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Description Provides fast and accurate inference for the parameter estimation problem in Ordinary Differential Equations, including the case when there are unobserved system components. Implements the MAGI method (MAnifold-constrained Gaussian process Inference) of Yang, Wong, and Kou (2021) <doi:10.1073/pnas.2020397118>.
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**Description**

Covariance calculations for Gaussian process kernels. Currently supports matern, rbf, compact1, periodicMatern, generalMatern, and rationalQuadratic kernels. Can also return m_phi and other additional quantities useful for ODE inference.

**Usage**

```r
calCov(
  phi,
  rInput,
  signrInput,
  bandsize = NULL,
  complexity = 3,
  kerneltype = "matern",
  df,
  noiseInjection = 1e-07
)
```

**Arguments**

- **phi**
  - the kernel hyper-parameters. See details for hyper-parameter specification for each `kerneltype`.

- **rInput**
  - the distance matrix between all time points s and t, i.e., |s - t|

- **signrInput**
  - the sign matrix of the time differences, i.e., sign(s - t)

- **bandsize**
  - size for band matrix approximation. See details.

- **complexity**
  - integer value for the complexity of the kernel calculations desired:
    - 0 includes C only
    - 1 additionally includes Cprime, Cdoubleprime, dCdphi
    - 2 or above additionally includes Ceigen1over, CeigenVec, Cinv, mphi, Kphi, Keigen1over, KeigenVec, Kinv, mphiLeftHalf, dCdphiCube
  - See details for their definitions.

- **kerneltype**
  - must be one of matern, rbf, compact1, periodicMatern, generalMatern, rationalQuadratic. See details for the kernel formulae.

- **df**
  - degrees of freedom, for generalMatern and rationalQuadratic kernels only. Default is df=2.01 for generalMatern and df=0.01 for rationalQuadratic.
noiseInjection a small value added to the diagonal elements of C and Kphi for numerical stability

Details

The covariance formulae and the hyper-parameters phi for the supported kernels are as follows. Stationary kernels have $C(s, t) = C(r)$ where $r = |s - t|$ is the distance between the two time points. Generally, the hyper-parameter $\phi[1]$ controls the overall variance level while $\phi[2]$ controls the bandwidth.

matern This is the simplified Matern covariance with $\text{df} = 5/2$:

$$C(r) = \phi[1] \times \left(1 + \sqrt{5r}/\phi[2] + 5r^2/(3\phi[2]^2)\right) \times \exp\left(-\sqrt{5r}/\phi[2]\right)$$

rbf

$$C(r) = \phi[1] \times \exp\left(-r^2/(2\phi[2]^2)\right)$$

compact1

$$C(r) = \phi[1] \times \max(1 - r/\phi[2], 0)^4 \times (4r/\phi[2] + 1)$$

periodicMatern Define $r' = |\sin(r\pi/\phi[3])| \times 2$. Then the covariance is given by $C(r')$ using the Matern formula.

generalMatern

$$C(r) = \phi[1] \times 2^{(1 - \text{df})} / \Gamma(\text{df}) \times (\sqrt{10.0*df}*r/\phi[2])^\text{df}*\text{besselK}(\sqrt{10.0*df}*r/\phi[2], \text{df})$$

where besselK is the modified Bessel function of the second kind.

rationalQuadratic

$$C(r) = \phi[1] \times (1 + r^2/(2df\phi[2]^2))^{(1 - \text{df})}$$

The kernel calculations available and their definitions are as follows:

C The covariance matrix corresponding to the distance matrix rInput.

Cprime The cross-covariance matrix $dC(s, t)/ds$.

Cdoubleprime The cross-covariance matrix $d^2C(s, t)/dsdt$.

dCdphi A list with the matrices $dC/dphi$ for each element of phi.

Ceigen1over The reciprocals of the eigenvalues of C.

CeigenVec Matrix of eigenvectors of C.

Cinv The inverse of C.

mphi The matrix Cprime * Cinv.

Kphi The matrix Cdoubleprime - Cprime * Kinv * t(Cprime).

Keigen1over The reciprocals of the eigenvalues of Kphi.

