that determines whether to standardise the summary statistics before applying the graphical lasso. This is only valid if method is “BSL”, shrinkage is “glasso” and penalty is not <code>NULL</code> . The diagonal elements will not be penalised if the shrinkage method is “glasso”. The default is <code>FALSE</code> .
<code>GRC</code>	A logical argument indicating whether the Gaussian rank correlation matrix (Boudt et al., 2012) should be used to estimate the covariance matrix in “BSL” method. The default is <code>FALSE</code> , which uses the sample covariance by default.
<code>log</code>	A logical argument indicating if the log of likelihood is given as the result. The default is <code>TRUE</code> .
<code>verbose</code>	A logical argument indicating whether an error message should be printed if the function fails to compute a likelihood. The default is <code>FALSE</code> .

Value

The estimated synthetic (log) likelihood value.

References

- Price, L. F., Drovandi, C. C., Lee, A., & Nott, D. J. (2018). Bayesian synthetic likelihood. *Journal of Computational and Graphical Statistics*. <https://doi.org/10.1080/10618600.2017.1302882>
- An, Z., South, L. F., Nott, D. J. & Drovandi, C. C. (2019). Accelerating Bayesian synthetic likelihood with the graphical lasso. *Journal of Computational and Graphical Statistics*. <https://doi.org/10.1080/10618600.2018.1537928>
- Friedman, J., Hastie, T., Tibshirani, R. (2008). Sparse inverse covariance estimation with the graphical lasso. *Biostatistics*. <https://doi.org/10.1093/biostatistics/kxm045>
- Warton, D. I. (2008). Penalized Normal Likelihood and Ridge Regularization of Correlation and Covariance Matrices, *Journal of the American Statistical Association*. <https://doi.org/10.1198/016214508000000021>

See Also

[gaussianSynLikeGhuryeOlkin](#) for the unbiased synthetic likelihood estimator, [semiparaKernelEstimate](#) for the semi-parametric likelihood estimator.

Examples

```
data(ma2)
y <- ma2$data # the observed data

theta_true <- c(0.6, 0.2)
x <- matrix(0, 300, 50)
set.seed(100)
for(i in 1:300) x[i, ] <- ma2_sim(theta_true, 50)

# the standard Gaussian synthetic likelihood (the likelihood estimator used in BSL)
gaussianSynLike(y, x)
# the Gaussian synthetic likelihood with glasso shrinkage estimation
# (the likelihood estimator used in BSlasso)
gaussianSynLike(y, x, shrinkage = 'glasso', penalty = 0.1)
# the Gaussian synthetic likelihood with Warton shrinkage estimation
gaussianSynLike(y, x, shrinkage = 'Warton', penalty = 0.9)
```

gaussianSynLikeGhuryeOlkin

Estimating the Gaussian synthetic likelihood with an unbiased estimator

Description

This function computes an unbiased, nonnegative estimate of a normal density function from simulations assumed to be drawn from it. See Price et al. (2018) and Ghurye and Olkin (1969).

Usage

```
gaussianSynLikeGhuryeOlkin(ssy, ssx, log = TRUE, verbose = FALSE)
```

Arguments

<code>ssy</code>	The observed summary statistic.
<code>ssx</code>	A matrix of the simulated summary statistics. The number of rows is the same as the number of simulations per iteration.
<code>log</code>	A logical argument indicating if the log of likelihood is given as the result. The default is <code>TRUE</code> .
<code>verbose</code>	A logical argument indicating whether an error message should be printed if the function fails to compute a likelihood. The default is <code>FALSE</code> .

Value

The estimated synthetic (log) likelihood value.

References

- Price, L. F., Drovandi, C. C., Lee, A., & Nott, D. J. (2018). Bayesian synthetic likelihood. Journal of Computational and Graphical Statistics. <https://doi.org/10.1080/10618600.2017.1302882>
- Ghurye, S. G., & Olkin, I. (1969). Unbiased estimation of some multivariate probability densities and related functions. The Annals of Mathematical Statistics. <https://projecteuclid.org/euclid.aoms/1177697501>

See Also

`gaussianSynLike` for the standard synthetic likelihood estimator, `semiparaKernelEstimate` for the semi-parametric likelihood estimator.

