

Package ‘Distributacalcul’

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Description Calculates expected values, variance, different moments (kth moment, truncated mean), stop-loss, mean excess loss, Value-at-Risk (VaR) and Tail Value-at-Risk (TVaR) as well as some density and cumulative (survival) functions of continuous, discrete and compound distributions. This package also includes a visual 'Shiny' component to enable students to visualize distributions and understand the impact of their parameters. This package is intended to expand the 'stats' package so as to enable students to develop an intuition for probability.

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URL https://alec42.github.io/Distributacalcul_Package/

BugReports https://github.com/alec42/Distributacalcul_Package/issues

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 Beta

Beta Distribution

Description

Beta distribution with shape parameters α and β .

Usage

```

expValBeta(shape1, shape2)
varBeta(shape1, shape2)
kthMomentBeta(k, shape1, shape2)
expValLimBeta(d, shape1, shape2)
expValTruncBeta(d, shape1, shape2, less.than.d = TRUE)
stopLossBeta(d, shape1, shape2)
meanExcessBeta(d, shape1, shape2)
VatRBeta(kap, shape1, shape2)
TVatRBeta(kap, shape1, shape2)
mgfBeta(t, shape1, shape2, k0)
  
```

Arguments

shape1	shape parameter α , must be positive.
shape2	shape parameter β , must be positive.
k	kth-moment.
d	cut-off value.
less.than.d	logical; if TRUE (default) truncated mean for values $\leq d$, otherwise, for values $> d$.
kap	probability.
t	t.
k0	point up to which to sum the distribution for the approximation.

Details

The Beta distribution with shape parameters α and β has density:

$$f(x) = \frac{\Gamma(\alpha + \beta)}{\Gamma(\alpha)\Gamma(\beta)} x^{\alpha-1} (1-x)^{\beta-1}$$

for $x \in [0, 1]$, $\alpha, \beta > 0$.

Value

Function :

- [expValBeta](#) gives the expected value.
- [varBeta](#) gives the variance.
- [kthMomentBeta](#) gives the kth moment.
- [expValLimBeta](#) gives the limited mean.
- [expValTruncBeta](#) gives the truncated mean.
- [stopLossBeta](#) gives the stop-loss.
- [meanExcessBeta](#) gives the mean excess loss.
- [VatRBeta](#) gives the Value-at-Risk.
- [TVatRBeta](#) gives the Tail Value-at-Risk.
- [mgfBeta](#) gives the moment generating function (MGF).

Invalid parameter values will return an error detailing which parameter is problematic.

Note

Function [VatRBeta](#) is a wrapper for the [qbeta](#) function from the stats package.

Examples

```
expValBeta(shape1 = 3, shape2 = 5)

varBeta(shape1 = 4, shape2 = 5)

kthMomentBeta(k = 3, shape1 = 4, shape2 = 5)

expValLimBeta(d = 0.3, shape1 = 4, shape2 = 5)

expValTruncBeta(d = 0.4, shape1 = 4, shape2 = 5)

# Values less than d
expValTruncBeta(d = 0.4, shape1 = 4, shape2 = 5, less.than.d = FALSE)

stopLossBeta(d = 0.3, shape1 = 4, shape2 = 5)

meanExcessBeta(d = .3, shape1 = 4, shape2 = 5)
```

```
VatRBeta(kap = .99, shape1 = 4, shape2 = 5)
TVatRBeta(kap = .99, shape1 = 4, shape2 = 5)
mgfBeta(t = 1, shape1 = 3, shape2 = 5, k0 = 1E2)
```

binom	<i>Binomial Distribution</i>
-------	------------------------------

Description

Binomial distribution with size n and probability of success p .

Usage

```
expValBinom(size, prob)
varBinom(size, prob)
expValTruncBinom(d, size, prob, less.than.d = TRUE)
VatRBinom(kap, size, prob)
TVatRBinom(kap, size, prob)
pgfBinom(t, size, prob)
mgfBinom(t, size, prob)
```

Arguments

size	Number of trials (0 or more).
prob	Probability of success in each trial.
d	cut-off value.
less.than.d	logical; if TRUE (default) truncated mean for values $\leq d$, otherwise, for values $> d$.
kap	probability.
t	t.

Details

The binomial distribution with probability of success p for n trials has probability mass function :

$$Pr(X = k) = \binom{n}{k} p^k (1 - p)^{n-k}$$

for $k = 0, 1, 2, \dots, n$, $p \in [0, 1]$, and $n > 0$

Value

Function :

- `mgfBinom` gives the moment generating function (MGF).
- `pgfBinom` gives the probability generating function (PGF).
- `expValBinom` gives the expected value.
- `varBinom` gives the variance.
- `expValTruncBinom` gives the truncated mean.
- `TVatRBinom` gives the Tail Value-at-Risk.
- `VatRBinom` gives the Value-at-Risk.

Invalid parameter values will return an error detailing which parameter is problematic.

Note

Function `VatRBinom` is a wrapper of the `qbinom` function from the stats package.

Examples

```
expValBinom(size = 3, prob = 0.5)
```

```
varBinom(size = 3, prob = 0.5)
```

```
expValTruncBinom(d = 2, size = 3, prob = 0.5)
```

```
expValTruncBinom(d = 0, size = 3, prob = 0.5, less.than.d = FALSE)
```

```
VatRBinom(kap = 0.8, size = 5, prob = 0.2)
```

```
TVatRBinom(kap = 0.8, size = 5, prob = 0.2)
```

```
pgfBinom(t = 1, size = 3, prob = 0.5)
```

```
mgfBinom(t = 1, size = 3, prob = 0.5)
```

Description

Computes CDF, PDF and simulations of of the bivariate Ali-Mikhail-Haq copula.

Usage

```
cBivariateAMH(u1, u2, dependencyParameter, ...)  
cdBivariateAMH(u1, u2, dependencyParameter, ...)  
crBivariateAMH(numberSimulations = 10000, seed = 42, dependencyParameter)
```

Arguments

u1, u2	points at which to evaluate the copula.
dependencyParameter	correlation parameter.
...	other parameters.
numberSimulations	Number of simulations.
seed	Simulation seed, 42 by default.

Details

The bivariate Ali-Mikhail-Haq copula has CDF :

Value

Function :

- `cBivariateAMH` returns the value of the copula.
- `cdBivariateAMH` returns the value of the density copula.
- `crBivariateAMH` returns simulated values of the copula.

Examples

```
cBivariateAMH(u1 = .76, u2 = 0.4, dependencyParameter = 0.4)  
cdBivariateAMH(u1 = .76, u2 = 0.4, dependencyParameter = 0.4)  
crBivariateAMH(numberSimulations = 10, seed = 42, dependencyParameter = 0.2)
```

bivariateCA

Bivariate Cuadras-Augé Copula

Description

Computes CDF and simulations of the bivariate Cuadras-Augé copula.

Usage

```
cBivariateCA(u1, u2, dependencyParameter, ...)
```

```
crBivariateCA(numberSimulations = 10000, seed = 42, dependencyParameter)
```

Arguments

u1, u2 points at which to evaluate the copula.
 dependencyParameter correlation parameter.
 ... other parameters.
 numberSimulations Number of simulations.
 seed Simulation seed, 42 by default.

Details

The bivariate Cuadras-Augé copula has CDF :

$$C(u_1, u_2) = u_1 u_2^{1-\alpha} \times \mathbf{1}_{\{u_1 \leq u_2\}} + u_1^{1-\alpha} u_2 \times \mathbf{1}_{\{u_1 \geq u_2\}}$$

for $u_1, u_2, \alpha \in [0, 1]$. It is the geometric mean of the independance and upper Fréchet bound copulas.

Value

Function :

- `cBivariateCA` returns the value of the copula.
- `crBivariateCA` returns simulated values of the copula.

Examples

```
cBivariateCA(u1 = .76, u2 = 0.4, dependencyParameter = 0.4)
```

```
crBivariateCA(numberSimulations = 10, seed = 42, dependencyParameter = 0.2)
```

 bivariateClayton

Bivariate Clayton Copula

Description

Computes CDF, PDF and simulations of the bivariate Clayton copula.

Usage

```
cBivariateClayton(u1, u2, dependencyParameter, ...)
cdBivariateClayton(u1, u2, dependencyParameter, ...)
crBivariateClayton(numberSimulations = 10000, seed = 42, dependencyParameter)
```

Arguments

u1, u2 points at which to evaluate the copula.
dependencyParameter correlation parameter.
... other parameters.
numberSimulations Number of simulations.
seed Simulation seed, 42 by default.

Details

The bivariate Clayton copula has CDF :

Value

Function :

- [cBivariateAMH](#) returns the value of the copula.
- [cdBivariateAMH](#) returns the value of the density function associated to the copula.

Examples

```
cBivariateClayton(u1 = .76, u2 = 0.4, dependencyParameter = 0.4)
cdBivariateClayton(u1 = .76, u2 = 0.4, dependencyParameter = 0.4)
crBivariateClayton(numberSimulations = 10, seed = 42, dependencyParameter = 0.2)
```

bivariateEFGM

Bivariate Eyraud-Farlie-Gumbel-Morgenstern (EFGM) Copula

Description

Computes CDF, PDF and simulations of the EFGM copula.

