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| basket-package | <i>Basket Trial Analysis</i> |
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Description

The R basket package provides for the designs and analysis of basket trials for multi-source exchangeability models (MEM) <<https://doi.org/10.1093/biostatistics/kxx031>> allowing arms to "share" power with similar arms in a trial. The package is intended to perform the exact or MCMC computation of the operating characteristics of different scenarios. Calculations derived from these analyses include the posterior probabilities, HPD boundaries, effective sample sizes (ESS), mean and median estimations can be calculated with this package using the MEM method. Along with providing

"basketwise" analyses, the package includes similar calculations for "clusterwise" analyses where a cluster a set of similar baskets. In addition plotting tools are provided to visualize basket and cluster density as well as their exchangeability. The package includes the following main functions:

- `[basket_name()]` Get the basket names in an analysis
- `[basket_pep()]` Get the Posterior Exchangeability Probability (PEP) matrix for the arms in the trial.
- `[basket_map()]` Get the Maximum A Posteriori (MAP) matrix for the arms in a trial.
- `[cluster_pep()]` Get the Posterior Exchangeability Probability (PEP) matrix for the arms in the trial.
- `[cluster_map()]` Get the Maximum A Posteriori (MAP) matrix for the arms in a trial.
- `[sample_posterior()]` Sample from the posterior distribution of the arms in the trial.
- `[mem_exact()]` Create a basket analysis using the exact method.
- `[mem_mcmc()]` Create a basket analysis using the exact method.
- `[summary()]` Summarize the results of an analysis.
- `[update_p0()]` Update the null that a basket response rate is above a specified value.
- `[plot_density()]` Plot the estimated densities of arms or clusters.
- `[plot_pep()]` Show the exchangeogram of the PEP matrix.
- `[plot_mem()]` Plot the arm prior, MAP, and PEP of a basket trial.

References

Vemurafenib in multiple nonmelanoma cancers with braf v600 mutations Hyman DM, Puzanov I, Subbiah V, Faris JE, Chau I, Blay JY, Wolf J, Raje NS, Diamond EL, Hollebecque A, et al. *New England Journal of Medicine* 2015; 373(8):726–736. <<https://doi:10.1056/NEJMoa1502309>>

Bayesian basket trial design with exchangeability monitoring BP Hobbs, R Landin *Statistics in medicine* 37 (25), 3557-357. <<https://doi.org/10.1002/sim.7893>>

Statistical challenges posed by uncontrolled master protocols: sensitivity analysis of the vemurafenib study BP Hobbs, MJ Kane, DS Hong, R Landin *Annals of Oncology* 29 (12), 2296-2301. <doi:10.1093/annonc/mdy457>

Bayesian hierarchical modeling based on multisource exchangeability AM Kaizer, JS Koopmeiners, BP Hobbs *Biostatistics* 19 (2), 169-184. <<https://doi.org/10.1093/biostatistics/kxx031>>

basket

Create a Basket Trial Analysis

Description

This function creates an analysis modeling the exchangeability and distribution characteristics of cohorts in a basket trial, where a single therapy is given to multiple cohorts. The model is based on the multi-source exchangeability model. This is a generalization of the Bayesian hierarchical model and it accomodates multiple sets of latent factors shared combinations of cohorts.

Usage

```

basket(
  responses,
  size,
  name,
  p0 = 0.15,
  shape1 = 0.5,
  shape2 = 0.5,
  prior = diag(length(responses))/2 + matrix(0.5, nrow = length(responses), ncol =
    length(responses)),
  hpd_alpha = 0.05,
  alternative = "greater",
  call = NULL,
  cluster_function = cluster_membership,
  method = c("mcmc", "lmem", "exact"),
  mcmc_iter = 2e+05,
  mcmc_burnin = 50000,
  initial_mem = round(prior - 0.001),
  cluster_analysis = FALSE,
  seed = get_seed()
)

