## Package ‘hdme’

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### R topics documented:

- coef.corrected_lasso  
- coef.gds
coef.corrected_lasso

Extract Coefficients of a Corrected Lasso object

Description

Default coef method for a corrected_lasso object.

Usage

## S3 method for class 'corrected_lasso'
coef(object, ...)

Arguments

object Fitted model object returned by corrected_lasso.
... Other arguments (not used).
**coef.gds**

*Extract Coefficients of a Generalized Dantzig Selector Object*

### Description

Default coef method for a gds object.

### Usage

```r
## S3 method for class 'gds'
coef(object, all = FALSE, ...)
```

### Arguments

- `object`: Fitted model object returned by `gds`.
- `all`: Logical indicating whether to show all coefficient estimates, or only non-zeros.
- `...`: Other arguments (not used).

---

**coef.gmus**

*Extract Coefficients of a GMUS object*

### Description

Default coef method for a gmus object.

### Usage

```r
## S3 method for class 'gmus'
coef(object, all = FALSE, ...)
```

### Arguments

- `object`: Fitted model object returned by `gmus`.
- `all`: Logical indicating whether to show all coefficient estimates, or only non-zeros. Only used when delta is a single value.
- `...`: Other arguments (not used).
coef.gmu_lasso  Extract Coefficients of a GMU Lasso object

Description

Default coef method for a gmu_lasso object.

Usage

## S3 method for class 'gmu_lasso'
coef(object, all = FALSE, ...)

Arguments

object  Fitted model object returned by gmu_lasso.
all  Logical indicating whether to show all coefficient estimates, or only non-zeros. Only used when delta is a single value.
...  Other arguments (not used).

corrected_lasso  Corrected Lasso

Description

Lasso (L1-regularization) for generalized linear models with measurement error.

Usage

corrected_lasso(  
  W,  
  y,  
  sigmaUU,  
  family = c("gaussian", "binomial", "poisson"),  
  radii = NULL,  
  no_radii = NULL,  
  alpha = 0.1,  
  maxits = 5000  
)
**Arguments**

- **W**: Design matrix, measured with error. Must be a numeric matrix.
- **y**: Vector of responses.
- **sigmaUU**: Covariance matrix of the measurement error.
- **family**: Response type. Character string of length 1. Possible values are "gaussian", "binomial" and "poisson".
- **radii**: Vector containing the set of radii of the l1-ball onto which the solution is projected. If not provided, the algorithm will select an evenly spaced vector of 20 radii.
- **no_radii**: Length of vector radii, i.e., the number of regularization parameters to fit the corrected lasso for.
- **alpha**: Step size of the projected gradient descent algorithm. Default is 0.1.
- **maxits**: Maximum number of iterations of the project gradient descent algorithm for each radius. Default is 5000.

**Details**

Corrected version of the lasso for generalized linear models. The method does require an estimate of the measurement error covariance matrix.

**Value**

An object of class "corrected_lasso".

**References**


**Examples**

```r
# Example with linear regression
# Number of samples
n <- 100
# Number of covariates
p <- 50
# True (latent) variables
X <- matrix(rnorm(n * p), nrow = n)
# Measurement error covariance matrix
sigmaUU <- diag(x = 0.2, nrow = p, ncol = p)
# Measurement matrix (this is the one we observe)
W <- X + rnorm(n, sd = diag(sigmaUU))
# Coefficient
beta <- c(seq(from = 0.1, to = 1, length.out = 5), rep(0, p-5))
# Response
```
y <- X %*% beta + rnorm(n, sd = 1)
# Run the corrected lasso
fit <- corrected_lasso(W, y, sigmaUU, family = "gaussian")
coef(fit)
plot(fit)
plot(fit, type = "path")

