Package ‘Rtropical’

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all_trees  Simulated Tree Data with Different Proximity Parameter Value

Description

Simulated Tree Data with Different Proximity Parameter Value

Usage

data(all_trees)

Format

A list of length 12 with each element a sublist containing an ape multiPhylo object with 300 rooted trees on 5 tips and the tree categories.
apicomplexa

Apicomplexa gene trees sample data set.

Usage

apicomplexa

Format

An ape multiPhylo object with 268 rooted trees on 8 tips.

Source


as.matrix.multiPhylo  Vectorize a Set of Phylogenetic Trees

Description

Unifies tip labels of all phylogenetic trees in multiPhylo object the same as the first tree and returns the cophenetic distance of their corresponding chronogram.

Usage

```r
## S3 method for class 'multiPhylo'
as.matrix(x, tipOrder = x[[1]]$tip.label, parallel = FALSE, ncores = 2, ...)
```

Arguments

- `x` an object of class multiPhylo
- `tipOrder` a numeric vector of order of leaf names to which all trees in the multiPhylo object will unified. If not specified on purpose, the tip order of the first tree will be used.
- `parallel` a logical value indicating if parallel computing should be used. (default: FALSE)
- `ncores` a numeric value indicating the number of threads utilized for multi-cored CPUs. (default: 2)
- `...` Not used. Other arguments to as.vector
Value

A data matrix with each row a vector representation of a chronogram. Each element of the vector is the distance between two leaves.

Examples

data(apicomplexa)
data <- as.matrix(apicomplexa[1:10]) # matrixize first ten trees

---

as.vector.phylo  Vectorize a Phylogenetic Tree

Description

Computes the cophenetic distance and outputs them in a vector of a phylogenetic tree in phylo object

Usage

## S3 method for class 'phylo'
as.vector(x, mode = "any")

Arguments

x  A object of class phylo
mode  The same as base::as.vector. But only numeric output in vector form is accepted for other functions in Rtropical

Value

A vector with its elements the distance between two leaves of the tree.

Examples

library(ape)
tree <- rcoal(5)
tree_vec <- as.vector(tree)
coef.cv.tropsvm

Extract Optimal Tropical Hyperplane from a cv.tropsvm object

Description

Obtain the optimal tropical hyperplane in the form of vectors from a cv.tropsvm object.

Usage

## S3 method for class 'cv.tropsvm'
coef(object, ...)

Arguments

object a fitted "cv.tropsvm" object.
...
Not used. Other arguments.

Value

An output of the apex of the fitted optimal tropical hyperplane.

coef.tropsvm

Extract Optimal Tropical Hyperplane from a tropsvm object

Description

Obtain the optimal tropical hyperplane in the form of vectors from a tropsvm object.

Usage

## S3 method for class 'tropsvm'
coef(object, ...)

Arguments

object a fitted "tropsvm" object.
...
Not used. Other arguments.

Value

An output of the apex of the fitted optimal tropical hyperplane.
Cross-Validation for Tropical Support Vector Machines

Description
Conduct k-fold cross validation for tropsvm and return an object "cv.tropsvm".

Usage
cv.tropsvm(x, y, parallel = FALSE, nfold = 10, nassignment = 10, ncores = 2)

Arguments
- **x**: a data matrix, of dimension nobs x nvars; each row is an observation vector.
- **y**: a response vector with one label for each row/component of x.
- **parallel**: a logical value indicating if parallel computing should be used. (default: FALSE)
- **nfold**: a numeric value of the number of data folds for cross-validation. (default: 10)
- **nassignment**: a numeric value indicating the size of the parameter grid of assignments. (default: 10)
- **ncores**: a numeric value indicating the number of threads utilized for multi-core CPUs. (default: 2)

Value
object with S3 class cv.tropsvm containing the fitted model, including:
- **apex**: The negative apex of the fitted optimal tropical hyperplane.
- **assignment**: The best assignment tuned by cross-validation.
- **index**: The best classification method tuned by cross-validation.
- **levels**: The name of each category, consistent with categories in y.
- **accuracy**: The validation accuracy for each fold.
- **nfold**: The number of folds used in cross-validation.