```

Arguments

| | |
|------------------|---|
| responses | the number of responses in each basket. |
| size | the size of each basket. |
| name | the name of each basket. |
| p0 | the null response rate for the poster probability calculation. (default 0.15) |
| shape1 | the first shape parameter(s) for the prior of each basket. (default 0.5) |
| shape2 | the second shape parameter(s) for the prior of each basket. (default 0.5) |
| prior | the matrix giving the prior inclusion probability for each pair of baskets. The default is on on the main diagonal and 0.5 elsewhere. |
| hpd_alpha | the highest posterior density trial significance. (default 0.05) |
| alternative | the alternative case definition (default "greater"). |
| call | the call of the function. (default NULL) |
| cluster_function | a function to cluster baskets. |
| method | "mcmc", "lmem" (local MEM), or "exact". See details for an explanation. (default "mcmc") |
| mcmc_iter | if the method is "mcmc" then this specifies the number of mcmc iterations. Otherwise, it is ignored. (default 200000) |
| mcmc_burnin | if the method is "mcmc" then this specifies the number of burn-in iterations. (default 50000) |
| initial_mem | if the method is "mcmc" then this specifies the initial MEM matrix. Otherwise, it is ignored. |

cluster_analysis if the cluster analysis is conducted.

seed the random seed for the mcmc calculations. By default this is .Random.seed. If this value is not initialized, then it is first initialized with Sys.time() and then returned.

Details

The model may be fit using an exact calculation via mcmc, or a local version of MEM. The first conducts posterior inference through the entire set of exchangeability relationships in the sample domain. This approach is computationally feasible only when the number of cohorts is relatively small. As a rule of thumb this option should be used with a maximum of 20 cohorts. By default, the second(mcmc) is used and it is based on the Metropolis algorithm and it extends the model's implementation to larger collections of subpopulations. The algorithm initiates with a burn-in period (see mcmc_burnin), which are discarded from the analysis. The third is based on a recent paper by Wei et al. The calculation is computationally efficient and tends to borrow to a lesser extent than other implemented methods.

Examples

```
# 3 baskets, each with enrollement size 5
trial_sizes <- rep(5, 3)

# The response rates for the baskets.
resp_rate <- 0.15

# The trials: a column of the number of responses and a column of the
# the size of each trial.
trials <- data.frame(
  responses = rbinom(trial_sizes, trial_sizes, resp_rate),
  size = trial_sizes,
  name = letters[1:3]
)

summary(basket(trials$responses, trials$size, trials$name))
```

basket_map

Get the Basketwise Maximum A Posteriori Probability Matrix

Description

MEM analyses include the maximum a posteriori exchangeability probability (MAP) of included arms indicating whether two arms in the trial are exchangeable. This function returns the matrix of those relationships.

Usage

```
basket_map(x)
```

Arguments

x either an exchangeability model or basket object.

Examples

```
# Create an MEM analysis of the Vemurafenib trial data.
data(vemu_wide)

mem_analysis <- mem_exact(
  vemu_wide$responders,
  vemu_wide$evaluable,
  vemu_wide$baskets
)

# Get basket MAPs.
basket_map(mem_analysis)
```

basket_name

The Names of the Baskets

Description

Retrieve the basket names in an exchangeability model.

Usage

```
basket_name(model)
```

Arguments

model the model to retrieve the basket names of

Examples

```
# 3 baskets, each with enrollement size 5
trial_sizes <- rep(5, 3)

# The response rates for the baskets.
resp_rate <- 0.15

# The trials: a column of the number of responses and a column of the
# the size of each trial.
trials <- data.frame(
  responses = rbinom(trial_sizes, trial_sizes, resp_rate),
  size = trial_sizes,
  name = paste("Basket", seq_len(3))
```

```
)  
basket_name(mem_mcmc(trials$responses, trials$size, trials$basket))
```

basket_peg

The Basketwise Posterior Exchangeability Probability Matrix

Description

MEM analyses include the posterior exchangeability probability (PEP) of included arms giving the probability that any two arms are exchangeable. This function returns the matrix of those probabilities.

Usage

```
basket_peg(x)
```

Arguments

x either an exchangeability model or basket object.