# Binomial, logistic regression
# Number of samples
n <- 1000
# Number of covariates
p <- 50
# True (latent) variables
X <- matrix(rnorm(n * p), nrow = n)
# Measurement error covariance matrix
sigmaUU <- diag(x = 0.2, nrow = p, ncol = p)
# Measurement matrix (this is the one we observe)
W <- X + rnorm(n, sd = diag(sigmaUU))
logit <- function(x) (1+exp(-x))^(-1)
# Response
y <- rbinom(n, size = 1, prob = logit(X %*% c(rep(5, 5), rep(0, p-5))))
fit <- corrected_lasso(W, y, sigmaUU, family = "binomial")
plot(fit)
coef(fit)

cv_corrected_lasso

Cross-validated Corrected lasso

Description

Cross-validated Corrected lasso

Usage

cv_corrected_lasso(
  W,
  y,
  sigmaUU,
  n_folds = 10,
  family = "gaussian",
  radii = NULL,
  no_radii = 100,
  alpha = 0.1,
  maxits = 5000
)
Arguments

- \( \mathbf{W} \): Design matrix, measured with error.
- \( y \): Vector of the continuous response value.
- \( \sigma_{UU} \): Covariance matrix of the measurement error.
- \( n_{folds} \): Number of folds to use in cross-validation. Default is 100.
- \( \text{family} \): Only "gaussian" is implemented at the moment.
- \( \text{radii} \): Optional vector containing the set of radii of the l1-ball onto which the solution is projected.
- \( \text{no_radii} \): Length of vector radii, i.e., the number of regularization parameters to fit the corrected lasso for.
- \( \alpha \): Optional step size of the projected gradient descent algorithm. Default is 0.1.
- \( \text{maxits} \): Optional maximum number of iterations of the project gradient descent algorithm for each radius. Default is 5000.

Details

Corrected version of the lasso for the case of linear regression, estimated using cross-validation. The method does require an estimate of the measurement error covariance matrix.

Value

An object of class "cv_corrected_lasso".

References


Examples

```r
# Gaussian
set.seed(100)
n <- 100; p <- 50 # Problem dimensions
# True (latent) variables
X <- matrix(rnorm(n * p), nrow = n)
# Measurement error covariance matrix
sigmaUU <- diag(x = 0.2, nrow = p, ncol = p)
# Measurement matrix (this is the one we observe)
W <- X + rnorm(n, sd = diag(sigmaUU))
# Coefficient
beta <- c(seq(from = 0.1, to = 1, length.out = 5), rep(0, p-5))
# Response
y <- X %*% beta + rnorm(n, sd = 1)
# Run the corrected lasso
```
cvfit <- cv_corrected_lasso(W, y, sigmaUU, no_radii = 5, n_folds = 3)
plot(cvfit)
print(cvfit)
# Run the standard lasso using the radius found by cross-validation
fit <- corrected_lasso(W, y, sigmaUU, family = "gaussian",
radii = cvfit$radius_min)
coef(fit)
plot(fit)

---

**cv_gds**  
*Cross-Validated Generalized Dantzig Selector*

**Description**

Generalized Dantzig Selector with cross-validation.

**Usage**

```r
cv_gds(
  X,
  y,
  family = "gaussian",
  no_lambda = 10,
  lambda = NULL,
  n_folds = 5,
  weights = rep(1, length(y))
)
```

**Arguments**

- **X**  
  Design matrix.

- **y**  
  Vector of the continuous response value.

- **family**  
  Use "gaussian" for linear regression, "binomial" for logistic regression and "poisson" for Poisson regression.

- **no_lambda**  
  Length of the vector lambda of regularization parameters. Note that if lambda is not provided, the actual number of values might differ slightly, due to the algorithm used by glmlnet::glmlnet in finding a grid of lambda values.

- **lambda**  
  Regularization parameter. If not supplied and if no_lambda > 1, a sequence of no_lambda regularization parameters is computed with glmlnet::glmlnet. If no_lambda = 1 then the cross-validated optimum for the lasso is computed using glmlnet::cv.glmlnet.

