

# Package ‘rwavelet’

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**Type** Package

**Title** Wavelet Analysis

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**Author** F. Navarro and C. Chesneau

**Maintainer** Navarro Fabien <fnavarro@math.cnrs.fr>

**Description** Perform wavelet analysis (orthogonal,translation invariant, tensorial, 1-2-3d transforms, thresholding, block thresholding, linear,...) with applications to data compression or denoising/regression. The core of the code is a port of 'MATLAB' Wavelab toolbox written by D. Donoho, A. Maleki and M. Shahram (<<https://statweb.stanford.edu/~wavelab/>>).

**URL** <https://github.com/fabnavarro/rwavelet>

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---

`aconv`                      *Convolution tool for two-scale transform*

---

### Description

Filtering by periodic convolution of `x` with the time-reverse of `f`.

### Usage

```
aconv(f, x)
```

### Arguments

<code>f</code>	filter.
<code>x</code>	1-d signal.

### Value

`y` filtered result.

### See Also

[iconvv](#), [UpDyadHi](#), [UpDyadLo](#), [DownDyadHi](#), [DownDyadLo](#).

### Examples

```
qmf <- MakeONFilter('Haar')
x <- MakeSignal('HeaviSine',2^3)
aconv(qmf,x)
```

---

**BlockThresh***1d wavelet Block Thresholding*

---

**Description**

This function is used for thresholding coefficients by group (or block) according to the hard or soft thresholding rule.

**Usage**

```
BlockThresh(wc, j0, hatsigma, L, qmf, thresh = "hard")
```

**Arguments**

wc	wavelet coefficients.
j0	coarsest decomposition scale.
hatsigma	estimator of noise variance.
L	Block size (n mod L must be 0).
qmf	Orthonormal quadrature mirror filter.
thresh	'hard' or 'soft'.

**Value**

wcb wavelet coefficient estimators.

**See Also**

[invblock\\_partition](#), [invblock\\_partition](#).

**Examples**

```
n <- 64
x <- MakeSignal('Ramp', n)
sig <- 0.01
y <- x + rnorm(n, sd=sig)
j0 <- 1
qmf <- MakeONFilter('Daubechies', 8)
wc <- FWT_PO(y, j0, qmf)
L <- 2
wcb <- BlockThresh(wc, j0, sig, L, qmf, "hard")
```

---

block_partition	<i>Construct 1d block partition</i>
-----------------	-------------------------------------

---

**Description**

This function is used to group the coefficients into blocks (or groups) of size L.

**Usage**

```
block_partition(x, L)
```

**Arguments**

x	(noisy) wc at a given scale.
L	block size.

**Value**

out partition of coefficients by block.

**See Also**

[invblock\\_partition](#), [BlockThresh](#).

**Examples**

```
x <- MakeSignal('Ramp', 8)
j0 <- 0
qmf <- MakeONFilter('Haar')
wc <- FWT_PO(x, j0, qmf)
L <- 2
wcb <- block_partition(wc, L)
```

---

block_partition2d	<i>Construct 2d block partition</i>
-------------------	-------------------------------------

---

**Description**

Group the coefficients into blocks (or groups) of size L.

**Usage**

```
block_partition2d(x, L)
```

**Arguments**

x (noisy) wc at a given scale.  
L block size.

**Value**

out partition of coefficients by block.

**See Also**

[inblock\\_partition2d](#)

**Examples**

```
x <- matrix(rnorm(2^2), ncol=2)
j0 <- 0
qmf <- MakeONFilter('Haar')
wc <- FWT2_PO(x, j0, qmf)
L <- 2
wcb <- block_partition2d(wc, L)
```

---

CircularShift

*Circular Shifting of a matrix/image*

---

**Description**

Pixels that get shifted off one side of the image are put back on the other side.

**Usage**

```
CircularShift(matrix, colshift = 0, rowshift = 0)
```

**Arguments**

matrix 2-d signal (matrix).  
colshift column shift index (integer).  
rowshift row shift index (integer).

**Value**

result 2-d shifted signal.

**See Also**

[FWT2\\_TI](#), [IWT2\\_TI](#).

**Examples**

```
A <- matrix(1:4, ncol=2, byrow=TRUE)
CircularShift(A, 0, -1)
```

---

**cubelength***Find length and dyadic length of square array*

---

**Description**

3d counterpart of Donoho's quadlength utilized by the 2d pair. Original matlab code Vicki Yang and Brani Vidakovic.

**Usage**

```
cubelength(x)
```

**Arguments**

x                    3-d array; dim(n,n,n),  $n = 2^J$  (hopefully).

**Value**

n length(x).

J least power of two greater than n.

**See Also**

[FWT3\\_PO](#), [IWT3\\_PO](#).