Kinv The inverse of Kphi.

mphiLeftHalf The matrix Cprime * CeigenVec.

dCdphiCube $dC/dphi$ as a 3-D array, with the third dimension corresponding to the elements of phi.

If bandsize is a positive integer, additionally CinvBand, mphiBand, and KinvBand are provided in the return list, which are band matrix approximations to Cinv, mphi, and Kinv with the specified bandsize.
Value
A list containing the kernel calculations included by the value of complexity.

Examples
foo <- outer(0:40, t(0:40), `-`)[,1]
r <- abs(foo)
signr <- -sign(foo)
calCov(c(0.2, 2), r, signr, bandsize=20, kerneltype="generalMatern", df=2.01)

gpsmoothing

Gaussian process smoothing

Description
Estimate hyper-parameters phi and noise standard deviation sigma for a vector of observations using Gaussian process smoothing.

Usage
gpsmoothing(yobs, tvec, kerneltype = "generalMatern", sigma = NULL)

Arguments

yobs vector of observations
tvec vector of time points corresponding to observations
kerneltype the covariance kernel, types matern, compact1, periodicMatern, generalMatern are supported. See calCov for their definitions.
sigma the noise level (if known). By default, both phi and sigma are estimated. If a value for sigma is supplied, then sigma is held fixed at the supplied value and only phi is estimated.

Value
A list containing the elements phi and sigma with their estimated values.

Examples
# Sample data and observation times
tvec <- seq(0, 20, by = 0.5)
y <- c(-1.16, -0.18, 1.57, 1.99, 1.95, 1.85, 1.49, 1.58, 1.47, 0.96, 0.75, 0.22, -1.34, -1.72, -2.11, -1.56, -1.51, -1.29, -1.22, -0.36, 1.78, 2.36, 1.78, 1.8, 1.76, 1.4, 1.02, 1.28, 1.21, 0.04, -1.35, -2.1, -1.9, -1.49, -1.55, -1.35, -0.98, -0.34, 1.9, 1.99, 1.84)
gpsmoothing(y, tvec)
**gpsmoothllik**

**Marginal log-likelihood for Gaussian process smoothing**

**Description**

Marginal log-likelihood and gradient as a function of GP hyper-parameters phi and observation noise standard deviation sigma. For use in Gaussian process smoothing where values of phi and sigma may be optimized.

**Usage**

gpsmoothllik(phisig, yobs, rInput, kerneltype = "generalMatern")

**Arguments**

- **phisig** vector containing GP hyper-parameters phi and observation noise SD sigma. See calCov for the definitions of the hyper-parameters.
- **yobs** vector of observations
- **rInput** distance matrix between all time points of yobs
- **kerneltype** the covariance kernel, types matern, rbf, compact1, periodicMatern, generalMatern are supported. See calCov for their definitions.

**Value**

A list with elements value and grad, which are the log-likelihood value and gradient with respect to phisig, respectively.

**Examples**

# Suppose phi[1] = 0.5, phi[2] = 3, sigma = 0.1
gpsmoothllik(c(0.5,3,0.1), rnorm(10), abs(outer(0:9, t(0:9), './')[,1,]))

**MagiPosterior**

**MAGI posterior density**

**Description**

Computes the MAGI log-posterior value and gradient for an ODE model with the given inputs: the observations Y, the latent system trajectories X, the parameters \( \theta \), the noise standard deviations \( \sigma \), and covariance kernels.
Usage

MagiPosterior(
  y,
  xlatent,
  theta,
  sigma,
  covAllDimInput,
  odeModel,
  priorTemperatureInput = 1,
  useBand = FALSE
)

Arguments

  y        data matrix of observations
  xlatent  matrix of system trajectory values
  theta    vector of parameter values \theta
  sigma    vector of observation noise for each system component
  covAllDimInput  list of covariance kernel objects for each system component. Covariance calculations may be carried out with \texttt{calCov}.
  odeModel list of ODE functions and inputs. See details.
  priorTemperatureInput  vector of tempering factors for the GP prior, derivatives, and observations, in that order. Controls the influence of the GP prior relative to the likelihood. Recommended values: the total number of observations divided by the total number of discretization points for the GP prior and derivatives, and 1 for the observations.
  useBand  logical: should the band matrix approximation be used? If \texttt{TRUE}, \texttt{covAllDimInput} must include CinvBand, mphiBand, and KinvBand as computed by \texttt{calCov}.