Examples

```
# Create an MEM analysis of the Vemurafenib trial data.  
data(vemu_wide)  
  
mem_analysis <- mem_exact(  
  vemu_wide$responders,  
  vemu_wide$evaluatable,  
  vemu_wide$baskets  
)  
  
# Get the PEP for baskets.  
basket_peg(mem_analysis)
```

cluster_baskets

Get the Cluster Members of MEM Models

Description

Object returned by the ‘mem_mcmc()’ and ‘mem_exact()’ include information about the arms in the trials and the cluster composed of sets of similar arms. This function returns the name of each arm in a cluster.

Usage

```
cluster_baskets(x)
```

Arguments

x either an exchangeability model or basket object.

Value

A named list is returned where the name is the cluster name and each element of the list is comprised of a character vector of the baskets in each cluster.

Examples

```
# Create an MEM analysis of the Vemurafenib trial data.
data(vemu_wide)

mem_analysis <- mem_exact(
  vemu_wide$responders,
  vemu_wide$evaluatable,
  vemu_wide$baskets,
  cluster_analysis = TRUE
)

# Get the baskets in the clusters.
cluster_baskets(mem_analysis)
```

cluster_map

Get the Clusterwise Maximum A Posteriori Probability Matrix

Description

MEM analyses include the maximum a posteriori exchangeability probability (MAP) of included arms indicating whether two arms in the trial are exchangeable. This function returns the matrix of those relationships.

Usage

```
cluster_map(x)
```

Arguments

x either an exchangeability model or basket object.

Examples

```
# Create an MEM analysis of the Vemurafenib trial data.
data(vemu_wide)

mem_analysis <- mem_exact(
  vemu_wide$responders,
  vemu_wide$evaluable,
  vemu_wide$baskets
)

# Get the cluster MAPs.
cluster_map(mem_analysis)
```

cluster_membership *Cluster Baskets Based on the Posterior Exchangeabilities*

Description

This is the default function used to cluster cohorts in the basket, `mem_mcmc`, and `mem_exact` functions. The approach creates a graph where each vertex is a cohort and the weight between two cohorts is determined by their posterior exchangeability probability. The graph is then clustered using **igraph**'s louvain function, which determines the number of clusters and the cluster memberships, and has been shown to perform well with real clinical data.

Usage

```
cluster_membership(m)
```

Arguments

`m` the adjacency matrix.

Value

A factor variable with cluster memberships for each cohort in the study.

See Also

basket mem_mcmc mem_exact

`cluster_pep`*Get the Clusterwise Posterior Exchangeability Matrix*

Description

MEM analyses include the posterior exchangeability probability (PEP) of clusters of arms giving the probability that any two arms are exchangeable. This function returns the matrix of those probabilities.

Usage

```
cluster_pep(x)
```

Arguments

`x` either an exchangeability model or basket object.

Examples

```
# Create an MEM analysis of the Vemurafenib trial data.
data(vemu_wide)

mem_analysis <- mem_exact(
  vemu_wide$responders,
  vemu_wide$evaluatable,
  vemu_wide$baskets
)

# Get cluster PEPs.
basket_pep(mem_analysis)
```

`get_seed`*Get the Current Random Seed*

Description

Get the value of the current random seed. If one has not been initialized, then initialize it and return the new seed value.

Usage

```
get_seed()
```

 mem_exact

Fit the Exact MEM Model

Description

Fit the MEM model using full Bayesian inference.

Usage

```
mem_exact(
  responses,
  size,
  name,
  p0 = 0.15,
  shape1 = 0.5,
  shape2 = 0.5,
  prior = diag(length(responses))/2 + matrix(0.5, nrow = length(responses), ncol =
    length(responses)),
  hpd_alpha = 0.05,
  alternative = "greater",
  seed = 1000,
  cluster_analysis = FALSE,
  call = NULL,
  cluster_function = cluster_membership
)
```