Examples

```
data(ma2)
y <- ma2$data # the observed data

theta_true <- c(0.6, 0.2)
x <- matrix(0, 300, 50)
set.seed(100)
for(i in 1:300) x[i, ] <- ma2_sim(theta_true, 50)

# unbiased estimate of the Gaussian synthetic likelihood
# (the likelihood estimator used in uBSL)
gaussianSynLikeGhuryeOlkin(y, x)
```

ma2*An MA(2) model*

Description

In this example we wish to estimate the parameters of a simple MA(2) time series model. We provide the data and tuning parameters required to reproduce the results in An et al. (2019).

Usage

```
data(ma2)

ma2_sim(theta, T)

ma2_sum(x)

ma2_prior(theta)

ma2_logPrior(theta)
```

Arguments

theta	A vector of proposed model parameters, θ_1 and θ_2 .
T	The number of observations.
x	Observed or simulated data in the format of a vector of length T .

Details

This example is based on estimating the parameters of a basic MA(2) time series model of the form

$$y_t = z_t + \theta_1 z_{t-1} + \theta_2 z_{t-2},$$

where $t = 1, \dots, T$ and $z_t \sim N(0, 1)$ for $t = -1, 0, \dots, T$. A uniform prior is used for this example, subject to the restrictions that $-2 < \theta_1 < 2$, $\theta_1 + \theta_2 > -1$ and $\theta_1 - \theta_2 < 1$ so that invertibility of the time series is satisfied. The summary statistics are simply the full data.

A simulated dataset

An example “observed” dataset and the tuning parameters relevant to that example can be obtained using `data(ma2)`. This “observed” data is a simulated dataset with $\theta_1 = 0.6$, $\theta_2 = 0.2$ and $T = 50$. Further information about this model and the specific choices of tuning parameters used in BSL and BSLasso can be found in An et al. (2019).

- `data`: A time series dataset, in the form of a vector of length T
- `sim_options`: A list containing $T = 50$
- `start`: A vector of suitable initial values of the parameters for MCMC
- `cov`: The covariance matrix of a multivariate normal random walk proposal distribution used in the MCMC, in the form of a 2 by 2 matrix

Author(s)

Ziwen An, Leah F. South and Christopher C. Drovandi

References

An, Z., South, L. F., Nott, D. J. & Drovandi, C. C. (2019). Accelerating Bayesian synthetic likelihood with the graphical lasso. *Journal of Computational and Graphical Statistics*. <https://doi.org/10.1080/10618600.2018.1537928>