Value

A list with elements \texttt{value} for the value of the log-posterior density and \texttt{grad} for its gradient.

Examples

# Trajectories from the Fitzhugh-Nagumo equations
tvec <- seq(0, 20, 2)
Vtrue <- c(-1, 1.91, 1.38, -1.32, -1.5, 1.73, 1.66, 0.89, -1.82, -0.93, 1.89)
Rtrue <- c(1, 0.33, -0.62, -0.82, 0.5, 0.94, -0.22, -0.9, -0.08, 0.95, 0.3)

# Noisy observations
Vobs <- Vtrue + rnorm(length(tvec), sd = 0.05)
Rob <- Rtrue + rnorm(length(tvec), sd = 0.1)

# Prepare distance matrix for covariance kernel calculation
foo <- outer(tvec, t(tvec),'-')[,1,]
r <- abs(foo)
r2 <- r^2
signr <- -sign(foo)

# Choose some hyperparameter values to illustrate
rphi <- c(0.95, 3.27)
vphi <- c(1.98, 1.12)
phiTest <- cbind(vphi, rphi)

# Covariance computations
curCovV <- calCov(phiTest[,1], r, signr, kerneltype = "generalMatern")
curCovR <- calCov(phiTest[,2], r, signr, kerneltype = "generalMatern")

# Y and X inputs to MagiPosterior
yInput <- data.matrix(cbind(Vobs, Robs))
xlatentTest <- data.matrix(cbind(Vtrue, Rtrue))

# ODE system for Fitzhugh-Nagumo equations
fnmodelODE <- function(theta, x, t) {
  V <- x[,1]
  R <- x[,2]

  result <- array(0, c(nrow(x), ncol(x)))

  result
}

# Gradient with respect to system components
fnmodelDx <- function(theta, x, t) {
  resultDx <- array(0, c(nrow(x), ncol(x), ncol(x)))
  V = x[,1]

  resultDx[,1,1] = theta[3] * (1 - V^2)
  resultDx[,2,1] = theta[3]
  resultDx[,1,2] = (-1.0 / theta[3])
  resultDx[,2,2] = ( -1.0*theta[2]/theta[3] )

  resultDx
}

# Gradient with respect to parameters theta
fnmodelDtheta <- function(theta, x, t) {
  resultDtheta <- array(0, c(nrow(x), length(theta), ncol(x)))
  V = x[,1]
  R = x[,2]

  resultDtheta[,3,1] = V - V^3 / 3.0 + R
  resultDtheta[,1,2] = 1.0 / theta[3]
  resultDtheta[,2,2] = -R / theta[3]
\[
\text{resultDtheta}[3,2] = 1.0/(\text{theta}[3]^2) * (V - \text{theta}[1] + \text{theta}[2] * R)
\]

\[
\text{resultDtheta}
\]

# Create odeModel list
fnmodel <- list(
    fOde=fnmodelODE,
    fOdeDx=fnmodelDx,
    fOdeDtheta=fnmodelDtheta,
    thetaLowerBound=c(0,0,0),
    thetaUpperBound=c(Inf,Inf,Inf)
)

MagiPosterior(yInput, xlatentTest, theta = c(0.2, 0.2, 3), sigma = c(0.05, 0.1),
              list(curCovV, curCovR), fnmodel)

---

**MagiSolver**  
**MAnifold-constrained Gaussian process Inference (MA GI)**

**Description**

Core function of the MAGI method for inferring the parameters and trajectories of dynamic systems governed by ordinary differential equations. See vignette for detailed usage examples.

**Usage**

MagiSolver(y, odeModel, tvec, control = list())

**Arguments**

- `y`: data matrix of observations
- `odeModel`: list of ODE functions and inputs. See details.
- `tvec`: vector of discretization time points corresponding to rows of `y`. If missing, MagiSolver will use the column named ‘time’ in `y`.

