Package ‘MUS’

March 20, 2019

Encoding UTF-8
Type Package
Title Monetary Unit Sampling and Estimation Methods, Widely Used in Auditing
Version 0.1.6
Date 2019-09-15
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Description Sampling and evaluation methods to apply Monetary Unit Sampling (or in older literature Dollar Unit Sampling) during an audit of financial statements.
Depends R (>= 3.4.0), stats
Suggests DescTools, pander
License GPL (>= 2)
NeedsCompilation no
BugReports https://github.com/alsguimaraes/MUS
Repository CRAN
Date/Publication 2019-03-20 21:34:48 UTC
RoxygenNote 6.1.1

R topics documented:

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Description

Sampling and evaluation methods to apply Monetary Unit Sampling (or in older literature Dollar Unit Sampling) during an audit of financial statements.

Details

Monetary Unit Sampling (MUS), also known as Dollar Unit Sampling (DUS) or Probability-Proportional-to-Size Sampling (PPS), is a sampling approach that is widely used in auditing.

This package was written mainly for a research project. However, it should be possible to use the methods for practical auditing, too. Furthermore, the package comes with ABSOLUTELY NO WARRANTY. Use it at your own risk!

You have to walk through four steps: 1. Plan a sample and determine the sample size, use function: MUS.planning 2. Extract the sample, use function: MUS.extract 3. Audit the extracted sample (e.g. by asking for debtor confirmations). 4. Evaluate the audited sample, use function: MUS.evaluation

Author(s)

Henning Prömpers, André Guimarães

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See Also

MUS.planning for planning a sample, MUS.extraction for extraction of the planned sample and MUS.evaluation for evaluation of the extracted and audited sample.

Examples

```r
# Simple Example
library(MUS)
# Assume 500 invoices, each between 1 and 1000 monetary units
e.xample.data.1 <- data.frame(book.value=round(runif(n=500, min=1, max=1000)))
# Plan a sample and cache it
plan.results.simple <- MUS.planning(data=example.data.1,
tolerable.error=100000, expected.error=20000)
# Extract a sample and cache it (no high values exist in this example)
```
extract.results.simple <- MUS.extraction(plan.results.simple)
# Copy book values into a new column audit values
audited.sample.simple <- extract.results.simple$sample
audited.sample.simple <- cbind(audited.sample.simple,
    audit.value=audited.sample.simple$book.value)
# Edit manually (if any audit difference occur)
#audited.sample.simple <- edit(audited.sample.simple)
# Evaluate the sample, cache and print it
evaluation.results.simple <- MUS.evaluation(extract.results.simple,
audited.sample.simple)
print(evaluation.results.simple)

MUS.binomial.bound  

Calculate a binomial bound for a Monetary Unit Sampling evaluation.

Description

Calculates a binomial bound for a Monetary Unit Sampling evaluation.
Please treat as experimental.

Usage

MUS.binomial.bound(x, scope, as.pct, include.high.values, confidence.level)

Arguments

x            A MUS.evaluation.result object (or a tainting vector) used to calculate the binomial bound.
scope        The required scope for the bound ("qty" or "value"). Default is "value".
as.pct       Boolean. Express results as percentage. Default is False.
include.high.values
            Boolean. Whether the bound should include high values. Default is "TRUE".
confidence.level
            The required confidence level. Default is 95%.

Value

Upper Error Limit calculated using the binomial bound.

Author(s)

Andre Guimaraes <alsguimaraes@gmail.com>

See Also

MUS.evaluation for evaluation of the audited sample.
Examples

# Assume 500 invoices, each between 1 and 1000 monetary units
data <- data.frame(book.value=round(runif(n=500, min=1, max=1000)))
# Plan a sample and cache it
plan <- MUS.planning(data=data, tolerable.error=10000, expected.error=2000)
# Extract a sample and cache it (no high values exist in this example)
extract <- MUS.extraction(plan)
# Copy book value into a new column audit values, and inject some error
audited <- extract$sample$book.value*(1-rbinom(nrow(extract$sample), 1, 0.05))
audited <- cbind(extract$sample, audit.value=audited)
# Evaluate the sample, cache and print it
evaluation <- MUS.evaluation(extract, audited)
MUS.binomial.bound(evaluation)