**Examples**

```
cubelength(array(1:3, c(2,2,2)))
```

---

**CVlinear***2-Fold Cross Validation for linear estimator*

---

**Description**

Selection of the number of wavelet coefficients to be maintained by the cross validation method proposed by Nason in the case of threshold selection. This method is adapted here to select among linear estimators.

**Usage**

```
CVlinear(Y, L, qmf, D, wc)
```

**Arguments**

Y	Noisy observations.
L	Level of coarsest scale.
qmf	Orthonormal quadrature mirror filter.
D	Dimension vector of the models considered.
wc	1-d wavelet coefficients.

**Value**

CritCV Cross validation criteria.  
 hat\_f\_m\_2FCV

**References**

- Nason, G. P. (1996). Wavelet shrinkage using cross-validation. *Journal of the Royal Statistical Society: Series B*, 58(2), 463–479.
- Navarro, F. and Saumard, A. (2017). Slope heuristics and V-Fold model selection in heteroscedastic regression using strongly localized bases. *ESAIM: Probability and Statistics*, 21, 412–451.

---

DownDyadHi	<i>Hi-Pass Downsampling operator (periodized)</i>
------------	---

---

**Description**

Hi-Pass Downsampling operator (periodized)

**Usage**

```
DownDyadHi(x, qmf)
```

**Arguments**

x	1-d signal at fine scale.
qmf	filter.

**Value**

y 1-d signal at coarse scale.

**See Also**

[DownDyadLo](#), [UpDyadHi](#), [UpDyadLo](#), [FWT\\_PO](#), [iconvv](#).

**Examples**

```
qmf <- MakeONFilter('Haar')
x <- MakeSignal('HeaviSine', 2^3)
DownDyadHi(x, qmf)
```



---

DownDyadLo	<i>Lo-Pass Downsampling operator (periodized)</i>
------------	---

---

**Description**

Lo-Pass Downsampling operator (periodized)

**Usage**

```
DownDyadLo(x, qmf)
```

**Arguments**

x	1-d signal at fine scale.
qmf	filter.

**Value**

d 1-d signal at coarse scale.

**See Also**

[DownDyadHi](#), [UpDyadHi](#), [UpDyadLo](#), [FWT\\_PO](#), [aconv](#).

**Examples**

```
qmf <- MakeONFilter('Haar')
x <- MakeSignal('HeaviSine', 2^3)
DownDyadLo(x, qmf)
```

---

dyad	<i>Index entire j-th dyad of 1-d wavelet xform</i>
------	--

---

**Description**

Index entire j-th dyad of 1-d wavelet xform

**Usage**

```
dyad(j)
```

**Arguments**

j	integer.
---	----------

**Value**

ix list of all indices of wavelet coeffs at j-th level.

**Examples**

```
dyad(0)
```

---

dyadlength	<i>Find length and dyadic length of array</i>
------------	---

---

**Description**

Find length and dyadic length of array

**Usage**

```
dyadlength(x)
```

**Arguments**

x                    array of length  $n = 2^J$  (hopefully).

**Value**

n length(x).

J least power of two greater than n.

**See Also**

[quadlength](#), [dyad](#)

**Examples**

```
x <- MakeSignal('Ramp', 8)
dyadlength(x)
```

---

FTWT2_PO	<i>2-d tensor wavelet transform (periodized, orthogonal).</i>
----------	---

---

### Description

A two-dimensional Wavelet Transform is computed for the array `x`. `qmf` filter may be obtained from [MakeONFilter](#). To reconstruct, use [ITWT2\\_PO](#).

### Usage

```
FTWT2_PO(x, L, qmf)
```

### Arguments

<code>x</code>	2-d image (n by n array, n dyadic).
<code>L</code>	coarse level.
<code>qmf</code>	quadrature mirror filter.

### Value

`wc` 2-d wavelet transform.

### See Also

[ITWT2\\_PO](#), [MakeONFilter](#).

### Examples

```
qmf <- MakeONFilter('Daubechies', 10)
L <- 0
x <- matrix(rnorm(2^2), ncol=2)
wc <- FTWT2_PO(x, L, qmf)
```

---

FWT2_PO	<i>2-d MRA Forwad Wavelet Transform (periodized, orthogonal)</i>
---------	--

---

### Description

A two-dimensional wavelet transform is computed for the array `x`. `qmf` filter may be obtained from [MakeONFilter](#). To reconstruct, use [IWT2\\_PO](#).

### Usage

```
FWT2_PO(x, L, qmf)
```

**Arguments**

x                    2-d image (n by n array, n dyadic).  
 L                    coarse level.  
 qmf                  quadrature mirror filter.

**Value**

wc 2-d wavelet transform.

**See Also**

[IWT2\\_PO](#), [MakeONFilter](#).