**Details**

The data matrix `y` has a column for each system component, and optionally a column ‘time’ with the discretization time points. If the column ‘time’ is not provided in `y`, a vector of time points must be provided via the `tvec` argument. The rows of `y` correspond to the discretization set \( I \) at which the GP is constrained to the derivatives of the ODE system. To set the desired discretization level for
inference, use `setDiscretization` to prepare the data matrix for input into `MagiSolver`. Missing observations are indicated with NA or NaN.

The list `odeModel` is used for specification of the ODE system and its parameters. It must include five elements:

- `fOde` function that computes the ODEs, specified with the form $f(\theta,x,t)$. See examples.
- `fOdeDx` function that computes the gradients of the ODEs with respect to the system components. See examples.
- `fOdeDtheta` function that computes the gradients of the ODEs with respect to the parameters $\theta$. See examples.
- `thetaLowerBound` a vector indicating the lower bounds of each parameter in $\theta$.
- `thetaUpperBound` a vector indicating the upper bounds of each parameter in $\theta$.

Additional control variables can be supplied to `MagiSolver` via the optional list `control`, which may include the following:

- `sigma` a vector of noise levels (observation noise standard deviations) $\sigma$ for each component, at which to initialize MCMC sampling. By default, `MagiSolver` computes starting values for `sigma` via Gaussian process (GP) smoothing. If the noise levels are known, specify `sigma` together with `useFixedSigma = TRUE`.
- `phi` a matrix of GP hyper-parameters for each component, with two rows for `phi[1]` and `phi[2]` and a column for each system component. By default, `MagiSolver` estimates `phi` via an optimization routine.
- `theta` a vector of starting values for the parameters $\theta$, at which to initialize MCMC sampling. By default, `MagiSolver` uses an optimization routine to obtain starting values.
- `xInit` a matrix of values for the system trajectories of the same dimension as $y$, at which to initialize MCMC sampling. Default is linear interpolation between the observed (non-missing) values of $y$ and an optimization routine for entirely unobserved components of $y$.
- `mu` a matrix of values for the mean function of the GP prior, of the same dimension as $y$. Default is a zero mean function.
- `dotmu` a matrix of values for the derivatives of the GP prior mean function, of the same dimension as $y$. Default is zero.
- `priorTemperature` the tempering factor by which to divide the contribution of the GP prior, to control the influence of the GP prior relative to the likelihood. Default is the total number of observations divided by the total number of discretization points.
- `niterHmc` MCMC sampling from the posterior is carried out via Hamiltonian Monte Carlo (HMC). `niterHmc` specifies the number of HMC iterations to run. Default is 20000 HMC iterations.
- `nstepsHmc` the number of leapfrog steps per HMC iteration. Default is 200.
- `burninRatio` the proportion of HMC iterations to be discarded as burn-in. Default is 0.5, which discards the first half of the MCMC samples.
- `stepSizeFactor` initial leapfrog step size factor for HMC. Default is 0.01, and the leapfrog step size is automatically tuned during burn-in to achieve an acceptance rate between 60-90%.
- `bandSize` a band matrix approximation is used to speed up matrix operations, with default band size 20. Can be increased if `MagiSolver` returns an error indicating numerical instability.
- `useFixedSigma` logical, set to TRUE if `sigma` is known. If `useFixedSigma=TRUE`, the known values of $\sigma$ must be supplied via the `sigma` control variable.
Value

MagiSolver returns a list with the following elements:

theta  matrix of MCMC samples for the system parameters \( \theta \), after burn-in.
xsampled  array of MCMC samples for the system trajectories at each discretization time point, after burn-in.
sigma  matrix of MCMC samples for the observation noise SDs \( \sigma \), after burn-in.
phi  matrix of estimated GP hyper-parameters, one column for each system component.
lp  vector of log-posterior values at each MCMC iteration, after burn-in.