Examples

```
## Not run:
# Loading the data for this example
data(ma2)
model <- BSLModel(fnSim = ma2$sim, fnSum = ma2$sum, simArgs = ma2$sim_options, theta0 = ma2$start,
                   fnLogPrior = ma2$logPrior)
true_ma2 <- c(0.6,0.2)

# Performing BSL (reduce the number of iterations M if desired)
resultMa2BSL <- bsl(y = ma2$data, n = 500, M = 300000, model = model, covRandWalk = ma2$cov,
                      method = 'BSL', verbose = TRUE)
show(resultMa2BSL)
summary(resultMa2BSL)
plot(resultMa2BSL, which = 1, thetaTrue = true_ma2, thin = 20)

# Performing uBSL (reduce the number of iterations M if desired)
resultMa2uBSL <- bsl(y = ma2$data, n = 500, M = 300000, model = model, covRandWalk=ma2$cov,
                      method = 'uBSL', verbose = TRUE)
show(resultMa2uBSL)
summary(resultMa2uBSL)
plot(resultMa2uBSL, which = 1, thetaTrue = true_ma2, thin = 20)

# Performing tuning for BSLasso
ssy <- ma2$sum(ma2$data)
lambda_all <- list(exp(seq(-3,0.5,length.out=20)), exp(seq(-4,-0.5,length.out=20)),
                     exp(seq(-5.5,-1.5,length.out=20)), exp(seq(-7,-2,length.out=20)))
set.seed(100)
sp_ma2 <- selectPenalty(ssy = ssy, n = c(50, 150, 300, 500), lambda_all, theta = true_ma2,
                           M = 100, sigma = 1.5, model = model, method = 'BSL', shrinkage = 'glasso')
sp_ma2
plot(sp_ma2)

# Performing BSLasso with a fixed penalty (reduce the number of iterations M if desired)
resultMa2BSLasso <- bsl(y = ma2$data, n = 300, M = 250000, model = model, covRandWalk=ma2$cov,
                         method = 'BSL', shrinkage = 'glasso', penalty = 0.027, verbose = TRUE)
show(resultMa2BSLasso)
summary(resultMa2BSLasso)
plot(resultMa2BSLasso, which = 1, thetaTrue = true_ma2, thin = 20)

# Performing semiBSL (reduce the number of iterations M if desired)
resultMa2SemiBSL <- bsl(y = ma2$data, n = 500, M = 300000, model = model, covRandWalk=ma2$cov,
```

```

    method = 'semiBSL', verbose = TRUE)
show(resultMa2SemiBSL)
summary(resultMa2SemiBSL)
plot(resultMa2SemiBSL, which = 1, thetaTrue = true_ma2, thin = 20)

# Plotting the results together for comparison
# plot using the R default plot function
par(mar = c(5, 4, 1, 2), oma = c(0, 1, 2, 0))
combinePlotsBSL(list(resultMa2BSL, resultMa2uBSL, resultMa2BSLasso, resultMa2SemiBSL), which = 1,
                 thetaTrue = true_ma2, thin = 20, label = c('bsl', 'uBSL', 'bslasso', 'semiBSL'),
                 col = c('black', 'red', 'blue', 'green'), lty = 1:4, lwd = 1)
mtext('Approximate Univariate Posteriors', outer = TRUE, cex = 1.5)

# plot using the ggplot2 package
combinePlotsBSL(list(resultMa2BSL, resultMa2uBSL, resultMa2BSLasso, resultMa2SemiBSL), which = 2,
                 thetaTrue = true_ma2, thin = 20, label = c('bsl', 'ubs1', 'bslasso', 'semiBSL'),
                 options.color = list(values=c('black', 'red', 'blue', 'green')),
                 options.linetype = list(values = 1:4), options.size = list(values = rep(1, 4)),
                 options.theme = list(plot.margin = grid::unit(rep(0.03,4), 'npc'),
                                      axis.title = ggplot2::element_text(size=12), axis.text = ggplot2::element_text(size = 8),
                                      legend.text = ggplot2::element_text(size = 12)))

## End(Not run)

```

Description

Here we provide the data and tuning parameters required to reproduce the results from the multivariate G & K (Drovandi and Pettitt, 2011) example from An et al. (2019).

Usage

```
mgnk_sim(theta_tilde, T, J, bound)
mgnk_sum(y)
```

Arguments

theta_tilde	A vector with 15 elements for the proposed model parameters.
T	The number of observations in the data.
J	The number of variables in the data.
bound	A matrix of boundaries for the uniform prior.
y	A $T \times J$ matrix of data.

Details

It is not practical to give a reasonable explanation of this example through R documentation given the number of equations involved. We refer the reader to the BSLasso paper (An et al., 2019) at <https://doi.org/10.1080/10618600.2018.1537928> for information on the model and summary statistic used in this example.

An example dataset

We use the foreign currency exchange data available from <http://www.rba.gov.au/statistics/historical-data.html> as in An et al. (2019).

- `data`: A 1651 by 3 matrix of data.
- `sim_options`: Values of `sim_options` relevant to this example.
- `start`: A vector of suitable initial values of the parameters for MCMC.
- `cov`: The covariance matrix of a multivariate normal random walk proposal distribution used in the MCMC, in the form of a 15 by 15 matrix

Author(s)

Ziwen An, Leah F. South and Christopher C. Drovandi

References

- An, Z., South, L. F., Nott, D. J. & Drovandi, C. C. (2019). Accelerating Bayesian synthetic likelihood with the graphical lasso. *Journal of Computational and Graphical Statistics*. <https://doi.org/10.1080/10618600.2018.1537928>
- Drovandi, C. C. and Pettitt, A. N. (2011). Likelihood-free Bayesian estimation of multivariate quantile distributions. *Computational Statistics and Data Analysis*. <https://doi.org/10.1016/j.csda.2011.03.019>