MUS.calc.n.conservative

*Calculate a conservative sample size.*

Description


Usage

`MUS.calc.n.conservative(confidence.level, tolerable.error, expected.error, book.value)`

Arguments

- `confidence.level` ditto.
- `tolerable.error` Tolerable error in monetary units.
- `expected.error` Expected error in monetary units.
- `book.value` Book value in monetary units.

Value

Returns the (conservative) sample size.

Author(s)

Andre Guimaraes <alsguimaraes@gmail.com>
Examples

MUS.calc.n.conservative(0.95, 100000, 50000, 1000000)

MUS.combine

Combine MUS objects (joining strata into a full set).

Description

Combine a list of MUS objects into a single object. Typical use case is to group multiple strata into a single object. Works with MUS.planning.result, MUS.extraction.result and MUS.evaluation.result objects.

Usage

MUS.combine(object.list)

Arguments

object.list A list of MUS.planning.result, MUS.extraction.result and MUS.evaluation.result objects.

Value

An object of the same type of the first item in the list is returned containing an aggregation of the objects in the list.

Author(s)

Andre Guimaraes <alsguimaraes@gmail.com>

Examples

## Simple Example

# Assume 500 invoices, each between 1 and 1000 monetary units
stratum.1 <- data.frame(book.value=round(runif(n=500, min=1, max=1000)))
plan.1 <- MUS.planning(data=stratum.1, tolerable.error=100000, expected.error=20000)
stratum.2 <- data.frame(book.value=round(runif(n=500, min=1, max=1000)))
plan.2 <- MUS.planning(data=stratum.2, tolerable.error=100000, expected.error=20000)
plan.combined <- MUS.combine(list(plan.1, plan.2))
print(plan.combined)
MUS.combined.high.error.rate

Calculate a high error rate bound for a combined Monetary Unit Sampling evaluation.

Description

Calculate a high error rate bound for a combined Monetary Unit Sampling evaluation.
Please treat as experimental.

Usage

MUS.combined.high.error.rate(evaluation, interval.type)

Arguments

- evaluation: A MUS.evaluation.result object used to calculate the combined bound.
- interval.type: Optional. Interval type for high error rate evaluation. Default is "one-sided".

Value

Upper Error Limit calculated using high error rate evaluation for a combined sample.

Author(s)

Andre Guimaraes <alsguimaraes@gmail.com>

See Also

MUS.evaluation for evaluation of the audited sample. MUS.combine for combining multiple evaluations.

Examples

# Assume 500 invoices, each between 1 and 1000 monetary units
data1 <- data.frame(book.value=round(runif(n=500, min=1, max=1000)))
# Plan a sample and cache it
plan1 <- MUS.planning(data=data1, tolerable.error=1000, expected.error=2000)
# Extract a sample and cache it (no high values exist in this example)
extract1 <- MUS.extraction(plan1)
# Copy book value into a new column audit values, and inject some error
audited1 <- extract1$sample$book.value*(1-rbinom(nrow(extract1$sample), 1, 0.05))
audited1 <- cbind(extract1$sample, audit.value=audited1)
# Evaluate the sample, cache and print it
evaluation1 <- MUS.evaluation(extract1, audited1)

# Assume 500 invoices, each between 1 and 1000 monetary units
Evaluate a sample using Monetary Unit Sampling.

Evaluate a sample using Monetary Unit Sampling. At the end of the evaluation step, you get to know the audit conclusion for the population. To conduct the evaluation step it is required that you audited the sample and high values before. You can use print() for a comprehensive output.