- **n_folds**  
  Number of cross-validation folds to use.

- **weights**  
  A vector of weights for each row of X. Defaults to 1 per observation.
Details

Cross-validation loss is calculated as the deviance of the model divided by the number of observations. For the Gaussian case, this is the mean squared error. Weights supplied through the weights argument are used both in fitting the models and when evaluating the test set deviance.

Value

An object of class cv_gds.

References


Examples

```R
## Not run:
# Example with logistic regression
n <- 1000  # Number of samples
p <- 10    # Number of covariates
X <- matrix(rnorm(n * p), nrow = n) # True (latent) variables # Design matrix
beta <- c(seq(from = 0.1, to = 1, length.out = 5), rep(0, p-5)) # True regression coefficients
y <- rbinom(n, 1, (1 + exp(-X %*% beta))^-1) # Binomially distributed response
cv_fit <- cv_gds(X, y, family = "binomial", no_lambda = 50, n_folds = 10)
print(cv_fit)
plot(cv_fit)

# Now fit a single GDS at the optimum lambda value determined by cross-validation
fit <- gds(X, y, lambda = cv_fit$lambda_min, family = "binomial")
plot(fit)

# Compare this to the fit for which lambda is selected by GDS
# This automatic selection is performed by glmnet::cv.glmnet, for
# the sake of speed
fit2 <- gds(X, y, family = "binomial")

The following plot compares the two fits.
library(ggplot2)
library(tidyr)
df <- data.frame(fit = fit$beta, fit2 = fit2$beta, index = seq(1, p, by = 1))
ggplot(gather(df, key = "Model", value = "Coefficient", -index)) +
geom_point() +
theme(legend.title = element_blank())

## End(Not run)
```
Description

Generalized Dantzig Selector

Usage

gds(X, y, lambda = NULL, family = "gaussian", weights = NULL)

Arguments

X Design matrix.
y Vector of the continuous response value.
lambda Regularization parameter. Only a single value is supported.
family Use "gaussian" for linear regression, "binomial" for logistic regression and "poisson" for Poisson regression.
weights A vector of weights for each row of X.

Value

Intercept and coefficients at the values of lambda specified.

References


Examples

```r
# Example with logistic regression
n <- 1000 # Number of samples
p <- 10 # Number of covariates
X <- matrix(rnorm(n * p), nrow = n) # True (latent) variables # Design matrix
beta <- c(seq(from = 0.1, to = 1, length.out = 5), rep(0, p-5)) # True regression coefficients
y <- rbinom(n, 1, (1 + exp(-X %*% beta))^(-1)) # Binomially distributed response
fit <- gds(X, y, family = "binomial")
print(fit)
plot(fit)
coef(fit)

# Try with more penalization
fit <- gds(X, y, family = "binomial", lambda = 0.1)
coef(fit)
```
# Case weighting
# Assume we wish to put more emphasis on predicting the positive cases correctly
# In this case we give the 1s three times the weight of the zeros.
weights <- (y == 0) * 1 + (y == 1) * 3
fit_w <- gds(X, y, family = "binomial", weights = weights, lambda = 0.1)

# Next we test this on a new dataset, generated with the same parameters
X_new <- matrix(rnorm(n * p), nrow = n)
y_new <- rbinom(n, 1, (1 + exp(-X_new %*% beta))^(-1))
# We use a 50 % threshold as classification rule
# Unweighted classification
classification <- ((1 + exp(- fit$intercept - X_new %*% fit$beta))^(-1) > 0.5) * 1
# Weighted classification
classification_w <- ((1 + exp(- fit_w$intercept - X_new %*% fit_w$beta))^(-1) > 0.5) * 1

# As expected, the weighted classification predicts many more 1s than 0s, since
# these are heavily up-weighted
table(classification, classification_w)