**Examples**

```
qmf <- MakeONFilter('Daubechies', 10)
L <- 3
x <- matrix(rnorm(128^2), ncol=128)
wc <- FWT2_PO(x, L, qmf)
```

---

FWT2\_TI

*2-d Translation Invariant Forward Wavelet Transform*


---

**Description**

1. qmf filter may be obtained from [MakeONFilter](#). 2. usually,  $\text{length}(\text{qmf}) < 2^{(L+1)}$ . 3. To reconstruct use [IWT\\_TI](#).

**Usage**

```
FWT2_TI(x, L, qmf)
```

**Arguments**

x                    2-d image (n by n real array, n dyadic).  
 L                    degree of coarsest scale.  
 qmf                  orthonormal quadrature mirror filter.

**Value**

TIWT translation-invariant wavelet transform table,  $(3(J-L)+1)n$  by  $n$ .

**Examples**

```
x <- matrix(rnorm(2^2), ncol=2)
L <- 0
qmf <- MakeONFilter('Haar')
TIWT <- FWT2_TI(x, L, qmf)
```

---

FWT3_PO	<i>3-d MRA Forward Wavelet Transform (periodized, orthogonal)</i>
---------	---

---

### Description

A three-dimensional wavelet transform is computed for the array `x`. `qmf` filter may be obtained from [MakeONFilter](#). To reconstruct, use [IWT3\\_PO](#).

### Usage

```
FWT3_PO(x, L, qmf)
```

### Arguments

<code>x</code>	3-d array (n by n by n array, n dyadic).
<code>L</code>	coarse level.
<code>qmf</code>	quadrature mirror filter.

### Details

3-D counterpart of Donoho's `FWT2_PO`, original matlab code Vicki Yang and Brani Vidakovic.

### Value

wc 3-d wavelet transform.

### See Also

[IWT3\\_PO](#), [MakeONFilter](#).

### Examples

```
qmf <- MakeONFilter('Daubechies', 10)
L <- 3
x <- array(rnorm(32^3), c(32,32,32))
wc <- FWT3_PO(x, L, qmf)
```

---

FWT\_PO *Forward Wavelet Transform (periodized, orthogonal)*

---

### Description

1. qmf filter may be obtained from [MakeONFilter](#). 2. usually,  $\text{length}(\text{qmf}) < 2^{(L+1)}$ . 3. To reconstruct use [IWT\\_PO](#).

### Usage

```
FWT_PO(x, L, qmf)
```

### Arguments

x	1-d signal; $\text{length}(x) = 2^J$ .
L	Coarsest Level of $V_0$ ; $L \ll J$ .
qmf	quadrature mirror filter (orthonormal).

### Value

wc 1-d wavelet transform of x.

### See Also

[IWT\\_PO](#), [MakeONFilter](#).

### Examples

```
x <- MakeSignal('Ramp', 8)
L <- 0
qmf <- MakeONFilter('Haar')
wc <- FWT_PO(x, L, qmf)
```

---

FWT\_TI *Translation Invariant Forward Wavelet Transform*

---

### Description

1. qmf filter may be obtained from [MakeONFilter](#). 2. usually,  $\text{length}(\text{qmf}) < 2^{(L+1)}$ . 3. To reconstruct use [IWT\\_TI](#).

### Usage

```
FWT_TI(x, L, qmf)
```

**Arguments**

x	array of dyadic length $n=2^J$ .
L	degree of coarsest scale.
qmf	orthonormal quadrature mirror filter.

**Value**

TIWT stationary wavelet transform table.

**See Also**

[IWT\\_TI](#), [MakeONFilter](#).

**Examples**

```
x <- MakeSignal('Ramp', 8)
L <- 0
qmf <- MakeONFilter('Haar')
TIWT <- FWT_TI(x, L, qmf)
```

---

GWN

*Generation of Gaussian White Noise*

---

**Description**

Generation of Gaussian White Noise

**Usage**

```
GWN(n, sigma)
```

**Arguments**

n	sample size.
sigma	standard deviation.

**Value**

epsilon resulting noise.

**Examples**

```
GWN(10, 0.1)
```

---

HardThresh	<i>Apply Hard Threshold</i>
------------	-----------------------------

---

**Description**

Apply Hard Threshold

**Usage**

```
HardThresh(y, t)
```

**Arguments**

y	Noisy Data.
t	Threshold.

**Value**

x filtered result ( $y \cdot 1_{|y|>t}$ ).

**See Also**

[SoftThresh](#).

**Examples**

```
f <- MakeSignal('HeaviSine',2^3)
qmf <- MakeONFilter('Daubechies', 10)
L <- 0
wc <- FWT_PO(f, L, qmf)
thr <- 2
wct <- HardThresh(wc, thr)
fhard <- IWT_PO(wct, L, qmf)
```

---

iconvv	<i>Convolution tool for two-scale transform</i>
--------	---

---

**Description**

Filtering by periodic convolution of x with f.