Usage

```
cBivariateEFGM(u1, u2, dependencyParameter)
cdBivariateEFGM(u1, u2, dependencyParameter)
crBivariateEFGM(numberSimulations = 10000, seed = 42, dependencyParameter)
```

Arguments

u1, u2 points at which to evaluate the copula.
dependencyParameter correlation parameter.
numberSimulations Number of simulations.
seed Simulation seed, 42 by default.

Details

The EFGM copula has CDF :

Value

Function :

- `cBivariateEFGM` returns the value of the copula.
- `cdBivariateEFGM` returns the value of the density function associated to the copula.
- `crBivariateEFGM` returns simulated values of the copula.

Examples

```
cBivariateEFGM(u1 = .76, u2 = 0.4, dependencyParameter = 0.4)
cdBivariateEFGM(u1 = .76, u2 = 0.4, dependencyParameter = 0.4)
crBivariateEFGM(numberSimulations = 10, seed = 42, dependencyParameter = 0.2)
```

bivariateFrank

Bivariate Frank Copula

Description

Computes CDF, PDF and simulations of the bivariate Frank copula.

Usage

```
cBivariateFrank(u1, u2, dependencyParameter, ...)  
cdBivariateFrank(u1, u2, dependencyParameter, ...)  
crBivariateFrank(numberSimulations = 10000, seed = 42, dependencyParameter)
```

Arguments

u1, u2	points at which to evaluate the copula.
dependencyParameter	correlation parameter.
...	other parameters.
numberSimulations	Number of simulations.
seed	Simulation seed, 42 by default.

Details

The bivariate Frank copula has CDF :

Value

Function :

- `cBivariateFrank` returns the value of the copula.
- `cdBivariateFrank` returns the value of the density function associated to the copula.
- `crBivariateFrank` returns simulated values of the copula.

Examples

```
cBivariateFrank(u1 = .76, u2 = 0.4, dependencyParameter = 0.4)  
cdBivariateFrank(u1 = .76, u2 = 0.4, dependencyParameter = 0.4)  
crBivariateFrank(numberSimulations = 10, seed = 42, dependencyParameter = 0.2)
```

bivariateGumbel

Bivariate Gumbel Copula

Description

Computes CDF, PDF and simulations of the bivariate Gumbel copula.

Usage

```
cBivariateGumbel(u1, u2, dependencyParameter, ...)  
cdBivariateGumbel(u1, u2, dependencyParameter, ...)  
crBivariateGumbel(numberSimulations = 10000, seed = 42, dependencyParameter)
```

Arguments

u1, u2	points at which to evaluate the copula.
dependencyParameter	correlation parameter.
...	other parameters.
numberSimulations	Number of simulations.
seed	Simulation seed, 42 by default.

Details

The bivariate Gumbel copula has CDF :

Value

Function :

- `cBivariateGumbel` returns the value of the copula.
- `cdBivariateGumbel` returns the value of the density function associated to the copula.
- `crBivariateGumbel` returns simulated values of the copula.

Examples

```
cBivariateGumbel(u1 = .76, u2 = 0.4, dependencyParameter = 1.4)  
cdBivariateGumbel(u1 = .76, u2 = 0.4, dependencyParameter = 1.4)  
crBivariateGumbel(numberSimulations = 10, seed = 42, dependencyParameter = 1.2)
```

bivariateMO

Bivariate Marshall-Olkin Copula

Description

Computes CDF and simulations of the bivariate Marshall-Olkin copula.

Usage

```
cBivariateMO(u1, u2, dependencyParameter, ...)
```

```
crBivariateMO(numberSimulations = 10000, seed = 42, dependencyParameter)
```

Arguments

u1, u2 points at which to evaluate the copula.
 dependencyParameter correlation parameters, must be vector of length 2.
 ... other parameters.
 numberSimulations Number of simulations.
 seed Simulation seed, 42 by default.

Details

The bivariate Marshall-Olkin copula has CDF :

$$C(u_1, u_2) = u_1 u_2^{1-\beta} \times \mathbf{1}_{\{u_1^\alpha \leq u_2^\beta\}} + u_1^{1-\alpha} u_2 \times \mathbf{1}_{\{u_1^\alpha \geq u_2^\beta\}}$$

for $u_1, u_2, \alpha, \beta \in [0, 1]$. It is the geometric mean of the independence and upper Fréchet bound copulas.

Value

Function :

- `cBivariateMO` returns the value of the copula.
- `crBivariateMO` returns simulated values of the copula.

Examples

```
cBivariateMO(u1 = .76, u2 = 0.4, dependencyParameter = c(0.4, 0.3))
```

```
crBivariateMO(numberSimulations = 10, seed = 42, dependencyParameter = c(0.2, 0.5))
```

Description

Computes various risk measures (mean, variance, Value-at-Risk (VaR), and Tail Value-at-Risk (TVaR)) for the compound Binomial distribution.

Usage

```
pCompBinom(  
  x,  
  size,  
  prob,  
  shape,  
  rate = 1/scale,  
  scale = 1/rate,  
  k0,  
  distr_severity = "Gamma"  
)
```

```
expValCompBinom(  
  size,  
  prob,  
  shape,  
  rate = 1/scale,  
  scale = 1/rate,  
  distr_severity = "Gamma"  
)
```

```
varCompBinom(  
  size,  
  prob,  
  shape,  
  rate = 1/scale,  
  scale = 1/rate,  
  distr_severity = "Gamma"  
)
```

```
VatRCompBinom(  
  kap,  
  size,  
  prob,  
  shape,  
  rate = 1/scale,  
  scale = 1/rate,  
  k0,  
  distr_severity = "Gamma"  
)
```

```
TVatRCompBinom(  
  kap,  
  size,  
  prob,  
  shape,  
  rate = 1/scale,  
  scale = 1/rate,
```

```

    vark,
    k0,
    distr_severity = "Gamma"
)

```

Arguments

x	vector of quantiles.
size	Number of trials (0 or more).
prob	Probability of success in each trial.
shape	shape parameter α , must be positive.
rate	rate parameter β , must be positive.
scale	alternative parameterization to the rate parameter, scale = 1 / rate.
k0	point up to which to sum the distribution for the approximation.
distr_severity	Choice of severity distribution. <ul style="list-style-type: none"> • "gamma" (default) • "lognormal" only for the expected value and variance.
kap	probability.
vark	Value-at-Risk (VaR) calculated at the given probability kap.

Details

The compound binomial distribution has density

Value

Function :

- [pCompBinom](#) gives the cumulative density function.
- [expValCompBinom](#) gives the expected value.
- [varCompBinom](#) gives the variance.
- [TVatRCompBinom](#) gives the Tail Value-at-Risk.
- [VatRCompBinom](#) gives the Value-at-Risk.

Returned values are approximations for the cumulative density function, TVaR, and VaR.

Examples

```

pCompBinom(x = 2, size = 1, prob = 0.2, shape = log(1000) - 0.405,
           rate = 0.9^2, k0 = 1E2, distr_severity = "Gamma")

```

```

expValCompBinom(size = 1, prob = 0.2, shape = log(1000) - 0.405, rate = 0.9^2,
                distr_severity = "Lognormale")

```

```

varCompBinom(size = 1, prob = 0.2, shape = log(1000) - 0.405, rate = 0.9^2,
              distr_severity = "Lognormale")

```

```
VatRCompBinom(kap = 0.9, size = 1, prob = 0.2, shape = log(1000) - 0.405,  
              rate = 0.9^2, k0 = 1E2, distr_severity = "Gamma")  
  
vark_calc <- VatRCompBinom(kap = 0.9, size = 1, prob = 0.2, shape = 0.59,  
                          rate = 0.9^2, k0 = 1E2, distr_severity = "Gamma")  
TVatRCompBinom(kap = 0.9, size = 1, prob = 0.2, shape = 0.59, rate = 0.9^2,  
               vark = vark_calc, k0 = 1E2, distr_severity = "Gamma")
```

CompNBinom

Compound Negative Binomial Distribution

Description

Computes various risk measures (mean, variance, Value-at-Risk (VatR), and Tail Value-at-Risk (TVatR)) for the compound Negative Binomial distribution.

Usage

```
pCompNBinom(  
  x,  
  size,  
  prob,  
  shape,  
  rate = 1/scale,  
  scale = 1/rate,  
  k0,  
  distr_severity = "Gamma"  
)  
  
expValCompNBinom(  
  size,  
  prob,  
  shape,  
  rate = 1/scale,  
  scale = 1/rate,  
  distr_severity = "Gamma"  
)  
  
varCompNBinom(  
  size,  
  prob,  
  shape,  
  rate = 1/scale,  
  scale = 1/rate,  
  distr_severity = "Gamma"  
)
```



```

VatRCompNBinom(
  kap,
  size,
  prob,
  shape,
  rate = 1/scale,
  scale = 1/rate,
  k0,
  distr_severity = "Gamma"
)

TVatRCompNBinom(
  kap,
  vark,
  size,
  prob,
  shape,
  rate = 1/scale,
  scale = 1/rate,
  k0,
  distr_severity = "Gamma"
)

```

Arguments

x	vector of quantiles.
size	Number of successful trials.
prob	Probability of success in each trial.
shape	shape parameter α , must be positive.
rate	rate parameter β , must be positive.
scale	alternative parameterization to the rate parameter, scale = 1 / rate.
k0	point up to which to sum the distribution for the approximation.
distr_severity	Choice of severity distribution. <ul style="list-style-type: none"> • "gamma" (default) • "lognormal" only for the expected value and variance.
kap	probability.
vark	Value-at-Risk (VaR) calculated at the given probability kap.