### Usage

```
MUS.evaluation(extract, filled.sample, filled.high.values, 
col.name.audit.values, col.name.riskweights, 
interval.type, print.advice, tainting.order, experimental, combined)
```

### Arguments

- **extract**: A MUS.extraction.result object that you got by executing the function MUS.extraction.
- **filled.sample**: A data frame or matrix with the sample from the extraction routine that have an additional column with the audit values.
- **filled.high.values**: A data frame or matrix with the high value items from the extraction routine that have an additional column with the audit values.
- **col.name.audit.values**: Single character with the name of the column containing the audit value in filled.sample respectively filled.high.values. Default is "audit.value".
- **col.name.riskweights**: Single character with the name of the column containing the risk weights in filled.sample respectively filled.high.values. Default is NULL, then no risk weights are included in the calculations (the ordinary MUS case).
- **interval.type**: Interval type for high error rate evaluation. Default is "one-sided".
print.advice  Boolean. Prints recommendations only if TRUE. Default is “TRUE”.
tainting.order  Calculates UEL with different tainting orders (increasing, absolute, random). Default is "decreasing".
experimental  Boolean. Calculates other bounds, such as momentum, binomial, multinomial. Not ready for production. Default is "FALSE".
combined  Boolean. Marks the dataset as a combination of multiple strata. Default is "FALSE".

Value

An object MUS.evaluation.result is returned which is a list containing the following elements:

MUS.extraction.result elements
All elements that are contained in MUS.extraction.result object. For auditing acceptability and for further steps all inputs are also returned.

filled.sample  dito.
filled.high.values  dito.
col.name.audit.values  dito.
Overstatements.Result.Details
Detail table for overstatements found in the sample.
Understatements.Result.Details
Detail table for understatements found in the sample.
Results.Sample
Comprehensive results of sample evaluation.
Results.High.values
Comprehensive results of individually significant item evaluation.
Results.Total
Comprehensive results of both evaluations (sample and individual significant items).
acceptable
Boolean, if population is acceptable given results, confidence level and materiality.

Author(s)

Henning Prömpers <henning@proempers.net>

Examples

```r
## Simple Example
# Assume 500 invoices, each between 1 and 1000 monetary units
e.example.data.1 <- data.frame(book.value=round(runif(n=500, min=1, max=1000)))
# Plan a sample and cache it
plan.results.simple <- MUS.planning(data=example.data.1,
tolerable.error=100000, expected.error=20000)
# Extract a sample and cache it (no high values exist in this example)
extract.results.simple <- MUS.extraction(plan.results.simple)
# Copy book value into a new column audit values
```
MUS.extend

Extend a MUS sample.

Description

Extends a sample that requires further evidence. Works with MUS.extraction.result. Please treat as experimental.

Usage

MUS.extend(extract, new_plan=NULL, additional.n=NULL)

Arguments

extract An object of the type MUS.extraction.result to be extended.
new_plan Provide a new MUS plan. If null, you must provide the qty of items to extend the sample.
additional.n Ignored if new_plan is provided, otherwise sample will be extended by additional.n items
Value

Returns an extended MUS.extraction.result object.

Author(s)

Andre Guimaraes <alsguimaraes@gmail.com>

Examples

```r
## Simple Example
# Assume 500 invoices
mydata <- data.frame(book.value =
    round(c(runif(n=480, min=10,max=20000),
    runif(n=20, min=15000,max=50000)))

# Plan a sample and cache it
plan <- MUS.planning(data=mydata,
    tolerable.error=50000, expected.error=3000)

# Extract a sample and cache it
extract <- MUS.extraction(plan, obey.n.as.min=TRUE)

# Create a new plan
new_plan <- MUS.planning(data=mydata,
    tolerable.error=50000, expected.error=5000)

# extends the sample using the new plan
extended <- MUS.extend(extract, new_plan)

# extends the sample by 20 itens using the original plan
extended20 <- MUS.extend(extract, additional.n=20)
```

---

**MUS.extraction**

Extract a sample using Monetary Unit Sampling.

Description

Extract a sample using Monetary Unit Sampling. At the end of the extraction step, you get to know the items that you have to audit.