**Usage**

```
iconvv(f, x)
```



**Arguments**

f                    filter.  
x                    1-d signal.

**Value**

y filtered result.

**See Also**

[aconv](#), [UpDyadHi](#), [UpDyadLo](#), [DownDyadHi](#), [DownDyadLo](#).

**Examples**

```
qmf <- MakeONFilter('Haar')  
x <- MakeSignal('HeaviSine', 2^3)  
iconvv(qmf, x)
```

---

invblock\_partition      *Inversion of the 1d block partition*

---

**Description**

Inversion of the 1d block partition

**Usage**

```
invblock_partition(x, n, L)
```

**Arguments**

x                    partition of coefficients by block.  
n                    scale.  
L                    block size.

**See Also**

[block\\_partition](#), [BlockThresh](#).

**Examples**

```
n <- 8  
x <- MakeSignal('Ramp', n)  
j0 <- 1  
qmf <- MakeONFilter('Haar')  
wc <- FWT_PO(x, j0, qmf)  
L <- 2  
wcb <- block_partition(wc, L)  
wcib <- invblock_partition(wcb, n, L)
```

---

invblock\_partition2d *Inversion of the 2d block partition*

---

### Description

Inversion of the 2d block partition

### Usage

```
invblock_partition2d(x, n, L)
```

### Arguments

x	partition of coefficients by block.
n	scale.
L	block size.

### Value

out coefficients.

### See Also

[block\\_partition2d](#)

### Examples

```
n <- 2
x <- matrix(rnorm(n^2), ncol=2)
j0 <- 0
qmf <- MakeONFilter('Haar')
wc <- FWT2_PO(x, j0, qmf)
L <- 2
wcb <- block_partition2d(wc, L)
wcib <- invblock_partition2d(wcb, n, L)
```

---

ITWT2\_PO

*Inverse 2-d Tensor Wavelet Transform (periodized, orthogonal)*

---

### Description

If `wc` is the result of a forward 2d wavelet transform, with `wc <- FWT2_PO(x, L, qmf)`, then `x <- ITWT2_PO(wc, L, qmf)` reconstructs `x` exactly. `qmf` is a nice `qmf`, e.g. one made by [MakeONFilter](#).

### Usage

```
ITWT2_PO(wc, L, qmf)
```

**Arguments**

wc                    2-d wavelet transform (n by n array, n dyadic).  
 L                     coarse level.  
 qmf                    quadrature mirror filter.

**Value**

x 2-d signal reconstructed from wc.

**See Also**

[FTWT2\\_PO](#), [MakeONFilter](#).

**Examples**

```

qmf <- MakeONFilter('Daubechies', 10)
L <- 0
x <- matrix(rnorm(2^2), ncol=2)
wc <- FTWT2_PO(x, L, qmf)
xr <- IWT2_PO(wc,L,qmf)

```

---

IWT2\_PO

---

*Inverse 2-d MRA Wavelet Transform (periodized, orthogonal)*


---

**Description**

If wc is the result of a forward 2d wavelet transform, with `wc <- FWT2_PO(x,L,qmf)`. then `x <- IWT2_PO(wc,L,qmf)` reconstructs x exactly qmf is a nice qmf, e.g. one made by [MakeONFilter](#).

**Usage**

```
IWT2_PO(wc, L, qmf)
```

**Arguments**

wc                    2-d wavelet transform (n by n array, n dyadic).  
 L                     coarse level.  
 qmf                    quadrature mirror filter.

**Value**

x 2-d signal reconstructed from wc.

**See Also**

[FWT2\\_PO](#), [MakeONFilter](#).

**Examples**

```
qmf <- MakeONFilter('Daubechies', 10)
L <- 3
x <- matrix(rnorm(128^2), ncol=128)
wc <- FWT2_PO(x, L, qmf)
xr <- IWT2_PO(wc, L, qmf)
```

---

**IWT2\_TI***Invert 2-d Translation Invariant Wavelet Transform*

---

**Description**

Invert 2-d Translation Invariant Wavelet Transform

**Usage**

```
IWT2_TI(tiw, L, qmf)
```

**Arguments**

tiwt	translation-invariant wavelet transform table, $(3(J-L)+1)n$ by $n$ .
L	degree of coarsest scale.
qmf	orthonormal quadrature mirror filter.

**Value**

$x$  2-d image reconstructed from translation-invariant transform TIWT.

**Examples**

```
x <- matrix(rnorm(2^2), ncol=2)
L <- 0
qmf <- MakeONFilter('Haar')
TIWT <- FWT2_TI(x, L, qmf)
xr <- IWT2_TI(TIWT, L, qmf)
```

---

**IWT3\_PO***Inverse 3-d MRA Wavelet Transform (periodized, orthogonal)*

---

**Description**

If `wc` is the result of a forward 3-d wavelet transform, with `wc <- FWT3_PO(x, L, qmf)`. then `x <- IWT3_PO(wc, L, qmf)` reconstructs `x` exactly `qmf` is a nice `qmf`, e.g. one made by [MakeONFilter](#).