Details

The compound negative binomial distribution has density

Value

Function :

- `pCompNBinom` gives the cumulative density function.
- `expValCompNBinom` gives the expected value.
- `varCompNBinom` gives the variance.
- `TVatRCompNBinom` gives the Tail Value-at-Risk.
- `VatRCompNBinom` gives the Value-at-Risk.

Returned values are approximations for the cumulative density function, TVatR, and VatR.

Examples

```
pCompNBinom(x = 2, size = 1, prob = 0.2, shape = log(1000) - 0.405,
             rate = 0.9^2, k0 = 1E2, distr_severity = "Gamma")
```

```
expValCompNBinom(size = 4, prob = 0.2, shape = 0, scale = 1,
                  distr_severity = "Lognormal")
```

```
varCompNBinom(size = 1, prob = 0.2, shape = log(1000) - 0.405, rate = 0.9^2,
               distr_severity = "Lognormale")
```

```
VatRCompNBinom(kap = 0.9, size = 1, prob = 0.2, shape = 0.59,
                rate = 0.9^2, k0 = 1E2, distr_severity = "Gamma")
```

```
vark_calc <- VatRCompNBinom(kap = 0.9, size = 1, prob = 0.2, shape = 0.59,
                             rate = 0.9^2, k0 = 1E2, distr_severity = "Gamma")
```

```
TVatRCompNBinom(kap = 0.9, size = 1, prob = 0.2, shape = 0.59, rate = 0.9^2,
                 vark = vark_calc, k0 = 1E2, distr_severity = "Gamma")
```

CompPois

Compound Poisson Distribution

Description

Computes various risk measures (mean, variance, Value-at-Risk (VaR), and Tail Value-at-Risk (TVaR)) for the compound Poisson distribution.

Usage

```
pCompPois(
  x,
  lambda,
  shape,
  rate = 1/scale,
  scale = 1/rate,
```

```
    k0,  
    distr_severity = "Gamma"  
  )  
  
  expValCompPois(  
    lambda,  
    shape,  
    rate = 1/scale,  
    scale = 1/rate,  
    distr_severity = "Gamma"  
  )  
  
  varCompPois(  
    lambda,  
    shape,  
    rate = 1/scale,  
    scale = 1/rate,  
    distr_severity = "Gamma"  
  )  
  
  VatRCompPois(  
    kap,  
    lambda,  
    shape,  
    rate = 1/scale,  
    scale = 1/rate,  
    k0,  
    distr_severity = "Gamma"  
  )  
  
  TVatRCompPois(  
    kap,  
    lambda,  
    shape,  
    rate = 1/scale,  
    scale = 1/rate,  
    vark,  
    k0,  
    distr_severity = "Gamma"  
  )
```

Arguments

x	vector of quantiles.
lambda	Rate parameter λ .
shape	shape parameter α , must be positive.
rate	rate parameter β , must be positive.
scale	alternative parameterization to the rate parameter, scale = 1 / rate.

<code>k0</code>	point up to which to sum the distribution for the approximation.
<code>distr_severity</code>	Choice of severity distribution. <ul style="list-style-type: none"> • "gamma" (default) • "lognormal" only for the expected value and variance.
<code>kap</code>	probability.
<code>vark</code>	Value-at-Risk (VaR) calculated at the given probability <code>kap</code> .

Details

The compound Poisson distribution with parameters ... has density

Value

Function :

- `pCompPois` gives the cumulative density function.
- `expValCompPois` gives the expected value.
- `varCompPois` gives the variance.
- `TVatRCompPois` gives the Tail Value-at-Risk.
- `VatRCompPois` gives the Value-at-Risk.

Returned values are approximations for the cumulative density function, TVaR, and VaR.

Examples

```
pCompPois(x = 2, lambda = 2, shape = log(1000) - 0.405,
          rate = 0.9^2, k0 = 1E2, distr_severity = "Gamma")

expValCompPois(lambda = 2, shape = log(1000) - 0.405, rate = 0.9^2,
               distr_severity = "Lognormale")

varCompPois(lambda = 2, shape = log(1000) - 0.405, rate = 0.9^2,
            distr_severity = "Lognormale")

VatRCompPois(kap = 0.9, lambda = 2, shape = log(1000) - 0.405,
             rate = 0.9^2, k0 = 1E2, distr_severity = "Gamma")

vark_calc <- VatRCompPois(kap = 0.9, lambda = 2, shape = 0.59,
                        rate = 0.9^2, k0 = 1E2, distr_severity = "Gamma")
TVatRCompPois(kap = 0.9, lambda = 2, shape = 0.59, rate = 0.9^2,
              vark = vark_calc, k0 = 1E2, distr_severity = "Gamma")
```

`copulaVis`*Interactive copula visualization*

Description

Opens an interactive Shiny app for the selected copula and modules.

Usage

```
copulaVis(copula, modules)
```

Arguments

<code>copula</code>	Copula to visualize, presently one of : <ul style="list-style-type: none">• "Independant": Independant copula.• "FrechetLowerBound": Fréchet Lower Bound copula.• "FrechetUpperBound": Fréchet Upper Bound copula.• "BivariateEFGM": Eyraud-Farlie-Gumbel-Morgenstern copula.• "Frechet": Fréchet copula.• "BivariateCA": Bivariate Cuadras-Augé copula.• "BivariateMO": Bivariate Marshall-Olkin copula.• "BivariateAMH": Bivariate Ali-Mikhail-Haq copula.• "BivariateClayton": Bivariate Clayton copula.• "BivariateFrank": Bivariate Frank copula.• "BivariateGumbel": Bivariate Gumbel copula.
<code>modules</code>	Vector of modules to visualize, one of : <ul style="list-style-type: none">• "all": Renders all boxes.• "simulationsPlot": Plot of simulations.• "distributionPlot": Plot of distribution.

Value

Launches Shiny application.

Examples

```
## Only run this example in interactive R sessions
if (interactive()) {
  copulaVis(copula = "BivariateEFGM", modules = "distributionPlot")
}
```

distributacalculVis *Interactive distribution visualization*

Description

Opens an interactive Shiny app for the selected distribution and modules.

Usage

```
distributacalculVis(law, mod)
```

Arguments

law	Distribution to visualize, presently one of these 2 parameter continuous distributions : <ul style="list-style-type: none">• "Norm": Normal distribution.• "Lnorm": Lognormal distribution.• "Gamma": Gamma distribution.• "Beta": Beta distribution.• "Unif": Uniform distribution.• "Llogis": Log-logistic distribution.• "Weibull": Weibull distribution.• "Pareto": Pareto distribution.
mod	Vector of modules to visualize, one of : <ul style="list-style-type: none">• "all": Renders all boxes.• "functions": Density and cumulative density functions• "moments": Various moments.• "riskMeasures": VaR and TVaR.

Value

Launches Shiny application.

Examples

```
## Only run this example in interactive R sessions
if (interactive()) {
  distributacalculVis(law = "Norm", mod = "functions")
}
```

Erl

*Hypergeometric Distribution***Description**

Hypergeometric distribution where we have a sample of k balls from an urn containing N , of which m are white and n are black.

Usage

`expValErl(N = n + m, m, n = N - m, k)`

`varErl(N = n + m, m, n = N - m, k)`

Arguments

N	Total number of balls (white and black) in the urn. $N = n + m$
m	Number of white balls in the urn.
n	Number of black balls in the urn. Can specify n instead of N .
k	Number of balls drawn from the urn, $k = 0, 1, \dots, m + n$.

Details

The Hypergeometric distribution for N total items of which m are of one type and n of the other and from which k items are picked has probability mass function :

$$Pr(X = x) = \frac{\binom{m}{x} \binom{n}{k-x}}{\binom{N}{k}}$$

for $x = 0, 1, \dots, \min(k, m)$.

Value

Function :

- `expValErl` gives the expected value.
- `varErl` gives the variance.

Invalid parameter values will return an error detailing which parameter is problematic.

Examples

```
# With total balls specified
expValErl(N = 5, m = 2, k = 2)

# With number of each colour of balls specified
expValErl(m = 2, n = 3, k = 2)

# With total balls specified
varErl(N = 5, m = 2, k = 2)

# With number of each colour of balls specified
varErl(m = 2, n = 3, k = 2)
```

erlang

Erlang Distribution

Description

Erlang distribution with shape parameter n and rate parameter β .