Usage

```r
MUS.extraction(plan, start.point, seed, obey.n.as.min, combined)
```
**Arguments**

- **plan**: A MUS.planning.result object that you got by executing the function MUS.planning.
- **start.point**: The extraction method uses fixed interval sampling. The monetary unit specified by start.point will be drawn in each interval. Default is NULL, in this case a random number is drawn.
- **seed**: A seed number which will be used to initialise the random number generator. Default is NULL which means that no new random number generator is initialised. This argument is mainly used for simulations or if you want to be able to regenerate the sample on another computer.
- **obey.n.as.min**: Boolean. If set to TRUE, the sample interval will be exactly recalculated and thus the sample size will be exactly the planned sample size. Default is FALSE which is what most commercial statistical software do. In this case the drawn sample size might be slightly smaller than specified.
- **combined**: Boolean. Marks the dataset as a combination of multiple strata. Default is "FALSE".

**Value**

An object MUS.extraction.result is returned which is a list containing the following elements:

- **MUS.planning.result elements**: All elements that are contained in MUS.planning.result object. For auditing acceptability and for further steps all inputs are also returned.
- **start.point**: dito.
- **seed**: dito.
- **obey.n.as.min**: dito.
- **high.values**: The part of the population that is classified as individually significant items. All of them have to be audited.
- **sample.population**: The part of the population that is not in the high-values-subpopulation.
- **sampling.interval**: The reassessed sampling interval that have to be used for evaluation.
- **sample**: The extracted sample. All elements have to be audited.

**Author(s)**

Henning Prömpers <henning@proempers.net>

**See Also**

MUS.planning for planning a sample and MUS.evaluation for evaluation of the extracted and audited sample.
Examples

```r
## Simple Example
# Assume 500 invoices, each between 1 and 1000 monetary units
example.data.1 <- data.frame(book.value=round(runif(n=500, min=1, max=1000)))
# Plan a sample and cache it
plan.results.simple <- MUS.planning(data=example.data.1, tolerable.error=100000, expected.error=20000)
# Extract a sample and cache it
extract.results.simple <- MUS.extraction(plan.results.simple)

## Advanced Example
example.data.2 <- data.frame(own.name.of.book.values=round(runif(n=500, min=1, max=1000)))
plan.results.advanced <- MUS.planning(data=example.data.2, col.name.book.values="own.name.of.book.values", confidence.level=.70, tolerable.error=100000, expected.error=20000, n.min=3)
extract.results.advanced <- MUS.extraction(plan.results.advanced, start.point=5, seed=0, obey.n.as.min=TRUE)
```

---

**MUS.factor**

*Calculate MUS Factor.*

**Description**


**Usage**

```
MUS.factor(confidence.level, pct.ratio)
```

**Arguments**

- `confidence.level` 
dito.
- `pct.ratio`  
Expected.error by tolerable.error.

**Value**

Returns the MUS factor.

**Author(s)**

Andre Guimaraes <alsguimaraes@gmail.com>
Examples

```r
MUS.factor(0.95, 0.5)
```

---

**Description**

Calculates the moment bound (Dworkin & Grimlund, 1984) for a Monetary Unit Sampling evaluation.

Please treat as experimental.

**Usage**

```r
MUS.moment.bounds(x, confidence.level, as.pct, include.high.values)
```

**Arguments**

- `x`: A `MUS.evaluation.result` object (or a tainting vector) used to calculate the moment bound.
- `confidence.level`: The required confidence level. Default is 95%.
- `as.pct`: Boolean. Express results as percentage. Default is False.
- `include.high.values`: Boolean. Whether the bound should include high values. Default is "TRUE".

**Value**

Upper Error Limit calculated using the moment bound.