**Usage**

```
IWT3_PO(wc, L, qmf)
```

**Arguments**

<code>wc</code>	3-d wavelet transform (n by n by n array, n dyadic).
<code>L</code>	coarse level.
<code>qmf</code>	quadrature mirror filter.

**Details**

3-d counterpart of Donoho's IWT2\_PO, original matlab code by Vicki Yang and Brani Vidakovic.

**Value**

`x` 3-d signal reconstructed from `wc`.

**See Also**

[FWT3\\_PO](#), [MakeONFilter](#).

**Examples**

```
qmf <- MakeONFilter('Daubechies', 10)
L <- 3
x <- array(rnorm(32^3), c(32, 32, 32))
wc <- FWT3_PO(x, L, qmf)
xr <- IWT3_PO(wc, L, qmf)
```

---

IWT\_PO *Inverse Wavelet Transform (periodized, orthogonal)*

---

### Description

Suppose  $wc \leftarrow \text{FWT\_PO}(x, L, \text{qmf})$  where  $\text{qmf}$  is an orthonormal quad. mirror filter, e.g. one made by [MakeONFilter](#). Then  $x$  can be reconstructed by  $x \leftarrow \text{IWT\_PO}(wc, L, \text{qmf})$ .

### Usage

`IWT_PO(wc, L, qmf)`

### Arguments

`wc`                    1-d wavelet transform:  $\text{length}(wc) = 2^J$ .  
`L`                      Coarsest scale ( $2^{(-L)} = \text{scale of } V_0$ );  $L \ll J$ .  
`qmf`                    quadrature mirror filter (orthonormal).

### Value

$x$  1-d signal reconstructed from  $wc$ .

### See Also

[FWT\\_PO](#), [MakeONFilter](#).

### Examples

```
x <- MakeSignal('Ramp', 8)
L <- 0
qmf <- MakeONFilter('Haar')
wc <- FWT_PO(x, L, qmf)
xr <- IWT_PO(wc, L, qmf)
```

---

IWT\_TI *Invert Translation Invariant Wavelet Transform*

---

### Description

Invert Translation Invariant Wavelet Transform

### Usage

`IWT_TI(pkt, qmf)`

**Arguments**

pkt translation-invariant wavelet transform table (TIWT).  
qmf orthonormal quadrature mirror filter.

**Value**

x 1-d signal reconstructed from translation-invariant transform TIWT.

**See Also**

[FWT\\_TI](#), [MakeONFilter](#).

**Examples**

```
x <- MakeSignal('Ramp', 8)
L <- 0
qmf <- MakeONFilter('Haar')
TIWT <- FWT_TI(x, L, qmf)
xr <- IWT_TI(TIWT, qmf)
```

---

JSThresh

*Apply James-Stein Threshold*

---

**Description**

(also called the nonnegative garrote)

**Usage**

```
JSThresh(y, t)
```

**Arguments**

y Noisy Data.  
t Threshold.

**Value**

x filtered result.

**See Also**

[HardThresh](#), [SoftThresh](#)

**Examples**

```
f <- MakeSignal('HeaviSine', 2^3)
qmf <- MakeONFilter('Daubechies', 10)
L <- 0
wc <- FWT_PO(f, L, qmf)
thr <- 2
wct <- JSThresh(wc, thr)
fsoft <- IWT_PO(wct, L, qmf)
```

---

lshift	<i>Circular left shift of 1-d signal</i>
--------	--

---

**Description**

Circular left shift of 1-d signal

**Usage**

```
lshift(a)
```

**Arguments**

a                    1-d signal.

**Value**

1 1-d signal  $l(i) = x(i+1)$  except  $l(n) = x(1)$ .

**Examples**

```
x <- MakeSignal('HeaviSine', 2^3)
lshift(x)
```

---

MAD	<i>Median Absolute Deviation</i>
-----	----------------------------------

---

**Description**

Compute the median absolute deviation.

**Usage**

```
MAD(x)
```

**Arguments**

x                    1-d signal.



**Examples**

```
x <- c(1, 1, 2, 2, 4, 6, 9)
MAD(x)
```

---

 MakeONFilter

*Generate Orthonormal QMF Filter for Wavelet Transform*


---

**Description**

The Haar filter (which could be considered a Daubechies-2) was the first wavelet, though not called as such, and is discontinuous.