See Also
summary, predict, coef and the tropsvm function.

Examples

```r
# data generation
library(Rfast)
set.seed(101)
e <- 20
n <- 10
```
lungfish

Coelacanths genome and transcriptome data

Description
Coelacanths genome and transcriptome data

Usage
lungfish

Format
An ape multiPhylo object with 1193 rooted trees on 10 tips.

Source
plot.troppca  
*Plot the Tropical Principal Components with Data Projections*

**Description**

Visualize the second order tropical principle components in troppca as a tropical triangle with projections on a two-dimensional plot via tropical isometry.

**Usage**

```r
## S3 method for class 'troppca'
plot(x, plab = NULL, fw = FALSE, ...)
```

**Arguments**

- `x`: a fitted `troppca` object.
- `plab`: a vector of labels of all points in the given data matrix. Not needed for unlabeled data. (default: NULL)
- `fw`: a logical variable to determine if to add Fermat-Weber point of the data projection. (default: FALSE)
- `...`: Not used. Other arguments to plot

**Value**

`plot.troppca` does not return anything other than the plot.

predict.cv.tropsvm  
*Predict Method for Tropical Support Vector Machines based on Cross-Validation*

**Description**

Predicts values based upon a model trained by `cv.tropsvm`.

**Usage**

```r
## S3 method for class 'cv.tropsvm'
predict(object, newx, ...)
```

**Arguments**

- `object`: a fitted "cv.tropsvm" object.
- `newx`: a data matrix, of dimension nobs x nvars used as testing data.
- `...`: Not used. Other arguments to predict.
Value

A vector of predicted values of a vector of labels.

See Also

summary, coef and the cv.tropsvm function.

Examples

```r
# data generation
library(Rfast)
e <- 20
n <- 10
N <- 10
s <- 5
x <- rbind(
  rmvnorm(n, mu = c(5, -5, rep(0, e - 2)), sigma = diag(s, e)),
  rmvnorm(n, mu = c(-5, 5, rep(0, e - 2)), sigma = diag(s, e))
)
y <- as.factor(c(rep(1, n), rep(2, n)))
newx <- rbind(
  rmvnorm(N, mu = c(5, -5, rep(0, e - 2)), sigma = diag(s, e)),
  rmvnorm(N, mu = c(-5, 5, rep(0, e - 2)), sigma = diag(s, e))
)
newy <- as.factor(rep(c(1, 2), each = N))

# train the tropical svm
cv_tropsvm_fit <- cv.tropsvm(x, y, parallel = FALSE)

# test with new data
pred <- predict(cv_tropsvm_fit, newx)

# check with accuracy
table(pred, newy)

# compute testing accuracy
sum(pred == newy) / length(newy)
```

---

**predict.tropsvm**

**Predict Method for Tropical Support Vector Machines**

**Description**

Predicts values based upon a model trained by tropsvm.

**Usage**

```r
## S3 method for class 'tropsvm'
predict(object, newx, ...)```

Arguments

object a fitted tropsvm object.
newx a data matrix, of dimension nob x nvars used as testing data.
... Not used. Other arguments to predict.

Value

A vector of predicted values of a vector of labels.

See Also

summary, coef and the tropsvm function.

Examples

# data generation
library(Rfast)
e <- 100
n <- 10
N <- 10
s <- 5
x <- rbind(
    rmvnorm(n, mu = c(5, -5, rep(0, e - 2)), sigma = diag(s, e)),
    rmvnorm(n, mu = c(-5, 5, rep(0, e - 2)), sigma = diag(s, e))
)
y <- as.factor(c(rep(1, n), rep(2, n)))
newx <- rbind(
    rmvnorm(N, mu = c(5, -5, rep(0, e - 2)), sigma = diag(s, e)),
    rmvnorm(N, mu = c(-5, 5, rep(0, e - 2)), sigma = diag(s, e))
)
newy <- as.factor(rep(c(1, 2), each = N))

# train the tropical svm
 tropsvm_fit <- tropsvm(x, y, auto.assignment = TRUE, ind = 1)

# test with new data
pred <- predict(tropsvm_fit, newx)

# check with accuracy
table(pred, newy)

# compute testing accuracy
sum(pred == newy) / length(newy)
**read.nexus.to.data.matrix**

*Read NEXUS-formatted trees from two categories into a data matrix*

**Description**

Read NEXUS-formatted trees from two categories into a data matrix

**Usage**

read.nexus.to.data.matrix(data.file1, data.file2)

**Arguments**

- **data.file1**: A data set with trees from one category.
- **data.file2**: A data set with trees from the other category.

**Value**

A data matrix with the first x rows corresponding the x trees in the first file and the last y rows are the trees from the second file.

---

**read.tree.to.data.matrix**

*Read Newick-formatted trees in two categories into a data matrix*

**Description**

Read Newick-formatted trees in two categories into a data matrix

**Usage**

read.tree.to.data.matrix(data.file1, data.file2)

**Arguments**

- **data.file1**: A file containing trees in Newick form in a category.
- **data.file2**: A file containing trees in Newick form in an assumed different category.

**Value**

read.tree.to.data.matrix has the same return as read.nexus.to.data.matrix.
sim_trees        Simulated Tree Data

**Description**

Simulated Tree Data

**Usage**