Examples

```
require(doParallel) # You can use a different package to set up the parallel backend
require(MASS)
require(ellipplot)

# Loading the data for this example
data(mgnk)

model <- BSLModel(fnSim = mgnk_sim, fnSum = mgnk_sum, simArgs = mgnk$sim_options,
                  theta0 = mgnk$start, thetaNames = expression(a[1],b[1],g[1],k[1],a[2],b[2],g[2],k[2],
                  a[3],b[3],g[3],k[3],delta[12],delta[13],delta[23])) 

# Performing BSL (reduce the number of iterations M if desired)
# Opening up the parallel pools using doParallel
cl <- makeCluster(detectCores() - 1)
registerDoParallel(cl)
resultMgnkBSL <- bsl(mgnk$data, n = 60, M = 80000, model = model, covRandWalk = mgnk$cov,
                      method = 'BSL', parallel = TRUE, parallelArgs = list(.packages='MASS', .export='ninenum'),
```

```

    verbose = TRUE)
stopCluster(cl)
registerDoSEQ()
show(resultMgnkBSL)
summary(resultMgnkBSL)
plot(resultMgnkBSL, which = 2, thin = 20)

# Performing uBSL (reduce the number of iterations M if desired)
# Opening up the parallel pools using doParallel
cl <- makeCluster(detectCores() - 1)
registerDoParallel(cl)
resultMgnkuBSL <- bsl(mgnk$data, n = 60, M = 80000, model = model, covRandWalk = mgnk$cov,
method = 'uBSL', parallel = TRUE, parallelArgs = list(.packages='MASS',.export='ninenum'),
verbose = TRUE)
stopCluster(cl)
registerDoSEQ()
show(resultMgnkuBSL)
summary(resultMgnkuBSL)
plot(resultMgnkuBSL, which = 2, thin = 20)

# Performing tuning for BSLasso
ssy <- mgnk_sum(mgnk$data)
lambda_all <- list(exp(seq(-2.5,0.5,length.out=20)), exp(seq(-2.5,0.5,length.out=20)),
exp(seq(-4,-0.5,length.out=20)), exp(seq(-5,-2,length.out=20)))

# Opening up the parallel pools using doParallel
cl <- makeCluster(detectCores() - 1)
registerDoParallel(cl)
set.seed(100)
sp_mgnk <- selectPenalty(ssy, n = c(15, 20, 30, 50), lambda_all = lambda_all, theta = mgnk$start,
M = 100, sigma = 1.5, model = model, method = 'BSL', shrinkage = 'glasso', standardise = TRUE,
parallelSim = TRUE, parallelSimArgs = list(.packages = 'MASS', .export = 'ninenum'),
parallelMain = TRUE)
stopCluster(cl)
registerDoSEQ()
sp_mgnk
plot(sp_mgnk)

# Performing BSLasso with a fixed penalty (reduce the number of iterations M if desired)
# Opening up the parallel pools using doParallel
cl <- makeCluster(detectCores() - 1)
registerDoParallel(cl)
resultMgnkBSLasso <- bsl(mgnk$data, n = 20, M = 80000, model = model, covRandWalk = mgnk$cov,
method = 'BSL', shrinkage = 'glasso', penalty = 0.3, standardise = TRUE, parallel = TRUE,
parallelArgs = list(.packages = 'MASS', .export = 'ninenum'), verbose = TRUE)
stopCluster(cl)
registerDoSEQ()
show(resultMgnkBSLasso)
summary(resultMgnkBSLasso)
plot(resultMgnkBSLasso, which = 2, thin = 20)

```

```

# Performing semiBSL (reduce the number of iterations M if desired)
# Opening up the parallel pools using doParallel
cl <- makeCluster(detectCores() - 1)
registerDoParallel(cl)
resultMgnkSemiBSL <- bsl(mgnk$data, n = 60, M = 80000, model = model, covRandWalk = mgnk$cov,
    method = 'semiBSL', parallel = TRUE, parallelArgs = list(.packages='MASS', .export='ninenum'),
    verbose = TRUE)
stopCluster(cl)
registerDoSEQ()
show(resultMgnkSemiBSL)
summary(resultMgnkSemiBSL)
plot(resultMgnkSemiBSL, which = 2, thin = 20)

# Plotting the results together for comparison
# plot using the R default plot function
par(mar = c(4, 4, 1, 1), oma = c(0, 1, 2, 0))
combinePlotsBSL(list(resultMgnkBSL, resultMgnkuBSL, resultMgnkBSLasso, resultMgnkSemiBSL),
    which = 1, thin = 20, label = c('bsl', 'bslasso', 'semiBSL'), col = c('red', 'blue', 'green'),
    lty = 2:4, lwd = 1)
mtext('Approximate Univariate Posteriors', outer = TRUE, line = 0.75, cex = 1.2)

# plot using the ggplot2 package
combinePlotsBSL(list(resultMgnkBSL, resultMgnkuBSL, resultMgnkBSLasso, resultMgnkSemiBSL),
    which = 2, thin = 20, label=c('bsl','bslasso','semiBSL'),
    options.color=list(values=c('red','blue','green')),
    options.linetype = list(values = 2:4), options.size = list(values = rep(1, 3)),
    options.theme = list(plot.margin = grid::unit(rep(0.03,4),'npc'),
        axis.title = ggplot2::element_text(size=12), axis.text = ggplot2::element_text(size = 8),
        legend.text = ggplot2::element_text(size = 12)))