Usage

```
dErlang(x, shape, rate = 1/scale, scale = 1/rate)
pErlang(q, shape, rate = 1/scale, scale = 1/rate, lower.tail = TRUE)
expValErlang(shape, rate = 1/scale, scale = 1/rate)
varErlang(shape, rate = 1/scale, scale = 1/rate)
kthMomentErlang(k, shape, rate = 1/scale, scale = 1/rate)
expVallimErlang(d, shape, rate = 1/scale, scale = 1/rate)
expValTruncErlang(d, shape, rate = 1/scale, scale = 1/rate, less.than.d = TRUE)
stopLossErlang(d, shape, rate = 1/scale, scale = 1/rate)
meanExcessErlang(d, shape, rate = 1/scale, scale = 1/rate)
VatRErlang(kap, shape, rate = 1/scale, scale = 1/rate)
TVatRErlang(kap, shape, rate = 1/scale, scale = 1/rate)
mgfErlang(t, shape, rate = 1/scale, scale = 1/rate)
```


Arguments

x	vector of quantiles.
shape	shape parameter n , must be a positive integer.
rate	rate parameter β , must be positive.
scale	alternative parameterization to the rate parameter, scale = 1 / rate.
q	vector of quantiles.
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
k	kth-moment.
d	cut-off value.
less.than.d	logical; if TRUE (default) truncated mean for values $\leq d$, otherwise, for values $> d$.
kap	probability.
t	t.

Details

The Erlang distribution with shape parameter n and rate parameter β has density:

$$f(x) = \frac{\beta^n}{\Gamma(n)} x^{n-1} e^{-\beta x}$$

for $x \in \mathcal{R}^+$, $\beta > 0$, $n \in \mathcal{N}^+$.

Value

Function :

- `dErlang` gives the probability density function (PDF).
- `pErlang` gives the cumulative density function (CDF).
- `expValErlang` gives the expected value.
- `varErlang` gives the variance.
- `kthMomentErlang` gives the kth moment.
- `expValLimErlang` gives the limited mean.
- `expValTruncErlang` gives the truncated mean.
- `stopLossErlang` gives the stop-loss.
- `meanExcessErlang` gives the mean excess loss.
- `VatRErlang` gives the Value-at-Risk.
- `TVatRErlang` gives the Tail Value-at-Risk.
- `mgfErlang` gives the moment generating function (MGF).

Invalid parameter values will return an error detailing which parameter is problematic.

Note

Function `VatRErlang` is a wrapper of the `qgamma` function from the `stats` package.

Examples

```
dErlang(x = 2, shape = 2, scale = 4)

pErlang(q = 2, shape = 2, scale = 4)

expValErlang(shape = 2, scale = 4)

varErlang(shape = 2, scale = 4)

kthMomentErlang(k = 3, shape = 2, scale = 4)

expValLimErlang(d = 2, shape = 2, scale = 4)

# With rate parameter
expValTruncErlang(d = 2, shape = 2, scale = 4)

# Values greater than d
expValTruncErlang(d = 2, shape = 2, scale = 4, less.than.d = FALSE)

stopLossErlang(d = 2, shape = 2, scale = 4)

meanExcessErlang(d = 3, shape = 2, scale = 4)

# With scale parameter
VatRErlang(kap = .2, shape = 2, scale = 4)

# With rate parameter
VatRErlang(kap = .2, shape = 2, rate = 0.25)

# With scale parameter
TVatRErlang(kap = .2, shape = 3, scale = 4)

# With rate parameter
TVatRErlang(kap = .2, shape = 3, rate = 0.25)

mgfErlang(t = 2, shape = 2, scale = .25)
```

 Exp

Exponential Distribution

Description

Exponential distribution with rate parameter β .

Usage

```

expValExp(rate = 1/scale, scale = 1/rate)

varExp(rate = 1/scale, scale = 1/rate)

kthMomentExp(k, rate = 1/scale, scale = 1/rate)

expValLimExp(d, rate = 1/scale, scale = 1/rate)

expValTruncExp(d, rate = 1/scale, scale = 1/rate, less.than.d = TRUE)

stopLossExp(d, rate = 1/scale, scale = 1/rate)

meanExcessExp(d, rate = 1/scale, scale = 1/rate)

VatRExp(kap, rate = 1/scale, scale = 1/rate)

TVatRExp(kap, rate = 1/scale, scale = 1/rate)

mgfExp(t, rate = 1/scale, scale = 1/rate)

```

Arguments

rate	rate parameter β , must be positive.
scale	alternative parameterization to the rate parameter, scale = 1 / rate.
k	kth-moment.
d	cut-off value.
less.than.d	logical; if TRUE (default) truncated mean for values $\leq d$, otherwise, for values $> d$.
kap	probability.
t	t.

Details

The Exponential distribution with rate parameter β has density:

$$f(x) = \frac{1}{\beta} e^{-\beta x}$$

$f(x) = b^a e^{-b x}$ for $x \in \mathcal{R}^+$, $\beta > 0$.

Value

Function :

- `expValExp` gives the expected value.
- `varExp` gives the variance.

- `kthMomentExp` gives the kth moment.
- `expValLimExp` gives the limited mean.
- `expValTruncExp` gives the truncated mean.
- `stopLossExp` gives the stop-loss.
- `meanExcessExp` gives the mean excess loss.
- `VatRExp` gives the Value-at-Risk.
- `TVatRExp` gives the Tail Value-at-Risk.
- `mgfExp` gives the moment generating function (MGF).

Invalid parameter values will return an error detailing which parameter is problematic.

Note

Function `VatRExp` is a wrapper of the `qexp` function from the `stats` package.

Examples

```
# With scale parameter
expValExp(scale = 4)

# With rate parameter
expValExp(rate = 0.25)

# With scale parameter
varExp(scale = 4)

# With rate parameter
varExp(rate = 0.25)

# With scale parameter
kthMomentExp(k = 2, scale = 4)

# With rate parameter
kthMomentExp(k = 2, rate = 0.25)

# With scale parameter
expValLimExp(d = 2, scale = 4)

# With rate parameter
expValLimExp(d = 2, rate = 0.25)

# With scale parameter
expValTruncExp(d = 2, scale = 4)

# With rate parameter, values greater than d
expValTruncExp(d = 2, rate = 0.25, less.than.d = FALSE)

# With scale parameter
stopLossExp(d = 2, scale = 4)
```

```

# With rate parameter
stopLossExp(d = 2, rate = 0.25)

# With scale parameter
meanExcessExp(d = 2, scale = 4)

# With rate parameter
meanExcessExp(d = 5, rate = 0.25)

# With scale parameter
VatRExp(kap = .99, scale = 4)

# With rate parameter
VatRExp(kap = .99, rate = 0.25)

# With scale parameter
TVatRExp(kap = .99, scale = 4)

# With rate parameter
TVatRExp(kap = .99, rate = 0.25)

mgfExp(t = 1, rate = 5)

```

 frechet

Fréchet Copula

Description

Computes CDF and simulations of the Fréchet copula.

Usage

```
cFrechet(u1, u2, dependencyParameter, ...)
```

```
crFrechet(numberSimulations = 10000, seed = 42, dependencyParameter)
```

Arguments

u1, u2 points at which to evaluate the copula.
 dependencyParameter correlation parameters, must be vector of length 2.
 ... other parameters.
 numberSimulations Number of simulations.
 seed Simulation seed, 42 by default.

Details

The Fréchet copula has CDF :

$$C(u_1, u_2) = (1 - \alpha - \beta)(u_1 \times u_2) + \alpha \min(u_1, u_2) + \beta \max(u_1 + u_2 - 1, 0)$$

for $u_1, u_2, \alpha, \beta \in [0, 1]$ and $\alpha + \beta \leq 1$.

Value

Function :

- `cFrechet` returns the value of the copula.
- `crFrechet` returns simulated values of the copula.

Examples

```
cFrechet(u1 = .76, u2 = 0.4, dependencyParameter = c(0.2, 0.3))
```

```
crFrechet(numberSimulations = 10, seed = 42, dependencyParameter = c(0.2, 0.3))
```

frechetLowerBound	<i>Fréchet Lower Bound Copula</i>
-------------------	-----------------------------------

Description

Computes CDF and simulations of the Fréchet lower bound copula.

Usage

```
cFrechetLowerBound(u1, u2, ...)
```

```
crFrechetLowerBound(numberSimulations = 10000, seed = 42)
```

Arguments

u1, u2	points at which to evaluate the copula.
...	other parameters.
numberSimulations	Number of simulations.
seed	Simulation seed, 42 by default.

Details

The Fréchet lower bound copula has CDF :

$$C(u_1, u_2) = \max(u_1 + u_2 - 1, 0)$$

for $u_1, u_2 \in [0, 1]$.

Value

Function :

- `cFrechetLowerBound` returns the value of the copula.
- `crFrechetLowerBound` returns simulated values of the copula.