References


Examples

# Setting up the Fitzhugh-Nagumo system equations, see vignette for details
# ODE system
fnmodelODE <- function(theta,x,t) {
  V <- x[,1]
  R <- x[,2]

  result <- array(0, c(nrow(x),ncol(x)))

  result
}

# Gradient with respect to system components
fnmodelDx <- function(theta,x,t) {
  resultDx <- array(0, c(nrow(x), ncol(x), ncol(x)))
  V = x[,1]

  resultDx[,1,1] = theta[3] * (1 - V^2)
  resultDx[,2,1] = theta[3]

  resultDx[,1,2] = (-1.0 / theta[3])
  resultDx[,2,2] = ( -1.0*theta[2]/theta[3] )

  resultDx
}

# Gradient with respect to parameters theta
fnmodelDtheta <- function(theta,x,t) {
  resultDtheta <- array(0, c(nrow(x), length(theta), ncol(x)))
  V = x[,1]
\[ R = x[,2] \]

\[
\text{resultDtheta}[3,1] = V - V^3 / 3.0 + R
\]

\[
\text{resultDtheta}[1,2] = 1.0 / \theta[3]
\]

\[
\text{resultDtheta}[2,2] = -R / \theta[3]
\]

\[
\]

\[
\text{resultDtheta}
\]

# Create odeModel list

\[
\text{fnmodel} \leftarrow \text{list(}
\begin{array}{l}
\text{fOde=fnmodelODE}, \\
\text{fOdeDx=fnmodelDx}, \\
\text{fOdeDtheta=fnmodelDtheta,} \\
\text{thetaLowerBound=c(0,0,0),} \\
\text{thetaUpperBound=c(Inf,Inf,Inf)}
\end{array}
\text{)}
\]

# Example noisy data observed from the FN system

\[
\text{tvec} \leftarrow \text{seq}(0, 20, \text{by}=0.5)
\]

\[
V \leftarrow c(-1.16, -0.18, 1.57, 1.99, 1.95, 1.85, 1.49, 1.58, 1.47, 0.96, \\
0.75, 0.22, -1.34, -1.72, -2.11, -1.56, -1.51, -1.29, -1.22, \\
-0.36, 1.78, 2.36, 1.78, 1.8, 1.76, 1.4, 1.02, 1.28, 1.21, 0.04, \\
-1.35, -2.1, -1.9, -1.49, -1.55, -1.35, -0.98, -0.34, 1.9, 1.99, 1.84)
\]

\[
R \leftarrow c(0.94, 1.22, 0.89, 0.13, 0.4, 0.04, -0.21, -0.65, -0.31, -0.65, \\
-0.72, -1.26, -0.56, -0.44, -0.63, 0.21, 1.07, 0.57, 0.85, 1.04, \\
0.92, 0.47, 0.27, 0.16, -0.41, -0.6, -0.58, -0.54, -0.59, -1.15, \\
-1.23, -0.37, -0.06, 0.16, 0.43, 0.73, 0.7, 1.37, 1.1, 0.85, 0.23)
\]

# Set discretization for a total of 161 time points

\[
\text{yobs} \leftarrow \text{data.frame(time=tvec, V=V, R=R)}
\]

\[
\text{yinput} \leftarrow \text{setDiscretization(yobs, level=2)}
\]

# Call MagiSolver

# short sampler run for demo only, more iterations needed for convergence

\[
\text{MagiSolver(yinput, fnmodel, control = list(nstepsHmc=5, niterHmc = 402))}
\]

# full run with 20000 HMC iterations

\[
\text{result} \leftarrow \text{MagiSolver(yinput, fnmodel, control = list(nstepsHmc=100))}
\]

---

**setDiscretization**

**Set discretization level**

Description

Set the discretization level of a data matrix for input to MagiSolver, by inserting time points where the GP is constrained to the derivatives of the ODE system.
Usage

setDiscretization(dat, level, by)

Arguments

dat   data matrix. Must include a column with name ‘time’.
level   discretization level (a positive integer). \(2^\text{level} - 1\) equally-spaced points will be inserted between existing data points in dat.
by   discretization interval. As an alternative to level, equally-spaced spaced time points will be inserted with interval by between successive points.

Details

Specify the desired discretization using level or by.

Value

Returns a data matrix with the same columns as dat, with rows added for the inserted discretization time points.

Examples

dat <- data.frame(time = 0:10, x = rnorm(11))
setDiscretization(dat, level = 2)
setDiscretization(dat, by = 0.2)

testDynamicalModel  Test dynamic system model specification

Description

Given functions for the ODE and its gradients (with respect to the system components and parameters), verify the correctness of the gradients using numerical differentiation.