**Author(s)**

Andre Guimaraes <alsguimaraes@gmail.com>

**See Also**

`MUS.evaluation` for evaluation of the audited sample.
Examples

```r
sample = c(rep(0, 96), -.16, .04, .18, .47)
MUS.moment.bound(sample)

# Assume 500 invoices, each between 1 and 1000 monetary units
data <- data.frame(book.value=round(runif(n=500, min=1, max=1000)))
# Plan a sample and cache it
plan <- MUS.planning(data=data, tolerable.error=10000, expected.error=2000)
# Extract a sample and cache it (no high values exist in this example)
extract <- MUS.extraction(plan)
# Copy book value into a new column audit values, and inject some error
audited <- extract$sample$book.value*(1-rbinom(nrow(extract$sample), 1, 0.05))
audited <- cbind(extract$sample, audit.value=audited)
# Evaluate the sample, cache and print it
evaluation <- MUS.evaluation(extract, audited)
MUS.moment.bound(evaluation)
```

MUS.multinomial.bound Calculate a multinomial bound for a Monetary Unit Sampling evaluation.

Description

Calculates a multinomial bound for a Monetary Unit Sampling evaluation.
Please treat as experimental.

Usage

```
MUS.multinomial.bound(x, as.pct, include.high.values)
```

Arguments

- **x** A MUS.evaluation.result object used to calculate the multinomial bound.
- **as.pct** Boolean. Express results as percentage. Default is False.
- **include.high.values** Boolean. Whether the bound should include high values. Default is "TRUE".

Value

Upper Error Limit calculated using the multinomial bound.

Author(s)

Andre Guimaraes <alsguimaraes@gmail.com>
**MUS.planning**

Plan a sample using Monetary Unit Sampling.

**Description**

Plan a sample for Monetary Unit Sampling. At the end of this planning step, you get to know the sample size.

Be aware that this MUS routines cannot calculate with decimals. Furthermore, you must provide book values etc. as Euro-Cent so that no decimals occur.

**Usage**

```r
MUS.planning(data, col.name.book.values, confidence.level, tolerable.error, expected.error, n.min, errors.as.pct, conservative, combined)
```

**Arguments**

- `data`: A data frame or matrix which contains at least one column with the book values.
- `col.name.book.values`: The name of the column that contains the book values. Default is "book.value".
- `confidence.level`: The required confidence level. Default is 95%.
- `tolerable.error`: The tolerable error (materiality) in Monetary Units.
- `expected.error`: The expected error which is contained in the population in Monetary Units.
- `n.min`: Minimum sample size that should be used. Default is 0.

**Examples**

```r
# Assume 500 invoices, each between 1 and 1000 monetary units
data <- data.frame(book.value=round(runif(n=500, min=1, max=1000)))
# Plan a sample and cache it
plan <- MUS.planning(data=data, tolerable.error=10000, expected.error=2000)
# Extract a sample and cache it (no high values exist in this example)
extact <- MUS.extraction(plan)
# Copy book value into a new column audit values, and inject some error
audited <- extract$sample$book.value*(1-rbinom(nrow(extract$sample), 1, 0.05))
audited <- cbind(extract$sample, audit.value=audited)
# Evaluate the sample, cache and print it
evaluation <- MUS.evaluation(extract, audited)
MUS.multinomial.bound(evaluation)
```
errors.as.pct  Boolean. Tolerable and Expected error informed as percentages. Default is False.

conservative  Boolean. If true, use greater sample size between normal calculation and conservative algorithm (i.e., gamma-based, AICPA compatible).

combined  Boolean. Marks the dataset as a combination of multiple strata. Default is "FALSE".

Value

An object MUS.planning.result is returned which is a list containing the following elements:

data  For auditing acceptability and for further steps all inputs are also returned.
col.name.book.values  ditto.
confidence.level  ditto.
tolerable.error  ditto.
expected.error  ditto.
book.value  The calculated gross book value of the population. Negative values are ignored.
n  The calculated sample size based on the input parameters which is greater or egal than the provided minimum sample size.

High.value.threshold  Whenever a book value of an element is above the threshold, the element will be considered individually significant. Individual significant items will be audited completely, no sample extrapolation will be necessary.
tolerable.taintings  The number of taintings in the sample that will be acceptable at maximum.