# Here we compare the performance of the weighted and unweighted models.
# The weighted model gets most of the 1s right, while the unweighted model
# gets the highest overall performance.
table(classification, y_new)
table(classification_w, y_new)

gmus

Generalized Matrix Uncertainty Selector

Description

Generalized Matrix Uncertainty Selector

Usage

gmus(W, y, lambda = NULL, delta = NULL, family = "gaussian", weights = NULL)

Arguments

W       Design matrix, measured with error. Must be a numeric matrix.
y       Vector of responses.
lambda  Regularization parameter.
delta   Additional regularization parameter, bounding the measurement error.
family  "gaussian" for linear regression, "binomial" for logistic regression or "poisson" for Poisson regression. Defaults go "gaussian".
weights A vector of weights for each row of X.
Value

An object of class "gmus".

References


Examples

```r
# Example with linear regression
set.seed(1)
n <- 100 # Number of samples
p <- 50 # Number of covariates
# True (latent) variables
X <- matrix(rnorm(n * p), nrow = n)
# Measurement matrix (this is the one we observe)
W <- X + matrix(rnorm(n*p, sd = 1), nrow = n, ncol = p)
# Coefficient vector
beta <- c(seq(from = 0.1, to = 1, length.out = 5), rep(0, p-5))
# Response
y <- X %*% beta + rnorm(n, sd = 1)
# Run the MU Selector
fit1 <- gmus(W, y)
# Draw an elbow plot to select delta
plot(fit1)
coef(fit1)

# Now, according to the "elbow rule", choose
# the final delta where the curve has an "elbow".
# In this case, the elbow is at about delta = 0.08,
# so we use this to compute the final estimate:
fit2 <- gmus(W, y, delta = 0.08)
# Plot the coefficients
plot(fit2)
coef(fit2)
coef(fit2, all = TRUE)
```

---

**gmu_lasso**

*Generalized Matrix Uncertainty Lasso*

**Description**

Generalized Matrix Uncertainty Lasso
Usage

gmu_lasso(
  W,
  y,
  lambda = NULL,
  delta = NULL,
  family = "binomial",
  active_set = TRUE,
  maxit = 1000
)

Arguments

- **W**: Design matrix, measured with error. Must be a numeric matrix.
- **y**: Vector of responses.
- **lambda**: Regularization parameter. If not set, lambda.min from glmnet::cv.glmnet is used.
- **delta**: Additional regularization parameter, bounding the measurement error.
- **family**: Character string. Currently "binomial" and "poisson" are supported.
- **active_set**: Logical. Whether or not to use an active set strategy to speed up coordinate descent algorithm.
- **maxit**: Maximum number of iterations of iterative reweighing algorithm.

Value

An object of class "gmu_lasso".

References


Examples

```r
set.seed(1)
# Number of samples
n <- 200
# Number of covariates
p <- 100
# Number of nonzero features
s <- 10
# True coefficient vector
beta <- c(rep(1,s),rep(0,p-s))
# Standard deviation of measurement error
sdU <- 0.2
```
# True data, not observed
X <- matrix(rnorm(n*p), nrow = n, ncol = p)

# Measured data, with error
W <- X + sdU * matrix(rnorm(n * p), nrow = n, ncol = p)

# Binomial response
y <- rbinom(n, 1, (1 + exp(-X%*%beta))**(-1))

# Run the GMU Lasso
fit <- gmu_lasso(W, y, delta = NULL)
print(fit)
plot(fit)
coef(fit)

# Get an elbow plot, in order to choose delta.
plot(fit)

---

**mus**

*Matrix Uncertainty Selector*

**Description**

Matrix Uncertainty Selector for linear regression.

**Usage**

```r
mus(W, y, lambda = NULL, delta = NULL)
```

**Arguments**

- `W`  
  Design matrix, measured with error. Must be a numeric matrix.
- `y`  
  Vector of responses.
- `lambda`  
  Regularization parameter.
- `delta`  
  Additional regularization parameter, bounding the measurement error.