Examples

```
cFrechetLowerBound(u1 = .76, u2 = 0.4)
```

```
crFrechetLowerBound(numberSimulations = 10, seed = 42)
```

frechetUpperBound	<i>Fréchet Upper Bound Copula</i>
-------------------	-----------------------------------

Description

Computes CDF and simulations of the Fréchet upper bound copula.

Usage

```
cFrechetUpperBound(u1, u2, ...)
```

```
crFrechetUpperBound(numberSimulations = 10000, seed = 42)
```

Arguments

u1, u2	points at which to evaluate the copula.
...	other parameters.
numberSimulations	Number of simulations.
seed	Simulation seed, 42 by default.

Details

The Fréchet upper bound copula has CDF :

$$C(u_1, u_2) = \min(u_1, u_2)$$

for $u_1, u_2 \in [0, 1]$.

Value

Function :

- `cFrechetUpperBound` returns the value of the copula.
- `crFrechetUpperBound` returns simulated values of the copula.

Examples

```
cFrechetUpperBound(u1 = .56, u2 = 0.4)
crFrechetUpperBound(numberSimulations = 10, seed = 42)
```

Gamma

*Gamma Distribution***Description**

Gamma distribution with shape parameter α and rate parameter β .

Usage

```
expValGamma(shape, rate = 1/scale, scale = 1/rate)
varGamma(shape, rate = 1/scale, scale = 1/rate)
kthMomentGamma(k, shape, rate = 1/scale, scale = 1/rate)
expVallimGamma(d, shape, rate = 1/scale, scale = 1/rate)
expValTruncGamma(d, shape, rate = 1/scale, scale = 1/rate, less.than.d = TRUE)
stopLossGamma(d, shape, rate = 1/scale, scale = 1/rate)
meanExcessGamma(d, shape, rate = 1/scale, scale = 1/rate)
VatRGamma(kap, shape, rate = 1/scale, scale = 1/rate)
TVatRGamma(kap, shape, rate = 1/scale, scale = 1/rate)
mgfGamma(t, shape, rate = 1/scale, scale = 1/rate)
```

Arguments

shape	shape parameter α , must be positive.
rate	rate parameter β , must be positive.
scale	alternative parameterization to the rate parameter, scale = 1 / rate.
k	kth-moment.
d	cut-off value.
less.than.d	logical; if TRUE (default) truncated mean for values $\leq d$, otherwise, for values $> d$.
kap	probability.
t	t.

Details

The Gamma distribution with shape parameter α and rate parameter β has density:

$$f(x) = \frac{\beta^\alpha}{\Gamma(\alpha)} x^{\alpha-1} e^{-\beta x}$$

for $x \in \mathcal{R}^+, \beta, \alpha > 0$.

Value

Function :

- `expValGamma` gives the expected value.
- `varGamma` gives the variance.
- `kthMomentGamma` gives the kth moment.
- `expValLimGamma` gives the limited mean.
- `expValTruncGamma` gives the truncated mean.
- `stopLossGamma` gives the stop-loss.
- `meanExcessGamma` gives the mean excess loss.
- `VatGamma` gives the Value-at-Risk.
- `TVatGamma` gives the Tail Value-at-Risk.
- `mgfGamma` gives the moment generating function (MGF).

Invalid parameter values will return an error detailing which parameter is problematic.

Note

Function `VatGamma` is a wrapper for the `qgamma` function stats package.

Examples

```
# With scale parameter
expValGamma(shape = 3, scale = 4)

# With rate parameter
expValGamma(shape = 3, rate = 0.25)

# With scale parameter
varGamma(shape = 3, scale = 4)

# With rate parameter
varGamma(shape = 3, rate = 0.25)

# With scale parameter
kthMomentGamma(k = 2, shape = 3, scale = 4)
```

```
# With rate parameter
kthMomentGamma(k = 2, shape = 3, rate = 0.25)

# With scale parameter
expValLimGamma(d = 2, shape = 3, scale = 4)

# With rate parameter
expValLimGamma(d = 2, shape = 3, rate = 0.25)

# With scale parameter
expValTruncGamma(d = 2, shape = 3, scale = 4)

# With rate parameter
expValTruncGamma(d = 2, shape = 3, rate = 0.25)

# values greather than d
expValTruncGamma(d = 2, shape = 3, rate = 0.25, less.than.d = FALSE)

# With scale parameter
stopLossGamma(d = 2, shape = 3, scale = 4)

# With rate parameter
stopLossGamma(d = 2, shape = 3, rate = 0.25)

# With scale parameter
meanExcessGamma(d = 2, shape = 3, scale = 4)

# With rate parameter
meanExcessGamma(d = 2, shape = 3, rate = 0.25)

# With scale parameter
VatGamma(kap = .2, shape = 3, scale = 4)

# With rate parameter
VatGamma(kap = .2, shape = 3, rate = 0.25)

# With scale parameter
TVatGamma(kap = .2, shape = 3, scale = 4)

# With rate parameter
TVatGamma(kap = .2, shape = 3, rate = 0.25)

mgfGamma(t = 1, shape = 3, rate = 5)
```

 IG *Inverse Gaussian Distribution*

Description

Inverse Gaussian distribution with mean μ and shape parameter β .

Usage

```

expValIG(mean, shape = dispersion * mean^2, dispersion = shape/mean^2)
varIG(mean, shape = dispersion * mean^2, dispersion = shape/mean^2)
expValLimIG(d, mean, shape = dispersion * mean^2, dispersion = shape/mean^2)
expValTruncIG(
  d,
  mean,
  shape = dispersion * mean^2,
  dispersion = shape/mean^2,
  less.than.d = TRUE
)
stopLossIG(d, mean, shape = dispersion * mean^2, dispersion = shape/mean^2)
meanExcessIG(d, mean, shape = dispersion * mean^2, dispersion = shape/mean^2)
VatRIG(kap, mean, shape = dispersion * mean^2, dispersion = shape/mean^2)
TVatRIG(kap, mean, shape = dispersion * mean^2, dispersion = shape/mean^2)
mgfIG(t, mean, shape = dispersion * mean^2, dispersion = shape/mean^2)

```

Arguments

mean	mean (location) parameter μ , must be positive.
shape	shape parameter β , must be positive
dispersion	alternative parameterization to the shape parameter, dispersion = 1 / rate.
d	cut-off value.
less.than.d	logical; if TRUE (default) truncated mean for values $\leq d$, otherwise, for values $> d$.
kap	probability.
t	t.

Details

The Inverse Gaussian distribution with

Value

Function :

- `expValIG` gives the expected value.
- `varIG` gives the variance.
- `expValLimIG` gives the limited mean.
- `expValTruncIG` gives the truncated mean.
- `stopLossIG` gives the stop-loss.
- `meanExcessIG` gives the mean excess loss.
- `VatRIG` gives the Value-at-Risk.
- `TVatRIG` gives the Tail Value-at-Risk.
- `mgfIG` gives the moment generating function (MGF).

Invalid parameter values will return an error detailing which parameter is problematic.

Note

Function `VatRIG` is a wrapper for the `qinvgauss` function from the `statmod` package.

Examples

```
expValIG(mean = 2, shape = 5)
```

```
varIG(mean = 2, shape = 5)
```

```
expValLimIG(d = 2, mean = 2, shape = 5)
```

```
expValTruncIG(d = 2, mean = 2, shape = 5)
```

```
stopLossIG(d = 2, mean = 2, shape = 5)
```

```
meanExcessIG(d = 2, mean = 2, shape = 5)
```

```
VatRIG(kap = 0.99, mean = 2, shape = 5)
```

```
TVatRIG(kap = 0.99, mean = 2, shape = 5)
```

```
mgfIG(t = 1, mean = 2, shape = .5)
```

independent	<i>Independence Copula</i>
-------------	----------------------------

Description

Computes CDF and simulations of the independence copula.

Usage

```
cIndependent(u1, u2, ...)
```

```
crIndependent(numberSimulations = 10000, seed = 42)
```

Arguments

u1, u2	points at which to evaluate the copula.
...	other parameters.
numberSimulations	Number of simulations.
seed	Simulation seed, 42 by default.

Details

The independence copula has CDF :

$$C(u_1, u_2) = u_1 \times u_2$$

for $u_1, u_2 \in [0, 1]$.

Value

Function :

- `cIndependent` returns the value of the copula.
- `crIndependent` returns simulated values of the copula.

Examples

```
cIndependent(u1 = .76, u2 = 0.4)
```

```
crIndependent(numberSimulations = 10, seed = 42)
```

llogis *Loglogistic Distribution*

Description

Loglogistic distribution with shape parameter τ and scale parameter λ .