```

penbsl

S3 reference class of the result from tuning to select the optimal penalty for BS Lasso

Description

Two functions (print and plot) are provided for class “penbsl”.

Usage

```

## S3 method for class 'penbsl'
print(x, digits = max(3L, getOption("digits") - 4L),
      ...)

## S3 method for class 'penbsl'
plot(x, logscale = TRUE, ...)

```

Arguments

x	A “penbsl” class object, typically the output of function selectPenalty .
digits	The number of digits to print.
...	Other arguments.
logscale	A logical indicator whether the x-axis (penalty) should be log transformed. The default is TRUE.

Author(s)

Ziwen An, Leah F. South and Christopher C. Drovandi

plot.bsl

Plot method for class “bsl”

Description

Plot the univariate marginal posterior plot of a bsl class object.

Usage

```
plot.bsl(x, which = 1L, thin = 1, thetaTrue = NULL,
          options.plot = NULL, top = "Approximate Univariate Posteriors",
          options.density = list(), options.theme = list())

marginalPostDefault(x, thin = 1, thetaTrue = NULL,
                     options.plot = NULL)

marginalPostGgplot(x, thin = 1, thetaTrue = NULL,
                    top = "Approximate Univariate Posteriors", options.density = list(),
                    options.theme = list())
```

Arguments

x	A “bsl” class object to plot.
which	An integer argument indicating which plot function to be used. The default, 1L, uses the plain plot to visualise the result. 2L uses ggplot2 to generate an aesthetically nicer figure.
thin	A numeric argument indicating the gap between samples to be taken when thinning the MCMC draws. The default is 1L, which means no thinning is used.
thetaTrue	A set of values to be included on the plots as a reference line. The default is NULL.
options.plot	A list of additional arguments to pass into the plot function. Only use when which is 1L.
top	A string argument of the combined plot title if which is 2L.

```
options.density
  A list of additional arguments to pass into the geom_density function. Only use
  when which is 2L.

options.theme  A list of additional arguments to pass into the theme function. Only use when
  which is 2L.
```

Author(s)

Ziwen An, Leah F. South and Christopher C. Drovandi

See Also

[combinePlotBSL](#) for a function to plot multiple BSL densities.

Examples

```
## Not run:
# pretend we had a bsl result
result <- new('bsl')
result@theta <- MASS::mvrnorm(10000, c(0.6, 0.2), diag(c(1, 1)))
result@M <- 10000

# plot using the R default plot function
par(mar = c(5, 4, 1, 2), oma = c(0, 1, 3, 0))
plot(result, which = 1, thin = 10, thetaTrue = c(0.6, 0.2),
      options.plot = list(cex.main = 1, col = 'red', lty = 2, lwd = 2, main = NA))
mtext('Approximate Univariate Posteriors', outer = TRUE, cex = 1.5)

# plot using the ggplot2 package
plot(result, which = 2, thin = 10, thetaTrue = c(0.6, 0.2),
      options.density = list(colour = 'darkblue', fill = 'grey80', size = 1),
      options.theme = list(plot.margin = grid::unit(rep(0.05,4), 'npc'),
                           axis.text = ggplot2::element_text(size = 10)))

## End(Not run)
```

Description

This is the main function for selecting the shrinkage (graphical lasso or Warton's estimation) penalty parameter for method BSL or semiBSL based on a point estimate of the parameters. Parallel computing is supported with the R package `foreach`.