**Details**

This function is just a wrapper for `gmus(W, y, lambda, delta, family = "gaussian")`.

**Value**

An object of class "gmus".

**References**


Examples

# Example with Gaussian response
set.seed(1)
# Number of samples
n <- 100
# Number of covariates
p <- 50
# True (latent) variables
X <- matrix(rnorm(n * p), nrow = n)
# Measurement matrix (this is the one we observe)
W <- X + matrix(rnorm(n*p, sd = 1), nrow = n, ncol = p)
# Coefficient vector
beta <- c(seq(from = 0.1, to = 1, length.out = 5), rep(0, p-5))
# Response
y <- X %*% beta + rnorm(n, sd = 1)
# Run the MU Selector
fit1 <- mus(W, y)
# Draw an elbow plot to select delta
plot(fit1)
coef(fit1)

# Now, according to the "elbow rule", choose the final delta where the curve has an "elbow".
# In this case, the elbow is at about delta = 0.08, so we use this to compute the final estimate:
fit2 <- mus(W, y, delta = 0.08)
plot(fit2) # Plot the coefficients
coef(fit2)
coef(fit2, all = TRUE)

plot.corrected_lasso

Description

Plot the output of corrected_lasso

Usage

## S3 method for class 'corrected_lasso'
plot(x, type = "nonzero", ...)

Arguments

x Object of class corrected_lasso, returned from calling corrected_lasso()

<table>
<thead>
<tr>
<th>Argument</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>type</td>
<td>Type of plot. Either &quot;nonzero&quot; or &quot;path&quot;. Ignored if length(x$radii) == 1, in case of which all coefficient estimates are plotted at the given regularization parameter.</td>
</tr>
<tr>
<td>...</td>
<td>Other arguments to plot (not used)</td>
</tr>
</tbody>
</table>
Examples

# Example with linear regression
n <- 100 # Number of samples
p <- 50 # Number of covariates
# True (latent) variables
X <- matrix(rnorm(n * p), nrow = n)
# Measurement error covariance matrix
# (typically estimated by replicate measurements)
sigmaUU <- diag(x = 0.2, nrow = p, ncol = p)
# Measurement matrix (this is the one we observe)
W <- X + rnorm(n, sd = diag(sigmaUU))
# Coefficient
beta <- c(seq(from = 0.1, to = 1, length.out = 5), rep(0, p-5))
# Response
y <- X %*% beta + rnorm(n, sd = 1)
# Run the corrected lasso
fit <- corrected_lasso(W, y, sigmaUU, family = "gaussian")
plot(fit)

Description

Plot the output of \texttt{cv_corrected_lasso}.

Usage

## S3 method for class 'cv_corrected_lasso'
plot(x, ...)

Arguments

x The object to be plotted, returned from \texttt{cv_corrected_lasso}.
...
Other arguments to plot (not used).

Description

Plot the output of \texttt{cv_gds}. 
plot.gds

Usage

```r
## S3 method for class 'cv_gds'
plot(x, ...)
```

Arguments

- `x` The object to be plotted, returned from `cv_gds`.
- `...` Other arguments to plot (not used).

Description

Plot the number of nonzero coefficients at the given lambda.

Usage

```r
## S3 method for class 'gds'
plot(x, ...)
```

Arguments

- `x` An object of class `gds`
- `...` Other arguments to plot (not used).

Examples

```r
set.seed(1)
# Example with logistic regression
# Number of samples
n <- 1000
# Number of covariates
p <- 10
# True (latent) variables (Design matrix)
X <- matrix(rnorm(n * p), nrow = n)
# True regression coefficients
beta <- c(seq(from = 0.1, to = 1, length.out = 5), rep(0, p-5))
# Binomially distributed response
y <- rbinom(n, 1, (1 + exp(-X %*% beta))^(-1))
# Fit the generalized Dantzig Selector
gds <- gds(X, y, family = "binomial")
# Plot the estimated coefficients at the chosen lambda
plot(gds)
```
Description
Plot the number of nonzero coefficients along a range of delta values if delta has length larger than 1, or the estimated coefficients if delta has length 1.