Author(s)

Henning Prömpers <henning@proempers.net>

See Also

MUS.extraction for extraction of the planned sample and MUS.evaluation for evaluation of the extracted and audited sample.

Examples

```r
# Simple Example
example.data.1 <- data.frame(book.value=round(runif(n=500, min=1, max=1000)))

# Plan a sample and cache it
plan.results.simple <- MUS.planning(data=example.data.1, tolerable.error=100000, expected.error=20000)
```
## Advanced Example

```r
example.data.2 <- data.frame(own.name.of.book.values=round(runif(n=500, 
min=1, max=1000)))
plan.results.advanced <- MUS.planning(data=example.data.2, 
col.name.book.values="own.name.of.book.values", confidence.level=.70, 
tolerable.error=100000, expected.error=20000, n.min=3)
```

## Pretty and comprehensive printing of MUS evaluation results

### Description

Pretty and comprehensive printing of MUS evaluation results that can be used for working papers.

### Usage

```r
## S3 method for class 'MUS.evaluation.result'
print(x, error.rate, print.misstatements, 
print.planning, print.extraction, print.error.as.pct, print.advice, 
style, use.pander, ...)
```

### Arguments

- `x`: A MUS.evaluation.result object that you got by executing the function MUS.evaluation.
- `error.rate`: Selects type of error rate calculation (i.e., "high", "low", "both" or "auto"). Defaults to "auto".
- `print.misstatements`: Boolean. Should misstatements table be printed? Defaults to TRUE.
- `print.planning`: Boolean. Should planning parameters be printed? Defaults to FALSE.
- `print.extraction`: Boolean. Should extraction parameters be printed? Defaults to FALSE.
- `print.error.as.pct`: Boolean. Should errors as percentage be printed? Defaults to TRUE.
- `print.advice`: Boolean. Should recommendations be printed? Defaults to TRUE.
- `style`: Two options: "report" or "default". Report uses an alternative layout. Defaults to "default".
- `use.pander`: Boolean. Uses pander to generate rmarkdown report. Defaults to FALSE.
- `...`: Further arguments, currently ignored.

### Author(s)

Henning Prömpers <henning@proempers.net>

### See Also

- `MUS.evaluation` for evaluation of the extracted and audited sample.
print.MUS.extraction.result

Pretty and comprehensive printing of MUS extraction results

Description

Pretty and comprehensive printing of MUS extraction results that can be used for working papers.

Usage

```r
## S3 method for class 'MUS.extraction.result'
print(x, print.title, print.planning, style, use.pander, ...)
```

Arguments

- `x` A MUS.evaluation.result object that you got by executing the function MUS.evaluation.
- `print.title` Boolean. Should title be printed? Defaults to TRUE.
- `print.planning` Boolean. Should planning parameters be printed? Defaults to FALSE.
- `style` Two options: "report" or "default". Report uses an alternative layout. Defaults to "default".
- `use.pander` Boolean. Uses pander to generate rmarkdown report. Defaults to FALSE.
- `...` Further arguments, currently ignored.

Author(s)

Henning Prömpers <henning@proempers.net>

See Also

- `MUS.extraction` for extraction of the audit sample.

print.MUS.planning.result

Pretty and comprehensive printing of MUS planning results

Description

Pretty and comprehensive printing of MUS planning results that can be used for working papers.

Usage

```r
## S3 method for class 'MUS.planning.result'
print(x, print.title, style, use.pander, ...)
```
print.MUS.planning.result

Arguments

- **x**: A MUS.evaluation.result object that you got by executing the function MUS.evaluation.
- **print.title**: Boolean. Should title be printed? Defaults to TRUE.
- **style**: Two options: "report" or "default". Report uses an alternative layout. Defaults to "default".
- **use.pander**: Boolean. Uses pander to generate markdown report. Defaults to FALSE.
- **...**: Further arguments, currently ignored.

Author(s)

Henning Prömpers <henning@proempers.net>

See Also

MUS.planning for planning of the audit sample.
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