Usage

```

dLlogis(x, shape, rate = 1/scale, scale = 1/rate)
pLlogis(q, shape, rate = 1/scale, scale = 1/rate, lower.tail = TRUE)
expValLlogis(shape, rate = 1/scale, scale = 1/rate)
varLlogis(shape, rate = 1/scale, scale = 1/rate)
kthMomentLlogis(k, shape, rate = 1/scale, scale = 1/rate)
expValLimLlogis(d, shape, rate = 1/scale, scale = 1/rate)
expValTruncLlogis(d, shape, rate = 1/scale, scale = 1/rate, less.than.d = TRUE)
stopLossLlogis(d, shape, rate = 1/scale, scale = 1/rate)
meanExcessLlogis(d, shape, rate = 1/scale, scale = 1/rate)
VatRLlogis(kap, shape, rate = 1/scale, scale = 1/rate)
TVatRLlogis(kap, shape, rate = 1/scale, scale = 1/rate)

```

Arguments

x	vector of quantiles.
shape	shape parameter τ , must be positive
rate	rate parameter β , must be positive.
scale	alternative parameterization to the rate parameter, scale = 1 / rate.
q	vector of quantiles.
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
k	kth-moment.
d	cut-off value.
less.than.d	logical; if TRUE (default) truncated mean for values $\leq d$, otherwise, for values $> d$.
kap	probability.

Details

The loglogistic distribution with shape parameter τ and scale parameter λ has density:

$$\frac{\tau \lambda^\tau x^{\tau-1}}{(\lambda^\tau + x^\tau)^2}$$

for $x \in \mathcal{R}^+$, $\lambda, \tau > 0$.

Value

Function :

- `dLlogis` gives the probability density function (PDF).
- `pLlogis` gives the cumulative density function (CDF).
- `expValLlogis` gives the expected value.
- `varLlogis` gives the variance.
- `kthMomentLlogis` gives the kth moment.
- `expValLimLlogis` gives the limited mean.
- `expValTruncLlogis` gives the truncated mean.
- `stopLossLlogis` gives the stop-loss.
- `meanExcessLlogis` gives the mean excess loss.
- `VatRLlogis` gives the Value-at-Risk.
- `TVatRLlogis` gives the Tail Value-at-Risk.

Invalid parameter values will return an error detailing which parameter is problematic.

Examples

```
dLlogis(x = 2, shape = 2, scale = 4)

# With scale parameter
pLlogis(q = 3, shape = 3, scale = 5)

# With rate parameter
pLlogis(q = 3, shape = 3, rate = 0.2)

# Survival function
pLlogis(q = 3, shape = 3, rate = 0.2, lower.tail = FALSE)

expValLlogis(shape = 2, scale = 4)

varLlogis(shape = 3, scale = 4)

kthMomentLlogis(k = 3, shape = 5, scale = 4)

expValLimLlogis(d = 2, shape = 2, scale = 4)

# With rate parameter
```

```

expValTruncLlogis(d = 2, shape = 2, scale = 4)

# Values greater than d
expValTruncLlogis(d = 2, shape = 2, scale = 4, less.than.d = FALSE)

stopLossLlogis(d = 2, shape = 2, scale = 4)

meanExcessLlogis(d = 3, shape = 2, scale = 4)

# With scale parameter
VatRLlogis(kap = .2, shape = 2, scale = 4)

# With rate parameter
VatRLlogis(kap = .2, shape = 2, rate = 0.25)

# With scale parameter
TVatRLlogis(kap = .2, shape = 3, scale = 4)

# With rate parameter
TVatRLlogis(kap = .2, shape = 3, rate = 0.25)

```

Lnorm

Lognormal Distribution

Description

Lognormal distribution with mean μ and variance σ .

Usage

```

expValLnorm(meanlog, sdlog)

varLnorm(meanlog, sdlog)

kthMomentLnorm(k, meanlog, sdlog)

expValLimLnorm(d, meanlog, sdlog)

expValTruncLnorm(d, meanlog, sdlog, less.than.d = TRUE)

stopLossLnorm(d, meanlog, sdlog)

meanExcessLnorm(d, meanlog, sdlog)

VatRLnorm(kap, meanlog, sdlog)

TVatRLnorm(kap, meanlog, sdlog)

```


Arguments

meanlog	location parameter μ .
sdlog	standard deviation σ , must be positive.
k	kth-moment.
d	cut-off value.
less.than.d	logical; if TRUE (default) truncated mean for values $\leq d$, otherwise, for values $> d$.
kap	probability.

Details

The Log-normal distribution with mean μ and standard deviation σ has density:

$$\frac{1}{\sqrt{2\pi\sigma x}} e^{-\frac{1}{2}\left(\frac{\ln(x)-\mu}{\sigma}\right)^2}$$

for $x \in \mathcal{R}^+$, $\mu \in \mathcal{R}$, $\sigma > 0$.

Value

Function :

- `expValLnorm` gives the expected value.
- `varLnorm` gives the variance.
- `kthMomentLnorm` gives the kth moment.
- `expValLimLnorm` gives the limited mean.
- `expValTruncLnorm` gives the truncated mean.
- `stopLossLnorm` gives the stop-loss.
- `meanExcessLnorm` gives the mean excess loss.
- `VatRLnorm` gives the Value-at-Risk.
- `TVatRLnorm` gives the Tail Value-at-Risk.

Invalid parameter values will return an error detailing which parameter is problematic.

Note

Function `VatRLnorm` is a wrapper of the `qlnorm` function from the stats package.

Examples

```
expValLnorm(meanlog = 3, sdlog = 5)
varLnorm(meanlog = 3, sdlog = 5)
kthMomentLnorm(k = 2, meanlog = 3, sdlog = 5)
expValLimLnorm(d = 2, meanlog = 2, sdlog = 5)
```

```

expValTruncLnorm(d = 2, meanlog = 2, sdlog = 5)

# Values greater than d
expValTruncLnorm(d = 2, meanlog = 2, sdlog = 5, less.than.d = FALSE)

stopLossLnorm(d = 2, meanlog = 2, sdlog = 5)

meanExcessLnorm(d = 2, meanlog = 2, sdlog = 5)

VatRLnorm(kap = 0.8, meanlog = 3, sdlog = 5)

TVatRLnorm(kap = 0.8, meanlog = 2, sdlog = 5)

```

Logarithmic

Logarithmic Distribution

Description

Logarithmic distribution with probability parameter γ .

Usage

```

dLogarithmic(x, prob)

pLogarithmic(q, prob, lower.tail = TRUE)

expValLogarithmic(prob)

varLogarithmic(prob)

VatRLogarithmic(kap, prob)

mgfLogarithmic(t, prob)

pgfLogarithmic(t, prob)

```

Arguments

x	vector of quantiles.
prob	probability parameter γ .
q	vector of quantiles.
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
kap	probability.
t	t.

Details

The Logarithmic distribution with probability parameter γ has probability mass function :

$$Pr(X = k) = \frac{-\gamma^k}{\ln(1 - \gamma)k}$$

, for $k = 0, 1, 2, \dots$, and $\gamma \in (0, 1]$.

Value

Function :

- `dLogarithmic` gives the probability density function (PDF).
- `pLogarithmic` gives the cumulative density function (CDF).
- `expValLogarithmic` gives the expected value.
- `varLogarithmic` gives the variance.
- `VatRLogarithmic` gives the Value-at-Risk.
- `mgfLogarithmic` gives the moment generating function (MGF).
- `pgfLogarithmic` gives the probability generating function (MGF).

Invalid parameter values will return an error detailing which parameter is problematic.

Examples

```
dLogarithmic(x = 3, prob = 0.2)
```

```
pLogarithmic(q = 3, prob = 0.2)
```

```
expValLogarithmic(prob = 0.50)
```

```
varLogarithmic(prob = 0.50)
```

```
VatRLogarithmic(kap = 0.99, prob = 0.2)
```

```
mgfLogarithmic(t = .2, prob = 0.50)
```

```
pgfLogarithmic(t = .2, prob = 0.50)
```

NBinom

Negative Binomial Distribution

Description

Negative binomial distribution with parameters r (number of successful trials) and p (probability of success).

Usage

```

expValNBinom(
  size,
  prob = (1/(1 + beta)),
  beta = ((1 - prob)/prob),
  nb_tries = FALSE
)

varNBinom(
  size,
  prob = (1/(1 + beta)),
  beta = ((1 - prob)/prob),
  nb_tries = FALSE
)

mgfNBinom(
  t,
  size,
  prob = (1/(1 + beta)),
  beta = ((1 - prob)/prob),
  nb_tries = FALSE
)

pgfNBinom(
  t,
  size,
  prob = (1/(1 + beta)),
  beta = ((1 - prob)/prob),
  nb_tries = FALSE
)

```

Arguments

size	Number of successful trials.
prob	Probability of success in each trial.
beta	Alternative parameterization of the negative binomial distribution where beta = (1 - p) / p.
nb_tries	logical; if FALSE (default) number of trials until the rth success, otherwise, number of failures until the rth success.
t	t.

Details

When k is the number of failures until the r th success, with a probability p of a success, the negative binomial has density:

$$\binom{r+k-1}{k} (p)^r (1-p)^k$$

for $k \in \{0, 1, \dots\}$

When k is the number of trials until the r th success, with a probability p of a success, the negative binomial has density:

$$\binom{k-1}{r-1} (p)^r (1-p)^{k-r}$$

for $k \in \{r, r+1, r+2, \dots\}$

The alternative parameterization of the negative binomial with parameter β , and k being the number of trials, has density:

$$\frac{\Gamma(r+k)}{\Gamma(r)k!} \left(\frac{1}{1+\beta}\right)^r \left(\frac{\beta}{1+\beta}\right)^{k-r}$$

for $k \in \{0, 1, \dots\}$

Value

Function :

- `expValNBinom` gives the expected value.
- `varNBinom` gives the variance.
- `mgfNBinom` gives the moment generating function (MGF).
- `pgfNBinom` gives the probability generating function (PGF).