Usage
## S3 method for class 'gmus'
plot(x, ...)  

Arguments
x An object of class gmus
... Other arguments to plot (not used).

Examples
# Example with linear regression
set.seed(1)
# Number of samples
n <- 100
# Number of covariates
p <- 50
# True (latent) variables
X <- matrix(rnorm(n * p), nrow = n)
# Measurement matrix (this is the one we observe)
W <- X + matrix(rnorm(n*p, sd = 0.4), nrow = n, ncol = p)
# Coefficient vector
beta <- c(seq(from = 0.1, to = 1, length.out = 5), rep(0, p-5))
# Response
y <- X %*% beta + rnorm(n, sd = 1)
# Run the MU Selector
mus1 <- mus(W, y)
# Draw an elbow plot to select delta
plot(mus1)

# Now, according to the "elbow rule", choose the final
delta where the curve has an "elbow".
# In this case, the elbow is at about delta = 0.08, so
# we use this to compute the final estimate:
mus2 <- mus(W, y, delta = 0.08)
# Plot the coefficients
plot(mus2)
plot.gmu_lasso

Plot the estimates returned by gmu_lasso

Description

Plot the number of nonzero coefficients along a range of delta values if delta has length larger than 1, or the estimated coefficients of delta has length 1.

Usage

## S3 method for class 'gmu_lasso'
plot(x, ...)

Arguments

x
An object of class gmu_lasso

... Other arguments to plot (not used).

Examples

set.seed(1)
n <- 200
p <- 50
s <- 10
beta <- c(rep(1,s),rep(0,p-s))
sdU <- 0.2

X <- matrix(rnorm(n*p),nrow = n,ncol = p)
W <- X + sdU * matrix(rnorm(n * p), nrow = n, ncol = p)

y <- rbinom(n, 1, (1 + exp(-X%*%beta))**(-1))
gmu_lasso <- gmu_lasso(W, y)

plot(gmu_lasso)

print.corrected_lasso

Print a Corrected Lasso object

Description

Default print method for a corrected_lasso object.

Usage

## S3 method for class 'corrected_lasso'
print(x, ...)

print(gmu_lasso)

Arguments

- `x` Fitted model object returned by `corrected_lasso`.
- `...` Other arguments (not used).

---

**print.cv_corrected_lasso**

*Print a Cross-Validated Corrected Lasso object*

Description

Default print method for a `cv_corrected_lasso` object.

Usage

```r
## S3 method for class 'cv_corrected_lasso'
print(x, ...)
```

Arguments

- `x` Fitted model object returned by `cv_corrected_lasso`.
- `...` Other arguments (not used).

---

**print.cv_gds**

*Print a Cross-Validated GDS Object*

Description

Default print method for a `cv_gds` object.

Usage

```r
## S3 method for class 'cv_gds'
print(x, ...)
```

Arguments

- `x` Fitted model object returned by `cv_gds`.
- `...` Other arguments (not used).
print.gds

Print a Generalized Dantzig Selector Object

Description
Default print method for a gds object.

Usage
## S3 method for class 'gds'
print(x, ...)

Arguments
x Fitted model object returned by gds.
... Other arguments (not used).

print.gmus

Print a GMUS object

Description
Default print method for a gmus object.

Usage
## S3 method for class 'gmus'
print(x, ...)

Arguments
x Fitted model object returned by gmus.
... Other arguments (not used).
Description

Default print method for a gmu_lasso object.

Usage

```r
## S3 method for class 'gmu_lasso'
print(x, ...)  
```

Arguments

- `x` Fitted model object returned by `gmu_lasso`.
- `...` Other arguments (not used).
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