```r
data(sim_trees)
```

**Format**

An ape multiPhylo object with 300 rooted trees on 5 tips.

---

summary.cv.tropsvm    Summarize an Analysis of Cross-Validated Tropical Support Vector Machine

**Description**

Return a summary with a more detailed explanation of the object "cv.tropsvm".

**Usage**

```r
## S3 method for class 'cv.tropsvm'
summary(object, ...)
```

**Arguments**

- `object` a fitted "cv.tropsvm" object.
- `...` Not used. Other arguments to summary.

**Value**

A summary of the crucial information of a tropical support vector machine is printed, including the selected best assignment and classification methods and the validation accuracy of each data fold. The summary section of classification methods specifies the sectors and their intersections used to classify points of two different categories.

**See Also**

`predict`, `coef` and the `cv.tropsvm` function.
Examples

```r
# data generation
library(Rfast)
e <- 20
n <- 10
N <- 10
s <- 5
x <- rbind(
  rmvnorm(n, mu = c(5, -5, rep(0, e - 2)), sigma = diag(s, e)),
  rmvnorm(n, mu = c(-5, 5, rep(0, e - 2)), sigma = diag(s, e))
)
y <- as.factor(c(rep(1, n), rep(2, n)))
newx <- rbind(
  rmvnorm(N, mu = c(5, -5, rep(0, e - 2)), sigma = diag(s, e)),
  rmvnorm(N, mu = c(-5, 5, rep(0, e - 2)), sigma = diag(s, e))
)
newy <- as.factor(rep(c(1, 2), each = N))

# train the tropical svm with cross-validation
cv_tropsvm_fit <- cv.tropsvm(x, y, parallel = FALSE)
summary(cv_tropsvm_fit)
```

tropdet  
**Tropical Determinant of a Matrix**

Description

Compute the tropical determinant for a given matrix. This is equivalent to solving an assignment problem.

Usage

```r
tropdet(x)
```

Arguments

- `x`: a square matrix

Value

The determinant of the given matrix,

Examples

```r
R <- matrix(sample(1:9, 9), nrow = 3)
tropdet(R)
```
tropFW  

Tropical Fermat-Weber Point

Description

Compute the tropical Fermat-Weber (FW) point for a given data matrix. The FW point minimizes the summed tropical distance to the trees described in the data matrix.

Usage

tropFW(x)

Arguments

x  a data matrix, of dimension nobs x nvars; each row is an observation vector.

Value

A list containing:

fw  The fermat-weber point.
distsum  The sum of distance from each observation to the fermat-weber point.

Examples

x <- matrix(rnorm(100), ncol = 10)
tropFW(x)

---

troppca.linsp  Tropical Principal Component Analysis by Tropical Linear Space

Description

Approximate the principal component as a tropical linear space for a given data matrix and returns the results as an object of class troppca.

Usage

troppca.linsp(x, pcs = 2, iteration = list(), ncores = 2)
Arguments

- **x**: a data matrix, of size n x e, with each row an observation vector. e is the dimension of the tropical space
- **pcs**: a numeric value indicating the order of principal component. (default: 2)
- **iteration**: a list with arguments controlling the iteration of the algorithm.
  - **exhaust**: a logical variable indicating if to iterate over all possible combinations of the linear space based on the given data matrix x. If FALSE, please input a number of iteration for niter. If TRUE, please enter 0 for niter and this function will iterate over all possible combinations of linear space. This could be time consuming when x is large. (default: FALSE)
  - **niter**: a numeric variable indicating the number of iterations. (default: 100)
  - **ncores**: a numeric value indicating the number of threads utilized for multi-cored CPUs. (default: 2)

Value

A list of S3 class "troppca", including:

- **pc**: The principal component as a tropical linear space
- **obj**: The tropical PCA objective, the sum of tropical distance from each point to the projection.
- **projection**: The projections of all data points.
- **type**: The geometry of principal component.

Examples