Invalid parameter values will return an error detailing which parameter is problematic.

Examples

```
# Where k is the number of trials for a rth success
expValNBinom(size = 2, prob = .4)

# Where k is the number of failures before a rth success
expValNBinom(size = 2, prob = .4, nb_tries = TRUE)

# With alternative parameterization where k is the number of trials
expValNBinom(size = 2, beta = 1.5)

# Where k is the number of trials for a rth success
varNBinom(size = 2, prob = .4)

# Where k is the number of failures before a rth success
varNBinom(size = 2, prob = .4, nb_tries = TRUE)

# With alternative parameterization where k is the number of trials
varNBinom(size = 2, beta = 1.5)

mgfNBinom(t = 1, size = 4, prob = 0.5)

pgfNBinom(t = 5, size = 3, prob = 0.3)
```

Norm	<i>Normal Distribution</i>
------	----------------------------

Description

Normal distribution

Usage

`expValNorm(mean, sd)`

`varNorm(mean, sd)`

`expValLimNorm(d, mean = 0, sd = 1)`

`expValTruncNorm(d, mean = 0, sd = 1, less.than.d = TRUE)`

`stopLossNorm(d, mean = 0, sd = 1)`

`meanExcessNorm(d, mean = 0, sd = 1)`

`VatRNorm(kap, mean = 0, sd = 1)`

`TVatRNorm(kap, mean = 0, sd = 1)`

`mgfNorm(t, mean = 0, sd = 1)`

Arguments

mean	mean (location) parameter μ .
sd	standard deviation σ , must be positive.
d	cut-off value.
less.than.d	logical; if TRUE (default) truncated mean for values $\leq d$, otherwise, for values $> d$.
kap	probability.
t	t.

Details

The Normal distribution with mean μ and standard deviation σ has density:

$$\frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}$$

for $x \in \mathcal{R}, \mu \in \mathcal{R}, \sigma > 0$.

Value

Function :

- `expValNorm` gives the expected value.
- `varNorm` gives the variance.
- `expValLimNorm` gives the limited mean.
- `expValTruncNorm` gives the truncated mean.
- `stopLossNorm` gives the stop-loss.
- `meanExcessNorm` gives the mean excess loss.
- `VatRNorm` gives the Value-at-Risk.
- `TVatRNorm` gives the Tail Value-at-Risk.
- `mgfNorm` gives the moment generating function (MGF).

Invalid parameter values will return an error detailing which parameter is problematic.

Note

Function `VatRNorm` is a wrapper of the `qnorm` function from the `stats` package.

Examples

```
expValNorm(mean = 3, sd = 5)
```

```
varNorm(mean = 3, sd = 5)
```

```
expValLimNorm(d = 2, mean = 2, sd = 5)
```

```
expValTruncNorm(d = 2, mean = 2, sd = 5)
```

```
stopLossNorm(d = 2, mean = 2, sd = 5)
```

```
meanExcessNorm(d = 2, mean = 2, sd = 5)
```

```
VatRNorm(kap = 0.8, mean = 3, sd = 5)
```

```
TVatRNorm(kap = 0.8, mean = 2, sd = 5)
```

```
mgfNorm(t = 1, mean = 3, sd = 5)
```

Pareto

*Pareto Distribution***Description**

Pareto distribution with shape parameter α and rate parameter λ .

Usage

```

dPareto(x, shape, rate = 1/scale, scale = 1/rate)
pPareto(q, shape, rate = 1/scale, scale = 1/rate, lower.tail = TRUE)
expValPareto(shape, rate = 1/scale, scale = 1/rate)
varPareto(shape, rate = 1/scale, scale = 1/rate)
kthMomentPareto(k, shape, rate = 1/scale, scale = 1/rate)
expVallimPareto(d, shape, rate = 1/scale, scale = 1/rate)
expValTruncPareto(d, shape, rate = 1/scale, scale = 1/rate, less.than.d = TRUE)
stopLossPareto(d, shape, rate = 1/scale, scale = 1/rate)
meanExcessPareto(d, shape, rate = 1/scale, scale = 1/rate)
VatRPareto(kap, shape, rate = 1/scale, scale = 1/rate)
TVatRPareto(kap, shape, rate = 1/scale, scale = 1/rate)

```

Arguments

x	vector of quantiles.
shape	shape parameter α , must be positive.
rate	rate parameter λ , must be positive.
scale	alternative parameterization to the rate parameter, $scale = 1 / rate$.
q	vector of quantiles.
lower.tail	logical; if TRUE (default), probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
k	kth-moment.
d	cut-off value.
less.than.d	logical; if TRUE (default) truncated mean for values $\leq d$, otherwise, for values $> d$.
kap	probability.

Details

The Pareto distribution with rate parameter λ as well as shape parameter α has density:

$$f(x) = \frac{\alpha \lambda^\alpha}{(\lambda + x)^{\alpha+1}}$$

for $x \in \mathcal{R}^+$, $\alpha, \lambda > 0$.

Value

Function :

- `dPareto` gives the probability density function (PDF).
- `pPareto` gives the cumulative density function (CDF).
- `expValPareto` gives the expected value.
- `varPareto` gives the variance.
- `kthMomentPareto` gives the kth moment.
- `expValLimPareto` gives the limited mean.
- `expValTruncPareto` gives the truncated mean.
- `stopLossPareto` gives the stop-loss.
- `meanExcessPareto` gives the mean excess loss.
- `VatRPareto` gives the Value-at-Risk.
- `TVatRPareto` gives the Tail Value-at-Risk.

Invalid parameter values will return an error detailing which parameter is problematic.

Examples

```
# With scale parameter
dPareto(x = 2, shape = 2, scale = 5)

# With rate parameter
dPareto(x = 2, shape = 2, rate = .20)

# With scale parameter
pPareto(q = 2, shape = 2, scale = 5)

# With rate parameter
pPareto(q = 2, shape = 2, rate = 0.20)

# Survival function
pPareto(q = 2, shape = 2, rate = 0.20, lower.tail = FALSE)

# With scale parameter
expValPareto(shape = 5, scale = 0.5)

# With rate parameter
expValPareto(shape = 5, rate = 2)
```

```
# With scale parameter
varPareto(shape = 5, scale = 0.5)

# With rate parameter
varPareto(shape = 5, rate = 2)

# With scale parameter
kthMomentPareto(k = 4, shape = 5, scale = 0.5)

# With rate parameter
kthMomentPareto(k = 4, shape = 5, rate = 2)

# With scale parameter
expValLimPareto(d = 4, shape = 5, scale = 0.5)

# With rate parameter
expValLimPareto(d = 4, shape = 5, rate = 2)

# With scale parameter
expValTruncPareto(d = 4, shape = 5, scale = 0.5)

# With rate parameter
expValTruncPareto(d = 4, shape = 5, rate = 2)

# With scale parameter
stopLossPareto(d = 2, shape = 5, scale = 0.5)

# With rate parameter
stopLossPareto(d = 2, shape = 5, rate = 2)

# With scale parameter
meanExcessPareto(d = 6, shape = 5, scale = 0.5)

# With rate parameter
meanExcessPareto(d = 6, shape = 5, rate = 2)

# With scale parameter
VatRPareto(kap = .99, shape = 5, scale = 0.5)

# With rate parameter
VatRPareto(kap = .99, shape = 5, rate = 2)

# With scale parameter
TVatRPareto(kap = .99, shape = 5, scale = 0.5)

# With rate parameter
TVatRPareto(kap = .99, shape = 5, rate = 2)
```

Description

Poisson distribution with rate parameter λ .

Usage

`expValPois(lambda)`

`varPois(lambda)`

`expValTruncPois(d, lambda, k0, less.than.d = TRUE)`

`TVatRPois(kap, lambda, k0)`

`mgfPois(t, lambda)`

`pgfPois(t, lambda)`

Arguments

<code>lambda</code>	Rate parameter λ .
<code>d</code>	cut-off value.
<code>k0</code>	point up to which to sum the distribution for the approximation.
<code>less.than.d</code>	logical; if TRUE (default) truncated mean for values $\leq d$, otherwise, for values $> d$.
<code>kap</code>	probability.
<code>t</code>	t.

Details

The Poisson distribution with rate parameter λ has probability mass function :

$$Pr(X = k) = \frac{\lambda^k e^{-\lambda}}{k!}$$

for $k = 0, 1, 2, \dots$, and $\lambda > 0$

Value

Function :

- `expValPois` gives the expected value.
- `varPois` gives the variance.
- `expValTruncPois` gives the truncated mean.
- `TVatRPois` gives the Tail Value-at-Risk.
- `mgfPois` gives the moment generating function (MGF).
- `pgfPois` gives the probability generating function (PGF).