**Usage**

```
MakeONFilter(Type, Par)
```

**Arguments**

Type	string, 'Haar', 'Beylkin', 'Coiflet', 'Daubechies', 'Symmlet', 'Vaidyanathan', 'Battle'.
Par	integer, it is a parameter related to the support and vanishing moments of the wavelets, explained below for each wavelet.

**Details**

The Beylkin filter places roots for the frequency response function close to the Nyquist frequency on the real axis.

The Coiflet filters are designed to give both the mother and father wavelets  $2 \cdot \text{Par}$  vanishing moments; here Par may be one of 1,2,3,4 or 5.

The Daubechies filters are minimal phase filters that generate wavelets which have a minimal support for a given number of vanishing moments. They are indexed by their length, Par, which may be one of 4,6,8,10,12,14,16,18 or 20. The number of vanishing moments is  $\text{par}/2$ .

Symmlets are also wavelets within a minimum size support for a given number of vanishing moments, but they are as symmetrical as possible, as opposed to the Daubechies filters which are highly asymmetrical. They are indexed by Par, which specifies the number of vanishing moments and is equal to half the size of the support. It ranges from 4 to 10.

The Vaidyanathan filter gives an exact reconstruction, but does not satisfy any moment condition. The filter has been optimized for speech coding.

The Battle-Lemarie filter generate spline orthogonal wavelet basis. The parameter Par gives the degree of the spline. The number of vanishing moments is  $\text{Par}+1$ .

**Value**

qmf quadrature mirror filter.

**See Also**

[FWT\\_PO](#), [IWT\\_PO](#), [FWT2\\_PO](#), [IWT2\\_PO](#).

**Examples**

```
Type <- 'Coiflet'
Par <- 1
qmf <- MakeONFilter(Type, Par)
```

---

MakeSignal

*Make artificial signal*

---

**Description**

Make artificial signal

**Usage**

```
MakeSignal(name, n)
```

**Arguments**

name	string, 'HeaviSine', 'Bumps', 'Blocks', 'Doppler', 'Ramp', 'Cusp', 'Sing', 'Hi-Sine', 'LoSine', 'LinChirp', 'TwoChirp', 'QuadChirp', 'MishMash', 'Werner-Sorrows' (Heisenberg), 'Leopold' (Kronecker), 'Riemann', 'HypChirps', 'LinChirps', 'Chirps', 'Gabor', 'sineoneoverx', 'Cusp2', 'SmoothCusp', 'Piece-Regular' (Piece-Wise Smooth), 'Piece-Polynomial' (Piece-Wise 3rd degree polynomial).
n	desired signal length.

**Value**

sig 1-d signal.

**See Also**

[FWT\\_PO](#), [IWT\\_PO](#), [FWT2\\_PO](#), [IWT2\\_PO](#).

**Examples**

```
name <- 'Cusp'
n <- 2^5
sig <- MakeSignal(name, n)
```

---

MakeSignalNewb	<i>Make artificial 1-d signal</i>
----------------	-----------------------------------

---

**Description**

Make artificial 1-d signal

**Usage**

```
MakeSignalNewb(name, n)
```

**Arguments**

name	string, 'Cusp', 'Step', 'Wave', 'Blip', 'Blocks', 'Bumps', 'HeaviSine', 'Doppler', 'Angles', 'Parabolas', 'Time Shifted Sine', 'Spikes', 'Corner'
n	desired signal length.

**Value**

sig 1-d signal.

**See Also**

[FWT\\_PO](#), [IWT\\_PO](#), [FWT2\\_PO](#), [IWT2\\_PO](#).

**Examples**

```
name <- 'Cusp'  
n <- 2^5  
sig <- MakeSignalNewb(name, n)
```

---

MinMaxThresh	<i>Minimax Thresholding</i>
--------------	-----------------------------

---

**Description**

Minimax Thresholding

**Usage**

```
MinMaxThresh(y)
```

**Arguments**

y	signal upon which to perform thresholding.
---	--

**Value**

x result.

**References**

D.L. Donoho and I.M. Johnstone (1994). Ideal spatial adaptation by wavelet shrinkage. *Biometrika*, 81(3), 425–455.

---

MirrorFilt	<i>Apply (-1)<sup>t</sup> modulation</i>
------------	--

---

**Description**

$h(t) = (-1)^{(t-1)} * x(t)$ ,  $1 \leq t \leq \text{length}(x)$

**Usage**

MirrorFilt(x)

**Arguments**

x                    1-d signal.

**Value**

h 1-d signal with DC frequency content shifted to Nyquist frequency

**See Also**

[DownDyadHi](#).

**Examples**

```
x <- MakeSignal('HeaviSine', 2^3)
h <- MirrorFilt(x)
```

---

MultiMAD	<i>Apply Shrinkage with level-dependent Noise level estimation</i>
----------	--

---

**Description**

Apply Shrinkage with level-dependent Noise level estimation

**Usage**

MultiMAD(wc, L)

**Arguments**

wc	Wavelet Transform of noisy sequence.
L	low-resolution cutoff for Wavelet Transform.