Usage

```
selectPenalty(ssy, n, lambda_all, M, sigma, model, theta = model@theta0,
  method = c("BSL", "semiBSL")[1], shrinkage = c("glasso",
  "Warton")[1], standardise = FALSE, GRC = FALSE,
  parallelSim = FALSE, parallelSimArgs = NULL, parallelMain = FALSE,
  verbose = TRUE, fnSim, fnSum, simArgs, sumArgs)
```

Arguments

<code>ssy</code>	A summary statistic vector for the observed data.
<code>n</code>	A vector of possible values of <code>n</code> , the number of simulations from the model per MCMC iteration for estimating the synthetic likelihood.
<code>lambda_all</code>	A list, with each entry containing the vector of penalty values to test for the corresponding choice of <code>n</code> .
<code>M</code>	The number of repeats to use in estimating the standard deviation of the estimated log synthetic likelihood.
<code>sigma</code>	The standard deviation of the log synthetic likelihood estimator to aim for, usually a value between 1 and 2. This reflects the mixing of a Markov chain.
<code>model</code>	A “BSLMODEL” object generated with function <code>BSLModel</code> . See BSLModel .
<code>theta</code>	A point estimate of the parameter value which all of the simulations will be based on.
<code>method</code>	A string argument indicating the method to be used. The default, “BSL”, runs BSL. “semiBSL” runs the semi-parametric BSL algorithm and is more robust to non-normal summary statistics.
<code>shrinkage</code>	A string argument indicating which shrinkage method to be used. Current options are “glasso” for the graphical lasso method of Friedman et al (2008) and “Warton” for the ridge regularisation method of Warton (2008).
<code>standardise</code>	A logical argument that determines whether to standardise the summary statistics before applying the graphical lasso. This is only valid if <code>method</code> is “BSL”, <code>shrinkage</code> is “glasso” and <code>penalty</code> is not <code>NULL</code> . The diagonal elements will not be penalised if the shrinkage method is “glasso”. The default is <code>FALSE</code> .
<code>GRC</code>	A logical argument indicating whether the Gaussian rank correlation matrix (Boudt et al., 2012) should be used to estimate the covariance matrix in “BSL” method. The default is <code>FALSE</code> , which uses the sample covariance by default.
<code>parallelSim</code>	A logical value indicating whether parallel computing should be used for simulation and summary statistic evaluation. Default is <code>FALSE</code> .
<code>parallelSimArgs</code>	A list of additional arguments to pass into the <code>foreach</code> function. Only used when <code>parallelSim</code> is <code>TRUE</code> , default is <code>NULL</code> .
<code>parallelMain</code>	A logical value indicating whether parallel computing should be used to computing the graphical lasso function. Default is <code>FALSE</code> .
<code>verbose</code>	A logical argument indicating whether the iteration numbers (<code>1:M</code>) should be printed to track progress. The default is <code>FALSE</code> .

<code>fnSim</code>	Deprecated, will be removed in the future, use <code>model</code> instead. A function that simulates data for a given parameter value. The first argument should be the parameters. Other necessary arguments (optional) can be specified with <code>simArgs</code> .
<code>fnSum</code>	Deprecated, will be removed in the future, use <code>model</code> instead. A function for computing summary statistics of data. The first argument should be the observed or simulated dataset. Other necessary arguments (optional) can be specified with <code>sumArgs</code> .
<code>simArgs</code>	Deprecated, will be removed in the future, use <code>model</code> instead. A list of additional arguments to pass into the simulation function. Only use when the input <code>fnSim</code> requires additional arguments. The default is <code>NULL</code> .
<code>sumArgs</code>	Deprecated, will be removed in the future, use <code>model</code> instead. A list of additional arguments to pass into the summary statistics function. Only use when the input <code>fnSum</code> requires additional arguments. The

Value

An object of class `penbsl` is returned, containing the following components:

- `resultsDF`: A data frame containing the following:
 - `n`: The choices of `n` that were specified.
 - `penalty`: The choices of the penalty that were specified.
 - `sigma`: The standard deviation of the log synthetic likelihood estimator under the above choices.
 - `sigmaOpt`: An indicator of whether it was the closest `sigma` to the desired one for each choice of `n`.
- `call`: The original code that was used to call the method.

The functions `print()` and `plot()` are both available for types of class `penbsl`.