Usage

testDynamicalModel(modelODE, modelDx, modelDtheta, modelName, x, theta, tvec)

Arguments

modelODE   function that computes the ODEs, specified with the form \(f(\theta, x, t)\). See examples.
modelDx   function that computes the gradients of the ODEs with respect to the system components. See examples.
modelDtheta   function that computes the gradients of the ODEs with respect to the parameters \(\theta\). See examples.
modelName string giving a name for the model
x data matrix of system values, one column for each component, at which to test the gradients
theta vector of parameter values for \( \theta \), at which to test the gradients
tvec vector of time points corresponding to the rows of \( x \)

Details

Calls `test_that` to test equality of the analytic and numeric gradients.

Value

A list with elements `testDx` and `testDtheta`, each with value `TRUE` if the corresponding gradient check passed and `FALSE` if not.

Examples

```r
# ODE system for Fitzhugh-Nagumo equations
fnmodelODE <- function(theta,x,t) {
  V <- x[,1]
  R <- x[,2]

  result <- array(0, c(nrow(x),ncol(x)))

  result
}

# Gradient with respect to system components
fnmodelDx <- function(theta,x,t) {
  resultDx <- array(0, c(nrow(x), ncol(x)))
  V = x[,1]

  resultDx[,1,1] = theta[3] * (1 - V^2)
  resultDx[,2,1] = theta[3]

  resultDx[,1,2] = (-1.0 / theta[3])
  resultDx[,2,2] = ( -1.0*theta[2]/theta[3] )

  resultDx
}

# Gradient with respect to parameters theta
fnmodelDtheta <- function(theta,x,t) {
  resultDtheta <- array(0, c(nrow(x), length(theta), ncol(x)))
  V = x[,1]
  R = x[,2]

  resultDtheta[,3,1] = V - V^3 / 3.0 + R
```
resultDtheta[,1,2] = 1.0 / theta[3]
resultDtheta[,2,2] = -R / theta[3]

resultDtheta

# Example incorrect gradient with respect to parameters theta
fnmodelDthetaWrong <- function(theta,x,t) {
  resultDtheta <- array(0, c(nrow(x), length(theta), ncol(x)))
  V = x[,1]
  R = x[,2]

  resultDtheta[,3,1] = V - V^3 / 3.0 - R
  resultDtheta[,1,2] = 1.0 / theta[3]
  resultDtheta[,2,2] = -R / theta[3]

  resultDtheta
}

# Sample data for testing gradient correctness
tvec <- seq(0, 20, by = 0.5)
V <- c(-1.16, -0.18, 1.57, 1.99, 1.95, 1.85, 1.49, 1.58, 1.47, 0.96,
      0.75, 0.22, -1.34, -1.72, -2.11, -1.56, -1.51, -1.29, -1.22,
      -0.36, 1.78, 2.36, 1.78, 1.8, 1.76, 1.4, 1.02, 1.28, 1.21, 0.04,
      -1.35, -2.1, -1.9, -1.49, -1.55, -1.35, -0.98, -0.34, 1.9, 1.99, 1.84)
R <- c(0.94, 1.22, 0.89, 0.13, 0.4, 0.04, -0.21, -0.65, -0.31, -0.65,
      -0.72, -1.26, -0.56, -0.44, -0.63, 0.21, 1.07, 0.57, 0.85, 1.04,
      0.92, 0.47, 0.27, 0.16, -0.41, -0.6, -0.58, -0.54, -0.59, -1.15,
      -1.23, -0.37, -0.06, 0.16, 0.43, 0.73, 0.7, 1.37, 1.1, 0.85, 0.23)

# Correct gradients
testDynamicalModel(fnmodelODE, fnmodelDx, fnmodelDtheta,
                     "FN equations", cbind(V,R), c(.5, .6, 2), tvec)

# Incorrect theta gradient (test fails)
testDynamicalModel(fnmodelODE, fnmodelDx, fnmodelDthetaWrong,
                     "FN equations", cbind(V,R), c(.5, .6, 2), tvec)
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