**Value**

ws result of applying VisuThresh to each wavelet level, after scaling so MAD of coefficient at each level = .6745

---

MultiSURE	<i>Apply Shrinkage to Wavelet Coefficients</i>
-----------	--

---

**Description**

SURE refers to Stein's Unbiased Risk Estimate.

**Usage**

MultiSURE(wc, L)

**Arguments**

wc	Wavelet Transform of noisy sequence with $N(0,1)$ noise.
L	low-frequency cutoff for Wavelet Transform.

**Value**

ws result of applying SUREThresh to each dyadic block.

---

 MultiVisu

*Apply Universal Thresholding to Wavelet Coefficients*


---

**Description**

Apply Universal Thresholding to Wavelet Coefficients

**Usage**

MultiVisu(wc, L)

**Arguments**

wc                    Wavelet Transform of noisy sequence with  $N(0,1)$  noise.  
 L                     low-frequency cutoff for Wavelet Transform

**Value**

x result of applying VisuThresh to each High Frequency Dyadic Block.

---

packet

*Packet table indexing*


---

**Description**

Packet table indexing

**Usage**

packet(d, b, n)

**Arguments**

d                     depth of splitting in packet decomposition.  
 b                     block index among  $2^d$  possibilities at depth d.  
 n                     length of signal.

**Value**

p linear indices of all coeff's in that block.

**Examples**

packet(1, 1, 8)

---

PlotSpikes	<i>Plot 1-d signal as baseline with series of spikes</i>
------------	--

---

**Description**

Plot 1-d signal as baseline with series of spikes

**Usage**

```
PlotSpikes(base, t, x, L, J)
```

**Arguments**

base	number, baseline level.
t	ordinate values.
x	1-d signal, specifies spike deflections from baseline.
L	level of coarsest scale.
J	least power of two greater than n.

**Value**

A plot of spikes on a baseline.

**See Also**

[PlotWaveCoeff](#).

**Examples**

```
## Not run:  
PlotSpikes(base, t, x, L, J)  
  
## End(Not run)
```

---

PlotWaveCoeff	<i>Spike-plot display of wavelet coefficients</i>
---------------	---

---

**Description**

Spike-plot display of wavelet coefficients

**Usage**

```
PlotWaveCoeff(wc, L, scal)
```

**Arguments**

`wc`                1-d wavelet transform.  
`L`                    level of coarsest scale.  
`scal`                scale factor (0 ==> autoscale).

**Value**

A display of wavelet coefficients (coarsest level NOT included) by level and position.

**See Also**

[FWT\\_PO](#), [IWT\\_PO](#), [PlotSpikes](#).

**Examples**

```

x <- MakeSignal('Ramp', 128)
qmf <- MakeONFilter('Daubechies', 10)
L <- 3
scal <- 1
wc <- FWT_PO(x, L, qmf)
PlotWaveCoeff(wc,L,scal)

```

---

quadlength

*Find length and dyadic length of square matrix*


---

**Description**

$h(t) = (-1)^{t-1} * x(t)$ ,  $1 \leq t \leq \text{length}(x)$

**Usage**

`quadlength(x)`

**Arguments**

`x`                    2-d image;  $\text{dim}(n,n)$ ,  $n = 2^J$  (hopefully).

**Value**

`n`  $\text{length}(x)$ .  
`J` least power of two greater than `n`.

**Examples**

```
quadlength(matrix(1:16,ncol=4))
```



---

RaphNMR

*Nuclear magnetic resonance (NMR) signal*

---

**Description**

A dataset containing a NMR signal.

**Usage**

```
data(RaphNMR)
```

**Format**

A numeric vector of length 1024.

**Source**

MRS Unit, VA Medical Center, San Francisco. Adrain Maudsley, Ph.D., Professor of Radiology. This NMR signal was obtained from Chris Raphael, then a postdoctoral fellow in the Department of Statistics at Stanford University who was working on Hidden Markov Models for restoring NMR Spectra.

---

repmat

*Replicate and tile an array*

---

**Description**

Repeat copies of array (equivalent of the repmat matlab function).

**Usage**

```
repmat(a, n, m)
```

**Arguments**

a                   input array (scalar, vector, matrix).  
n                   number of time to repeat input array in row and column dimensions.  
m                   repetition factor.

**Examples**

```
repmat(10,3,2)
```

---

rshift                      *Circular right shift of 1-d signal*

---

**Description**

Circular right shift of 1-d signal

**Usage**

```
rshift(a)
```

**Arguments**

a                      1-d signal.

**Value**

r 1-d signal  $r(i) = x(i-1)$  except  $r(1) = x(n)$ .