Author(s)

Ziwen An, Leah F. South and Christopher C. Drovandi

References

- An, Z., South, L. F., Nott, D. J. & Drovandi, C. C. (2019). Accelerating Bayesian synthetic likelihood with the graphical lasso. *Journal of Computational and Graphical Statistics*. <https://doi.org/10.1080/10618600.2018.1537928>
- Warton, D. I. (2008). Penalized Normal Likelihood and Ridge Regularization of Correlation and Covariance Matrices, *Journal of the American Statistical Association*. <https://doi.org/10.1198/016214508000000021>

See Also

`ma2`, `cell` and `mgnk` for examples. `bsl` for a function to run BS Lasso after selecting the tuning parameter and `penbsl` for functions related to visualisation.

semiparaKernelEstimate*Estimating the semi-parametric joint likelihood*

Description

This function computes the semi-parametric likelihood estimator of An et al (2018). Kernel density estimates are used for modelling each univariate marginal distribution, and the dependence structure between summaries are captured using a Gaussian copula.

Usage

```
semiparaKernelEstimate(ssy, ssx, kernel = "gaussian", shrinkage = NULL,
penalty = NULL, log = TRUE)
```

Arguments

ssy	The observed summary statistic.
ssx	A matrix of the simulated summary statistics. The number of rows is the same as the number of simulations per iteration.
kernel	A string argument indicating the smoothing kernel to pass into density for estimating the marginal distribution of each summary statistic. Only "gaussian" and "epanechnikov" are available. The default is "gaussian".
shrinkage	A string argument indicating which shrinkage method to be used on the correlation matrix of the Gaussian copula. The default is NULL, which means no shrinkage is used. Current options are "glasso" for graphical lasso and "Warton" for the ridge regularisation method of Warton (2008).
penalty	The penalty value to be used for the specified shrinkage method. Must be between zero and one if the shrinkage method is "Warton".
log	A logical argument indicating if the log of the likelihood is given as the result. The default is TRUE.

Value

The estimated synthetic (log) likelihood value.

References

- An, Z., Nott, D. J. & Drovandi, C. (2018). Robust Bayesian Synthetic Likelihood via a Semi-Parametric Approach. <https://arxiv.org/abs/1809.05800>
- Friedman, J., Hastie, T., Tibshirani, R. (2008). Sparse inverse covariance estimation with the graphical lasso. *Biostatistics*. <https://doi.org/10.1093/biostatistics/kxm045>
- Warton, D. I. (2008). Penalized Normal Likelihood and Ridge Regularization of Correlation and Covariance Matrices, *Journal of the American Statistical Association*. <https://www.tandfonline.com/doi/abs/10.1198/016214508000000021>

See Also

[gaussianSynLike](#) for the standard synthetic likelihood estimator, [gaussianSynLikeGhuryeOlkin](#) for the unbiased synthetic likelihood estimator.

Examples

```
data(ma2)
y <- ma2$data # the observed data

theta_true <- c(0.6, 0.2)
x <- matrix(0, 300, 50)
set.seed(100)
for(i in 1:300) x[i, ] <- ma2_sim(theta_true, 50)

# the default semi-parametric synthetic likelihood estimator of semiBSL
semiparaKernelEstimate(y, x)
# using shrinkage on the correlation matrix of the Gaussian copula is also possible
semiparaKernelEstimate(y, x, shrinkage = 'Warton', penalty = 0.6)
```

setns

Find the length of summary statistics (for internal use)

Description

Find and set the length of summary statistics with a test run (for internal use).

Usage

```
setns(.Object)
```

Arguments

.Object	A “BSLMODEL” object.
---------	----------------------

show.bsl

Show method for class “bsl”. Display the basic information of a bsl object.

Description

Display the basic information of a bsl object.

Usage

```
show.bsl(object)
```

Arguments

- object A “bsl” class object.

summary.bsl

Summary method for class “bsl”

Description

Summarise a bsl class object.

Usage

```
summary.bsl(object, thetaNames = NULL)
```

Arguments

- object A “bsl” class object to be summarised.
thetaNames Parameter names to be shown in the summary table. Parameter names of the bsl object will be used by default.

Value

A vector of the number of simulations per iteration, acceptance rate of the Markov chain and effective sample size for each parameter.

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