Arguments

| | |
|------------------|---|
| responses | the number of responses in each basket. |
| size | the size of each basket. |
| name | the name of each basket. |
| p0 | the null response rate for the poster probability calculation (default 0.15). |
| shape1 | the first shape parameter(s) for the prior of each basket (default 0.5). |
| shape2 | the second shape parameter(s) for the prior of each basket (default 0.5). |
| prior | the matrix giving the prior inclusion probability for each pair of baskets. The default is on on the main diagonal and 0.5 elsewhere. |
| hpd_alpha | the highest posterior density trial significance. |
| alternative | the alternative case definition (default greater) |
| seed | the random number seed. |
| cluster_analysis | if the cluster analysis is conducted. |
| call | the call of the function (default NULL). |
| cluster_function | a function to cluster baskets |

See Also

cluster_membership

Examples

```
# 3 baskets, each with enrollement size 5
trial_sizes <- rep(5, 3)

# The response rates for the baskets.
resp_rate <- 0.15

# The trials: a column of the number of responses and a column of the
# the size of each trial.
trials <- data.frame(
  responses = rbinom(trial_sizes, trial_sizes, resp_rate),
  size = trial_sizes,
  name = letters[1:3]
)

summary(mem_exact(trials$responses, trials$size, trials$name))
```

mem_mcmc

Fit the MEM Model using MCMC

Description

Fit the MEM model using Bayesian Metropolis-Hasting MCMC inference.

Usage

```
mem_mcmc(
  responses,
  size,
  name,
  p0 = 0.15,
  shape1 = 0.5,
  shape2 = 0.5,
  prior = diag(length(responses))/2 + matrix(0.5, nrow = length(responses), ncol =
    length(responses)),
  hpd_alpha = 0.05,
  alternative = "greater",
  mcmc_iter = 2e+05,
  mcmc_burnin = 50000,
  initial_mem = round(prior - 0.001),
  seed = 1000,
  cluster_analysis = FALSE,
```

```

    call = NULL,
    cluster_function = cluster_membership
  )

```

Arguments

| | |
|------------------|---|
| responses | the number of responses in each basket. |
| size | the size of each basket. |
| name | the name of each basket. |
| p0 | the null response rate for the poster probability calculation (default 0.15). |
| shape1 | the first shape parameter(s) for the prior of each basket (default 0.5). |
| shape2 | the second shape parameter(s) for the prior of each basket (default 0.5). |
| prior | the matrix giving the prior inclusion probability for each pair of baskets. The default is on on the main diagonal and 0.5 elsewhere. |
| hpd_alpha | the highest posterior density trial significance. |
| alternative | the alternative case definition (default greater) |
| mcmc_iter | the number of MCMC iterations. |
| mcmc_burnin | the number of MCMC Burn_in iterations. |
| initial_mem | the initial MEM matrix. |
| seed | the random number seed. |
| cluster_analysis | if the cluster analysis is conducted. |
| call | the call of the function. |
| cluster_function | a function to cluster baskets |

Examples

```

# 3 baskets, each with enrollement size 5
trial_sizes <- rep(5, 3)

# The response rates for the baskets.
resp_rate <- 0.15

# The trials: a column of the number of responses and a column of the
# the size of each trial.
trials <- data.frame(
  responses = rbinom(trial_sizes, trial_sizes, resp_rate),
  size = trial_sizes,
  name = letters[1:3]
)
res <- mem_mcmc(trials$responses, trials$size)

```

`plot_density`*Plot the Response Densities in Basket Trials*

Description

The MEM analysis calculates the probability of exchangeability of baskets and clusters in a basket trial. This function creates density plots of the response rates of each basket or each cluster under the MEM design taking into account the extent to which power can be borrowed from similar trials.

Usage

```
plot_density(x, ...)
```

Arguments

`x` the exchangeability model.
`...` other options. See Details for more information.

Details

The ... options can be used to specify the colors of the response density plot or, when plotting an object of class `'exchangeability_model'` the type can be specified. In this case, the default is `'type = c("both", "basket", "cluster")'`.