**Examples**

```
x <- MakeSignal('HeaviSine', 2^3)
rshift(x)
```

---

ShapeAsRow                      *Make signal a row vector*

---

**Description**

Make signal a row vector

**Usage**

```
ShapeAsRow(sig)
```

**Arguments**

sig                      a row or column vector.

**Value**

row a row vector.

**Examples**

```
sig <- matrix(1:4)
row <- ShapeAsRow(sig)
```

---

SLphantom	<i>3-d Shepp-Logan phantom</i>
-----------	--------------------------------

---

**Description**

A dataset containing a 3d head phantom that can be used to test 3-d reconstruction algorithms. Shepp-Logan phantom is well-known imitation of human cerebral.

**Usage**

```
data(SLphantom)
```

**Format**

A numeric array of size 64x64x64.

---

SNR	<i>Signal/Noise ratio</i>
-----	---------------------------

---

**Description**

Signal/Noise ratio

**Usage**

```
SNR(x, y)
```

**Arguments**

x	Original reference signal.
y	Restored or noisy signal.

**Value**

Signal/Noise ratio.

**Examples**

```
n <- 2^4
x <- MakeSignal('HeaviSine', n)
y <- x + rnorm(n, mean=0, sd=1)
SNR(x, y)
```

SoftThresh

*Apply Soft Threshold*

---

**Description**

Apply Soft Threshold

**Usage**

```
SoftThresh(y, t)
```

**Arguments**

y	Noisy Data.
t	Threshold.

**Value**

x filtered result ( $y - |y| > t$ ).

**See Also**

[HardThresh](#)

**Examples**

```
f <- MakeSignal('HeaviSine', 2^3)
qmf <- MakeONFilter('Daubechies', 10)
L <- 0
wc <- FWT_PO(f, L, qmf)
thr <- 2
wct <- SoftThresh(wc, thr)
fsoft <- IWT_PO(wct, L, qmf)
```

---

SUREThresh*Adaptive Threshold Selection Using Principle of SURE*

---

**Description**

SURE refers to Stein's Unbiased Risk Estimate.

**Usage**

```
SUREThresh(y)
```

**Arguments**

y Noisy Data with Std. Deviation = 1.

**Value**

x Estimate of mean vector

thresh Threshold used.

---

UpDyadHi

*Hi-Pass Upsampling operator; periodized*

---

**Description**

Hi-Pass Upsampling operator; periodized

**Usage**

```
UpDyadHi(x, qmf)
```

**Arguments**

x 1-d signal at coarser scale.

qmf filter.

**Value**

u 1-d signal at finer scale.

**See Also**

[DownDyadLo](#), [DownDyadHi](#), [UpDyadLo](#), [IWT\\_PO](#), [aconv](#).

**Examples**

```
qmf <- MakeONFilter('Haar')
x <- MakeSignal('HeaviSine', 2^3)
UpDyadHi(x, qmf)
```

---

UpDyadLo *Lo-Pass Upsampling operator; periodized*

---

**Description**

Lo-Pass Upsampling operator; periodized

**Usage**

UpDyadLo(x, qmf)

**Arguments**

x                    1-d signal at coarser scale.  
 qmf                  filter.

**Value**

y 1-d signal at finer scale.

**See Also**

[DownDyadLo](#), [DownDyadHi](#), [UpDyadHi](#), [IWT\\_PO](#), [iconvv](#).

**Examples**

```
qmf <- MakeONFilter('Haar')
x <- MakeSignal('HeaviSine', 2^3)
UpDyadLo(x, qmf)
```

---

UpSampleN *Upsampling operator*

---

**Description**

Upsampling operator

**Usage**

UpSampleN(x, s)

**Arguments**

x                    1-d signal, of length n.  
 s                    upsampling scale, default = 2.

**Value**

y 1-d signal, of length  $s*n$  with zeros interpolating alternate samples  $y(s*i-1) = x(i)$ ,  $i=1,\dots,n$

---

ValSUREThresh

*Adaptive Threshold Selection Using Principle of SURE*


---

**Description**

SURE refers to Stein's Unbiased Risk Estimate.

**Usage**

ValSUREThresh(x)

**Arguments**

x                      Noisy Data with Std. Deviation = 1.

**Value**

thresh Value of Threshold.

---

VisuThresh

*Visually calibrated Adaptive Smoothing*


---

**Description**

Visually calibrated Adaptive Smoothing

**Usage**

VisuThresh(y, thresh = "soft")

**Arguments**

y                      Signal upon which to perform visually calibrated Adaptive Smoothing.  
 thresh                'hard' or 'soft'.

**Value**

x result of applying VisuThresh.

**References**

D.L. Donoho and I.M. Johnstone (1994). Ideal spatial adaptation by wavelet shrinkage. *Biometrika*, 81(3), 425–455.

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