```r
library(Rfast)
n <- 100
e <- 10
sig2 <- 1
x <- rbind(rmvnorm(n, mu = c(5, -5, rep(0, e - 2)), sigma = diag(sig2, e)))
troppca_fit <- troppca.linsp(x)
```

Description

Approximate the principal component as a tropical polytope converted from tropical linear space for a given data matrix via MCMC and return the results as an object of class `troppca`.
Usage

troppca.linsp2poly(x, pcs = 2, nsample = 1000, ncores = 2)

Arguments

- **x**: a data matrix, of size n x e, with each row an observation vector. e is the dimension of the tropical space.
- **pcs**: a numeric value indicating the order of principal component. (default: 2)
- **nsample**: a numeric value indicating the number of samples of MCMC. (default: 1000)
- **ncores**: a numeric value indicating the number of threads utilized for multi-core CPUs. (default: 2)

Value

A list of S3 class "troppca", including:

- **pc**: The principal component as a tropical linear space
- **obj**: The tropical PCA objective, the sum of tropical distance from each point to the projection.
- **projection**: The projections of all data points.
- **type**: The geometry of principal component.

Examples

```r
library(Rfast)
n <- 50
e <- 50
s <- 5
x <- rbind(
  rmvnorm(n, mu = c(5, -5, rep(0, e - 2)), sigma = diag(s, e)),
  rmvnorm(n, mu = c(-5, 5, rep(0, e - 2)), sigma = diag(s, e))
)
troppca_fit <- troppca.linsp2poly(x)
```

Troppca.poly

**Tropical Principal Component Analysis by Tropical Polytope**

Description

Approximates the principal component as a tropical polytope for a given data matrix via MCMC and return the results as an object of class troppca.
Usage

troppca.poly(x, pcs = 2, nsample = 1000, ncores = 2)

Arguments

x     a data matrix, of size n x e, with each row an observation vector. e is the dimension of the tropical space.

pcs   a numeric value indicating the order of principal component. (default: 2)

nsample a numeric value indicating the number of samples of MCMC. (default: 1000)

ncores a numeric value indicating the number of threads utilized for multi-cored CPUs. (default: 2)

Value

A list of S3 class "troppca", including:

pc     The principal component as a tropical linear space

obj    The tropical PCA objective, the sum of tropical distance from each point to the projection.

projection The projections of all data points.

type   The geometry of principal component.

Examples

library(Rfast)
n <- 50
e <- 50
s <- 5
x <- rbind(
    rmvnorm(n, mu = c(5, -5, rep(0, e - 2)), sigma = diag(s, e)),
    rmvnorm(n, mu = c(-5, 5, rep(0, e - 2)), sigma = diag(s, e))
)
troppca.fit <- troppca.poly(x)
plot(troppca_fit)


Description

Compute projection of data points on a given tropical linear space.
Usage

tropproj.linsp(x, V)

Arguments

<table>
<thead>
<tr>
<th></th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>x</td>
<td>a data matrix, of size n x e, with each row an observation.</td>
</tr>
<tr>
<td>V</td>
<td>a data matrix, of dimension s x e, with each row a basis of tropical linear space.</td>
</tr>
</tbody>
</table>

Value

A matrix of projections of all data points.

Examples