Examples

```
# Create an MEM analysis of the Vemurafenib trial data.
data(vemu_wide)

mem_analysis <- mem_exact(
  vemu_wide$responders,
  vemu_wide$evaluatable,
  vemu_wide$baskets
)

plot_density(mem_analysis)
```

plot_map

Plot the Map Exchangeability of a Basket Trial

Description

The Maximum A Posteriori Probability (MAP) of an MEM is the estimate of the exchangeability structure of a basket trial. This function visualizes this matrix as an exchangeogram.

Usage

```
plot_map(x, ...)
```

Arguments

`x` basket element of the exchangeability model.
`...` other options passed to ggplot2 to alter the visual

Details

The `plot_map` function attempts to place the basket names to the left of the main diagonal in a way that makes it easy to read. However, for especially long basket names options are provided. Here is a list of all options available to “fine tune” the visualizations. These auxiliary options include:

- `[palette]` A color palette consisting of 3 colors: the first corresponds to a low degree of exchangeability, the second to 50 exchangeability, and the third to a high degree of exchangeability. Interpolation between these colors is performed for intermediary degrees of exchangeability.
- `[text_color]` A text string setting the color of the exchangeability values printed on the plot. (Default "white")
- `[tile_color]` A text string setting the color of the edges of the tiles. (Default "white")
- `[expand]` The proportion to expand the viewport (Default `expand = c(0.3, 0.3)`)
- `[text_size]` The text size. (Default 4)
- `[legend_position]` The legend position. (Default `legend_position = c(0.25, 0.8)`)
- `[draw_legend]` Should the legend be drawn? (Default TRUE)
- `[basket_name_hoffset]` The horizontal offset of the basket names.. (Default 0)
- `[basket_name_hjust]` The basket name justification.. (Default 1 - right justified)

Examples

```
# Create an MEM analysis of the Vemurafenib trial data.
data(vemu_wide)

mem_analysis <- mem_exact(
  vemu_wide$responders,
```

```

    vemu_wide$evaluable,
    vemu_wide$baskets
  )

plot_map(mem_analysis$basket)

```

plot_mem

Plot the Prior, MAP, and PEP of a Basket Trial

Description

: Plot the Prior, MAP, and PEP Matrices

Usage

```
plot_mem(x, type = c("prior", "map", "pep"), ...)
```

Arguments

x the exchangeability model.
 type the plot type that will be plotted.
 ... other options. See Details for more information.

plot_pep

Plot the Posterior Exchangeability of a Basket Trial

Description

The posterior exchangeability of the baskets in a MEM analysis can be visualized via an exchangeogram using this function.

Usage

```
plot_pep(x, ...)
```

Arguments

x basket element of the exchangeability model.
 ... other options passed to ggplot2 to alter the visual characteristics of the plot. See Details for more information.

Details

The `plot_pep` function attempts to place the basket names to the left of the main diagonal in a way that makes it easy to read. However, for especially long basket names options are provided. Here is a list of all options available to “fine tune” the visualizations. These auxiliary options include:

- `[palette]` A color palette consisting of 3 colors: the first corresponds to a low degree of exchangeability, the second to 50 exchangeability, and the third to a high degree of exchangeability. Interpolation between these colors is performed for intermediary degrees of exchangeability. `[text_color]`A text string setting the color of the exchangeability values printed on the plot. (Default "white") `[tile_color]`A text string setting the color of the edges of the tiles. (Default "white") (Default `RColorBrewer::brewer.pal(3, "BuGn")`)
- `[expand]` The proportion to expand the viewport (Default `expand = c(0.3, 0.3)`)
- `[text_size]` The text size. (Default 4)
- `[legend_position]` The legend position. (Default `legend_position = c(0.25, 0.8)`)
- `[draw_legend]` Should the legend be drawn? (Default TRUE)
- `[basket_name_hoffset]` The horizontal offset of the basket names.. (Default 0)
- `[basket_name_hjust]` The basket name justification.. (Default 1 - right justified)