Invalid parameter values will return an error detailing which parameter is problematic.

Examples

```

expValPois(lambda = 3)

varPois(lambda = 3)

expValTruncPois(d = 0, lambda = 2, k0 = 2E2, less.than.d = FALSE)
expValTruncPois(d = 2, lambda = 2, k0 = 2E2, less.than.d = TRUE)

TVatRPois(kap = 0.8, lambda = 3, k0 = 2E2)

mgfPois(t = 1, lambda = 3)

pgfPois(t = 1, lambda = 3)

```

```
simulatedCopulaHexPlot
```

Plot of simulated observations for copula

Description

Plot of simulated observations for copula

Usage

```

simulatedCopulaHexPlot(
  copula,
  numberSimulations = 10000,
  seed = 42,
  dependencyParameter
)

```

Arguments

copula Copula to visualize, presently one of :

- "Independant": Independant copula.
- "FrechetLowerBound": Fréchet Lower Bound copula.
- "FrechetUpperBound": Fréchet Upper Bound copula.
- "BivariateEFGM": Eyraud-Farlie-Gumbel-Morgenstern copula.
- "Frechet": Fréchet copula.
- "BivariateCA": Bivariate Cuadras-Augé copula.
- "BivariateMO": Bivariate Marhsall-Olkin copula.
- "BivariateAMH": Bivariate Ali-Mikhail-Haq copula.
- "BivariateClayton": Bivariate Clayton copula.
- "BivariateFrank": Bivariate Frank copula.
- "BivariateGumbel": Bivariate Gumbel copula.

numberSimulations Number of simulations.
 seed Simulation seed, 42 by default.
 dependencyParameter correlation parameter.

Value

Returns plot of simulated observations for the chosen copula.

Unif *Uniform Distribution*

Description

Uniform distribution with min a and max b .

Usage

expValUnif(min = 0, max = 1)
 varUnif(min = 0, max = 1)
 kthMomentUnif(k, min = 0, max = 1)
 expVallimUnif(d, min = 0, max = 1)
 expValTruncUnif(d, min = 0, max = 1, less.than.d = TRUE)
 stopLossUnif(d, min = 0, max = 1)
 meanExcessUnif(d, min = 0, max = 1)
 VatUnif(kap, min = 0, max = 1)
 TVatUnif(kap, min = 0, max = 1)
 mgfUnif(t, min = 0, max = 1)

Arguments

min lower and upper limits of the distribution. Must be finite.
 max lower and upper limits of the distribution. Must be finite.
 k kth-moment.
 d cut-off value.

less.than.d	logical; if TRUE (default) truncated mean for values $\leq d$, otherwise, for values $> d$.
kap	probability.
t	t.

Details

The (continuous) uniform distribution with min and max parameters a and b respectively has density:

$$f(x) = \frac{1}{b-a} \times \mathbf{1}_{\{x \in [a,b]\}}$$

for $x \in [a, b]$.

Value

Function :

- `expValUnif` gives the expected value.
- `varUnif` gives the variance.
- `kthMomentUnif` gives the kth moment.
- `expValLimUnif` gives the limited mean.
- `expValTruncUnif` gives the truncated mean.
- `stopLossUnif` gives the stop-loss.
- `meanExcessUnif` gives the mean excess loss.
- `VatRUnif` gives the Value-at-Risk.
- `TVatRUnif` gives the Tail Value-at-Risk.

Invalid parameter values will return an error detailing which parameter is problematic.

Examples

```
expValUnif(min = 3, max = 4)

varUnif(min = 3, max = 4)

kthMomentUnif(k = 2, min = 3, max = 4)

expValLimUnif(d = 3, min = 2, max = 4)

expValTruncUnif(d = 3, min = 2, max = 4)

# Values greather than d
expValTruncUnif(d = 3, min = 2, max = 4, less.than.d = FALSE)

stopLossUnif(d = 3, min = 2, max = 4)

meanExcessUnif(d = 2, min = 2, max = 4)
```

```
VatRUnif(kap = .99, min = 3, max = 4)
TVatRUnif(kap = .99, min = 3, max = 4)
mgfUnif(t = 2, min = 0, max = 1)
```

unifDiscr	<i>Discrete Uniform Distribution</i>
-----------	--------------------------------------

Description

Discrete uniform distribution with min a and max b .

Usage

```
pUnifD(q, min = 0, max = 1)
dUnifD(x, min = 0, max = 1)
varUnifD(min = 0, max = 1)
expValUnifD(min = 0, max = 1)
```

Arguments

q	vector of quantiles.
min	lower and upper limits of the distribution. Must be finite.
max	lower and upper limits of the distribution. Must be finite.
x	vector of quantiles.

Details

The (discrete) uniform distribution with min and max parameters a and b respectively has density:

$$\Pr(X = x) = \frac{1}{b - a + 1}$$

for $x \in \{a, a + 1, \dots, b - 1, b\}$.

Value

Function :

- `dUnifD` gives the probability density function (PDF).
- `pUnifD` gives the cumulative density function (CDF).
- `expValUnifD` gives the expected value.
- `varUnifD` gives the variance.

Invalid parameter values will return an error detailing which parameter is problematic.

Examples

```

pUnifD(q = 0.2, min = 0, max = 1)

dUnifD(min = 0, max = 1)

varUnifD(min = 0, max = 1)

expValUnifD(min = 0, max = 1)

```

Weibull

Weibull Distribution

Description

Weibull distribution with shape parameter τ and rate parameter β .

Usage

```

expValWeibull(shape, rate = 1/scale, scale = 1/rate)

varWeibull(shape, rate = 1/scale, scale = 1/rate)

kthMomentWeibull(k, shape, rate = 1/scale, scale = 1/rate)

expValLimWeibull(d, shape, rate = 1/scale, scale = 1/rate)

expValTruncWeibull(
  d,
  shape,
  rate = 1/scale,
  scale = 1/rate,
  less.than.d = TRUE
)

stopLossWeibull(d, shape, rate = 1/scale, scale = 1/rate)

meanExcessWeibull(d, shape, rate = 1/scale, scale = 1/rate)

VatRWeibull(kap, shape, rate = 1/scale, scale = 1/rate)

TVatRWeibull(kap, shape, rate = 1/scale, scale = 1/rate)

```

Arguments

shape	shape parameter τ , must be positive
rate	rate parameter β , must be positive.

scale	alternative parameterization to the rate parameter, scale = 1 / rate.
k	kth-moment.
d	cut-off value.
less.than.d	logical; if TRUE (default) truncated mean for values <= d, otherwise, for values > d.
kap	probability.

Details

The Weibull distribution with shape parameter τ and rate parameter β has density:

$$f(x) = \beta\tau (\beta x)^{\tau-1} e^{-(\beta x)^\tau}$$

for $x \in \mathcal{R}^+$, $\beta > 0$, $\tau > 0$

Value

Function :

- `expValWeibull` gives the expected value.
- `varWeibull` gives the variance.
- `kthMomentWeibull` gives the kth moment.
- `expValLimWeibull` gives the limited mean.
- `expValTruncWeibull` gives the truncated mean.
- `stopLossWeibull` gives the stop-loss.
- `meanExcessWeibull` gives the mean excess loss.
- `VatRWeibull` gives the Value-at-Risk.
- `TVatRWeibull` gives the Tail Value-at-Risk.

Invalid parameter values will return an error detailing which parameter is problematic.

Examples

```
# With scale parameter
expValWeibull(shape = 2, scale = 5)

# With rate parameter
expValWeibull(shape = 2, rate = 0.2)

# With scale parameter
varWeibull(shape = 2, scale = 5)

# With rate parameter
varWeibull(shape = 2, rate = 0.2)

# With scale parameter
kthMomentWeibull(k = 2, shape = 2, scale = 5)
```

```
# With rate parameter
kthMomentWeibull(k = 2, shape = 2, rate = 0.2)

# With scale parameter
expValLimWeibull(d = 2, shape = 2, scale = 5)

# With rate parameter
expValLimWeibull(d = 2, shape = 2, rate = 0.2)

# With scale parameter
expValTruncWeibull(d = 2, shape = 2, scale = 5)

# With rate parameter
expValTruncWeibull(d = 2, shape = 2, rate = 0.2)

# Mean of values greater than d
expValTruncWeibull(d = 2, shape = 2, rate = 0.2, less.than.d = FALSE)

# With scale parameter
stopLossWeibull(d = 2, shape = 3, scale = 4)

# With rate parameter
stopLossWeibull(d = 2, shape = 3, rate = 0.25)

# With scale parameter
meanExcessWeibull(d = 2, shape = 3, scale = 4)

# With rate parameter
meanExcessWeibull(d = 2, shape = 3, rate = 0.25)

# With scale parameter
VatRWeibull(kap = .2, shape = 3, scale = 4)

# With rate parameter
VatRWeibull(kap = .2, shape = 3, rate = 0.25)

# With scale parameter
TVatRWeibull(kap = .2, shape = 3, scale = 4)

# With rate parameter
TVatRWeibull(kap = .2, shape = 3, rate = 0.25)
```

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