```r
library(Rfast)
n <- 100
e <- 10
sig2 <- 1
s <- 3
x <- rbind(rmvnorm(n, mu = c(5, -5, rep(0, e - 2)), sigma = diag(sig2, e)))
V <- matrix(runif(s * e, -10, 10), nrow = s, ncol = e)
x_proj <- tropproj.linsp(x, V)
head(x_proj)
```

---

### tropproj.poly

**Projection on Tropical Polytope**

Description

Project a point onto a given tropical polytope.

Usage

tropproj.poly(x, tconv)

Arguments

<table>
<thead>
<tr>
<th></th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>x</td>
<td>a data vector, of length e.</td>
</tr>
<tr>
<td>tconv</td>
<td>a data matrix, of size e x s, with each column a vertex of the tropical polytope.</td>
</tr>
</tbody>
</table>

Value

A projected vector on the given tropical polytope.
Examples

```r
# Generate a tropical polytope consisting of three trees each with 5 leaves
library(ape)
pltp <- sapply(1:3, function(i) { as.vector(rcoal(5)) })
# Generate an observation and vectorize it
tree <- rcoal(5)
tree_vec <- as.vector(tree)
tropproj.poly(tree_vec, pltp)
```

tropsvm  

**Tropical Support Vector Machines**

**Description**

Fit a discriminative two-class classifier via linear programming defined by the tropical hyperplane which maximizes the minimum tropical distance from data points to itself in order to separate the data points into sectors (half-spaces) in the tropical projective torus.

**Usage**

tropsvm(x, y, auto.assignment = FALSE, assignment = NULL, ind = 1)

**Arguments**

- **x**
  a data matrix, of dimension nob x nvars; each row is an observation vector.

- **y**
  a response vector with one label for each row/component of x.

- **auto.assignment**
  a logical value indicating if to provide an assignment manually. If FALSE, an input is required, otherwise the function automatically finds a good assignment. (default: FALSE)

- **assignment**
  a numeric vector of length 4 indicating the sectors of tropical hyperplane that the data will be assigned to. The first and third elements in the assignment are the coordinates of an observed point in data matrix x believed from the first category where the maximum and second maximum of the vector addition between the fitted optimal tropical hyperplane and the point itself are achieved. The meanings for the second and the fourth element in the assignment are the same but for the points in the second category. Namely, the first and second values in the assignment are the indices of sectors where the two point clouds are assigned. Not needed when auto.assignment = TRUE. (default: NULL)

- **ind**
  a numeric value or a numeric vector ranging from 1 to 70 indicating which classification method to be used. There are 70 different classification methods. Details of a given method can be retrieved by summary. The different classification methods are proposed to resolve the issue when points fall on the intersections of sectors. Users can have personal choices if better knowledge is assumed. (default: 1)
Value

An object with S3 class `tropsvm` containing the fitted model, including:

- **apex**: The negative apex of the fitted optimal tropical hyperplane.
- **assignment**: The user-input or auto-found assignment.
- **index**: The user-input classification method.
- **levels**: The name of each category, consistent with categories in `y`.

See Also

`predict`, `coef` and the `cv.tropsvm` function.

Examples

```r
# data generation
library(Rfast)
e <- 100
n <- 10
N <- 100
s <- 10
x <- rbind(
  rmvnorm(n, mu = c(5, -5, rep(0, e - 2)), sigma = diag(s, e)),
  rmvnorm(n, mu = c(-5, 5, rep(0, e - 2)), sigma = diag(s, e))
)
y <- as.factor(c(rep(1, n), rep(2, n)))
newx <- rbind(
  rmvnorm(N, mu = c(5, -5, rep(0, e - 2)), sigma = diag(s, e)),
  rmvnorm(N, mu = c(-5, 5, rep(0, e - 2)), sigma = diag(s, e))
)
newy <- as.factor(rep(c(1, 2), each = N))

# train the tropical svm
tropsvm_fit <- tropsvm(x, y, auto.assignment = TRUE, ind = 1)
coef(tropsvm_fit)

# test with new data
pred <- predict(tropsvm_fit, newx)

# check with accuracy
table(pred, newy)

# compute testing accuracy
sum(pred == newy) / length(newy)
```
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