Examples

```
# Create an MEM analysis of the Vemurafenib trial data.
data(vemu_wide)

mem_analysis <- mem_exact(
  vemu_wide$responders,
  vemu_wide$evaluable,
  vemu_wide$baskets
)

plot_pep(mem_analysis$basket)
```

plot_pep_graph

Plot a Network Graph of the PEP Matrix

Description

Plot a Network Graph of the PEP Matrix

Usage

```
plot_pep_graph(
  x,
  color_by = c("post_prob", "mean_est", "median_est"),
  layout = c("fr", "nicely", "kk", "drl"),
  pep_cutoff = 0
)
```

Arguments

| | |
|------------|---|
| x | the exchangeability model. |
| color_by | which variable to color by. One of "post_prob", "mean_est", "median_est". |
| layout | the layout algorithm to use for the graph. One of |
| pep_cutoff | a value between 0 and 1 indicating the cutoff for PEP above which edges of the graph will be drawn. |

Examples

```
# Create an MEM analysis of the Vemurafenib trial data.
data(vemu_wide)

mem_analysis <- mem_exact(
  vemu_wide$responders,
  vemu_wide$evaluatable,
  vemu_wide$baskets
)

plot_pep_graph(mem_analysis)
```

sample_posterior

Sample Posterior Samples from a Basket Trial

Description

Sample Posterior Samples from a Basket Trial

Usage

```
sample_posterior(model, num_samples = 10000)
```

Arguments

| | |
|-------------|--|
| model | the exchangeability model |
| num_samples | the number of samples to draw. Default 10000 |

Examples

```
# 3 baskets, each with enrollement size 5
trial_sizes <- rep(5, 3)

# The response rates for the baskets.
resp_rate <- 0.15
```

```
# The trials: a column of the number of responses and a column of the
# the size of each trial.
trials <- data.frame(
  responses = rbinom(trial_sizes, trial_sizes, resp_rate),
  size = trial_sizes,
  name = paste("Basket", seq_len(3))
)
```

update_p0

Update Full Bayes results with different p0 values

Description

After running either ‘mem_mcmc’ or ‘mem_exact’, the test can be updated without rerunning the entire analysis. This function provides updating of both the null response rate along with the alternative rerunning relevant test.

Usage

```
update_p0(res, p0 = 0.15, alternative = "greater")
```

Arguments

| | |
|-------------|---|
| res | the result of an mem analysis. |
| p0 | the null response rate for the poster probability calculation (default 0.15). |
| alternative | the alternative case definition (default greater) |

Examples

```
## Not run:
# Create an MEM analysis of the Vemurafenib trial data.
data(vemu_wide)

mem_analysis <- mem_exact(
  vemu_wide$responders,
  vemu_wide$evaluatable,
  vemu_wide$baskets
)

# Update the null from p0 = 0.15 the default, to p = 0.25.
update_p0(mem_analysis, 0.20)

## End(Not run)
```

Description

The 'vemu' and 'vemu_wide' data sets provides response information taken from the "Vemurafenib in multiple nonmelanoma cancers with BRAF v600 mutations" study where, in total, 18 responders were observed among the 84 patients contributing evaluable outcomes for statistical estimation. Observed response rates varied from 42% and 43% for baskets of NSCLC and ECD or LCH to 0 and 4%, for CRC with vemurafenib mono and combination therapies, respectively. Two responders of seven patients, ATC was associated with a 29% response rate, while one responder of eight patients was observed in the cholangiocarcinoma basket. Contrasting favorable results for preliminary vemurafenib activity among NSCLC and ECD or LCH patients with less favorable results for CRC patients, the authors concluded that nonmelanoma tumor types harboring BRAF^{V600} mutations failed to respond uniformly to BRAF-targeted therapy giving credence to more conventional organ-specific nosology when compared to molecular tumor nosology.

Later, in the "Statistical challenges posed by basket trials: sensitivity analysis of the Vemurafenib study" it was shown that patient-enrollment types we likely drove the negative results for several targets, rather than Vemurafenib itself.

References

Hyman DM, Puzanov I, Subbiah V, Faris JE, Chau I, Blay JY, Wolf J, Raje NS, Diamond EL, Hollebecque A, et al. Vemurafenib in multiple nonmelanoma cancers with braf v600 mutations. *New England Journal of Medicine* 2015; **373**(8):726

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